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**Information technology — Security  
techniques — Signcryption**

*Technologies de l'information — Techniques de sécurité —  
Signcryptage*

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## Foreword

ISO (the International Organization for Standardization) and IEC (the International Electrotechnical Commission) form the specialized system for worldwide standardization. National bodies that are members of ISO or IEC participate in the development of International Standards through technical committees established by the respective organization to deal with particular fields of technical activity. ISO and IEC technical committees collaborate in fields of mutual interest. Other international organizations, governmental and non-governmental, in liaison with ISO and IEC, also take part in the work. In the field of information technology, ISO and IEC have established a joint technical committee, ISO/IEC JTC 1.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of the joint technical committee is to prepare International Standards. Draft International Standards adopted by the joint technical committee are circulated to national bodies for voting. Publication as an International Standard requires approval by at least 75 % of the national bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO and IEC shall not be held responsible for identifying any or all such patent rights.

ISO/IEC 29150 was prepared by Joint Technical Committee ISO/IEC JTC 1, *Information technology*, Subcommittee SC 27, *IT Security techniques*.

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## Introduction

When data is sent from one place to another, it is often necessary to protect it in some way whilst it is in transit, e.g. against eavesdropping or unauthorized modification. Similarly, when data is stored in an environment to which unauthorized parties can have access, it is important to protect it against unauthorized access.

If the confidentiality of the data needs to be protected, e.g. against eavesdropping, then one solution is to use public key encryption, as specified in ISO/IEC 18033. Alternatively, if it is necessary to protect the data against unauthorized modification or forgery, then digital signatures, as specified in ISO/IEC 9796 and ISO/IEC 14888, can be used. If both confidentiality and unforgeability are required, then one possibility is to use both public key encryption and digital signature. Whilst these operations can be combined in many ways, not all combinations of such mechanisms provide the same security guarantees. As a result it is desirable to define in detail exactly how confidentiality and unforgeability mechanisms should be combined to provide the optimum level of security. Moreover, in some cases significant efficiency gains can be obtained by defining a single method of processing the data with the objective of providing both confidentiality and unforgeability.

In this International Standard, *signcryption mechanisms* are defined. These are methods for processing data to provide both confidentiality and unforgeability. These data processing methods typically involve either the use of an asymmetric encryption scheme and a digital signature scheme combined in a specific way or the use of a specially developed algorithm which fulfils both functions simultaneously.

The methods specified in this International Standard have been designed to maximise the level of security and provide efficient processing of data. All the mechanisms defined here have mathematical “proofs of security”, i.e. rigorous arguments supporting their security claims.

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# Information technology — Security techniques — Signcryption

## 1 Scope

This International Standard specifies four mechanisms for signcryption that employ public key cryptographic techniques requiring both the originator and the recipient of protected data to have their own public and private key pairs.

This International Standard is not applicable to infrastructures for management of public keys which are defined in ISO/IEC 11770-1 and ISO/IEC 9594.

NOTE 1 Signcryption mechanisms are defined ways of processing a data string with the following security objectives:

- **data confidentiality**, i.e. protection against unauthorized disclosure of data;
- **data integrity**, i.e. protection that enables the recipient of data to verify that it has not been modified;
- **data origin authentication**, i.e. protection that enables the recipient of data to verify the identity of the data originator;
- **data unforgeability**, i.e. protection against unauthorized modification of data, even by a recipient of the data.

These four security objectives are not necessarily mutually exclusive. The fourth objective, data unforgeability, in particular is a stronger notion of security that implies both data integrity and data origin authentication.

NOTE 2 Two of the mechanisms specified in this International Standard, namely mechanisms DLSC and ECDLSC, require the employment of system wide public key parameters for both the sender and the recipient of data. In a system where a multiple number of pairs of senders and recipients exist, the same system wide parameters are required to be used by all these users. The two remaining specified mechanisms, namely IFSC and EtS, do not require the use of such system wide public key parameters.

NOTE 3 In selecting the four signcryption mechanisms for inclusion in this International Standard from the large variety of such techniques published and in use, the same seven criteria as those stated in ISO/IEC 18033-1:2005, Annex A, have been followed. The exclusion of particular methods does not imply that those methods are insecure.

NOTE 4 This International Standard bears a conceptual similarity to ISO/IEC 19772<sup>[14]</sup> which specifies a number of mechanisms for authenticated encryption, that is, simultaneously achieving message integrity and confidentiality. Major differences between ISO/IEC 19772 and this International Standard include (1) mechanisms specified in ISO/IEC 19772 fall into the category of symmetric cryptographic techniques, whereas those specified in this International Standard are representatives of asymmetric cryptographic techniques; (2) while all mechanisms specified in ISO/IEC 19772 and this International Standard offer the capability of data integrity and origin authentication, mechanisms specified in this International Standard further offer the capability of data unforgeability, even by a recipient of the data.

## 2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO/IEC 9796-2:2010, *Information technology — Security techniques — Digital signature schemes giving message recovery — Part 2: Integer factorization based mechanisms*

ISO/IEC 9796-3:2006, *Information technology — Security techniques — Digital signature schemes giving message recovery — Part 3: Discrete logarithm based mechanisms*

ISO/IEC 14888-1:2008, *Information technology — Security techniques — Digital signatures with appendix — Part 1: General*

ISO/IEC 14888-2:2008, *Information technology — Security techniques — Digital signatures with appendix — Part 2: Integer factorization based mechanisms*

ISO/IEC 14888-3:2006, *Information technology — Security techniques — Digital signatures with appendix — Part 3: Discrete logarithm based mechanisms*

ISO/IEC 18033-1:2005, *Information technology — Security techniques — Encryption algorithms — Part 1: General*

ISO/IEC 18033-2:2006, *Information technology — Security techniques — Encryption algorithms — Part 2: Asymmetric ciphers*

### 3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

- 3.1**  
**asymmetric cipher**  
alternative term for asymmetric encryption system  
[ISO/IEC 18033-1:2005]
- 3.2**  
**asymmetric cryptographic technique**  
cryptographic technique that uses two related transformations, a public transformation (defined by the public key) and a private transformation (defined by the private key)  
[ISO/IEC 11770-1:2010]
- 3.3**  
**asymmetric encryption system**  
system based on asymmetric cryptographic techniques whose public transformation is used for encryption and whose private transformation is used for decryption  
[ISO/IEC 9798-1:2010]
- 3.4**  
**asymmetric key pair**  
pair of related keys where the private key defines the private transformation and the public key defines the public transformation  
[ISO/IEC 9798-1:2010]
- 3.5**  
**block**  
string of bits of a defined length

**3.6****block cipher**

symmetric encryption system with the property that encryption operates on a block of plaintext, i.e. a string of bits of a defined length, to yield a block of ciphertext, and decryption operates on the ciphertext to yield the original plaintext

[ISO/IEC 18033-1:2005]

**3.7****cipher**

alternative term for encryption system

[ISO/IEC 18033-1:2005]

**3.8****ciphertext**

data which has been transformed to hide its information content

[ISO/IEC 10116:2006]

**3.9****cleartext**

alternative term for plaintext

**3.10****collision-resistant hash-function**

hash-function satisfying the following property: it is computationally infeasible to find any two distinct inputs which map to the same output

[ISO/IEC 10118-1:2000]

**3.11****data element**

integer or bit string or set of integers or set of bit strings

**3.12****decryption**

reversal of encryption by a cryptographic algorithm to produce a plaintext

**3.13****decryption algorithm**

process which transforms a ciphertext into a plaintext

[ISO/IEC 18033-1:2005]

**3.14****domain**

set of entities operating under a single security policy

[ISO/IEC 14888-1:2008]

**3.15****domain parameter**

data element which is common to and known by or accessible to all entities within the domain

[ISO/IEC 14888-1:2008]

**3.16**  
**encryption**

(reversible) transformation of data by a cryptographic algorithm to produce a ciphertext, i.e. to hide the information content of the data

NOTE Adapted from ISO/IEC 9797-1:2011.

**3.17**  
**encryption algorithm**

process which transforms a plaintext into a ciphertext

[ISO/IEC 18033-1:2005]

**3.18**  
**encryption system**

cryptographic technique used to protect the confidentiality of data, and which consists of three component processes: a method for generating keys, an encryption algorithm and a decryption algorithm

**3.19**  
**full domain cryptographic hash function**

function that maps strings of bits to integers in a fixed range, satisfying the properties of (1) for a given output, it is computationally infeasible to find an input which maps to this output, and (2) for a given input, it is computationally infeasible to find a second input which maps to the same output

NOTE A full domain cryptographic hash function is similar to a standard cryptographic hash function with the exception that the former outputs an integer rather than a bit string; see 7.2.2.

**3.20**  
**identification data**

sequence of data elements, including the distinguishing identifier for an entity, assigned to an entity and used to identify it

NOTE The identification data can additionally contain data elements such as identifier of the signature process, identifier of the signature key, validity period of the signature key, restrictions on key usage, associated security policy parameters, key serial number, or domain parameters.

[ISO/IEC 14888-1:2008]

**3.21**  
**key**

sequence of symbols that controls the operation of a cryptographic transformation (e.g. encryption, decryption)

[ISO/IEC 11770-1:2010]

**3.22**  
**key pair**

pair consisting of a public key and a private key associated with an asymmetric cipher

**3.23**  
**keystream**

pseudorandom sequence of symbols, intended to be secret, used by the encryption and decryption algorithms of a stream cipher

NOTE If a portion of the keystream is known by an attacker, then it is computationally infeasible for the attacker to deduce any information about the remainder of the keystream.

**3.24**  
**message**

string of bits of any length

**3.25*****n*-bit block cipher**

block cipher with the property that plaintext blocks and ciphertext blocks are *n* bits in length

[ISO/IEC 10116:2006]

**3.26****one-way hash function**

function which maps strings of bits to fixed-length strings of bits, satisfying the following two properties:

- for a given output, it is computationally infeasible to find an input which maps to this output;
- for a given input, it is computationally infeasible to find a second input which maps to the same output

[ISO/IEC 10118-1:2000]

**3.27****parameter**

integer or bit string or function

**3.28****plaintext**

unencrypted information

[ISO/IEC 10116:2006]

**3.29****private key**

that key of a key pair associated with an entity's asymmetric cipher which is kept secret and used by that entity only

[ISO/IEC 11770-1:2010]

**3.30****public key**

that key of a key pair associated with an entity's asymmetric cipher which can be made public and used by any entity

[ISO/IEC 11770-1:2010]

**3.31****secret key**

key used with symmetric cryptographic techniques by a specified set of entities

[ISO/IEC 11770-3:2008]

**3.32****signature**

one or more data elements resulting from the signature process

**3.33****signature key**

set of private data elements specific to an entity and usable only by this entity in the signature process

[ISO/IEC 14888-1:2008]

**3.34****signature process**

process which takes as inputs the message, the signature key and the domain parameters, and which gives as output the signature

**3.35**

**signcrypt**

to apply signcryption on a plaintext

**3.36**

**signcryption**

(reversible) transformation of data by a cryptographic algorithm to produce a ciphertext from which no information about the original data can be recovered (except possibly its length), nor can a new ciphertext be forged by an unauthorized entity without detection, that is, it provides data confidentiality, data integrity, data origin authentication, and non-repudiation

NOTE Unforgeability implies data integrity, data origin authentication, and non-repudiation.

**3.37**

**signcryption algorithm**

one of the three component algorithms of a signcryption mechanism which takes as input a plaintext, a sender's public and private key pair, a recipient's public key and other data, outputs a ciphertext after performing a sequence of specified operations on the input

**3.38**

**signcryption mechanism**

cryptographic technique used to protect the confidentiality and simultaneously guarantee the origin, integrity and non-repudiation of data, and which consists of three component algorithms: a key generation algorithm, a signcryption algorithm and a unisigncryption algorithm

**3.39**

**signed message**

set of data elements consisting of the signature, the part of the message which cannot be recovered from the signature, and an optional text field

[ISO/IEC 14888-1:2008]

**3.40**

**symmetric cipher**

cipher based on symmetric cryptographic techniques that uses the same secret key for both the encryption and decryption algorithms

[ISO/IEC 18033-1:2005]

**3.41**

**symmetric cryptographic technique**

cryptographic technique that uses the same secret key for both the originator's and the recipient's transformation

NOTE 1 Without knowledge of the secret key, it is computationally infeasible to compute either the originator's or the recipient's transformation.

NOTE 2 Examples of symmetric cryptographic techniques include symmetric ciphers and Message Authentication Codes (MACs). In a symmetric cipher, the same secret key is used to encrypt and decrypt data. In a MAC, the same secret key is used to generate and verify MACs.

**3.42**

**unisigncrypt**

to apply unisigncryption on a ciphertext

**3.43**

**unisigncryption**

verification and decryption of a ciphertext by a cryptographic algorithm

**3.44****unsigned encryption algorithm**

one of the three component algorithms of a signcryption mechanism which takes as input a ciphertext, a recipient's public and private key pair, a sender's public key and other data, outputs a pair consisting of either a symbolic value ACCEPT and a plaintext, or a symbolic value REJECT and the null string

**3.45****verification key**

set of public data elements which is mathematically related to an entity's signature key and which is used by the verifier in the verification process

[ISO/IEC 14888-1:2008]

**3.46****verification process**

process which takes as input the signed message, the verification key and the domain parameters, and which gives as output the result of the signature verification: valid or invalid

[ISO/IEC 14888-1:2008]

**4 Symbols and notations**

For the purposes of this International Standard, the following symbols and notations apply:

$\lfloor x \rfloor$	the largest integer less than or equal to real number $x$ . For example, $\lfloor 8 \rfloor = 8$ , $\lfloor 8.7 \rfloor = 8$ and $\lfloor -10.4 \rfloor = -11$ .
$\lceil x \rceil$	the smallest integer greater than or equal to real number $x$ . For example, $\lceil 8 \rceil = 8$ , $\lceil 8.2 \rceil = 9$ , and $\lceil -9.5 \rceil = -9$ .
$[a, \dots, b]$	the interval of integers from $a$ to $b$ , including both $a$ and $b$ .
$(a, \dots, b)$	the interval of integers from $a$ to $b$ , but excluding both $a$ and $b$ .
$ X $	if $X$ is a finite set, then the cardinality of $X$ , namely the number of elements in the set $X$ ; if $X$ is a finite abelian group or a finite field, then the cardinality of the underlying set of elements; if $X$ is a real number, then the absolute value of $X$ ; if $X$ is a bit string, then the length in bits of the string.
$x \oplus y$	the bit-wise exclusive-or (XOR) of two bit strings $x$ and $y$ , where $x$ and $y$ are of equal length. (See also 6.1.)
$\langle x_1, \dots, x_l \rangle$	the bit string of length $l$ consisting of $l$ bits $x_1, \dots, x_l$ in the given order. (See also 6.1.)
$x \parallel y$	The result of concatenating two data items $x$ and $y$ in the order specified. In cases where the result of concatenating two or more data items is input to a cryptographic algorithm as part of a signcryption mechanism, this result shall be composed so that it can be uniquely resolved into its constituent data strings, i.e. so that there is no possibility of ambiguity in interpretation. This latter property can be achieved in a variety of different ways, depending on the application. For example, it can be guaranteed by (a) fixing the length of each of the substrings throughout the domain of use of the mechanism, or (b) encoding the sequence of concatenated strings using a method that guarantees unique decoding, e.g. using the distinguished encoding rules defined in ISO/IEC 8825-1 [6].
$\gcd(a, b)$	the greatest common divisor of two integers $a$ and $b$ .
$a   b$	integer $a$ divides integer $b$ ; that is, there exists an integer $c$ such that $b = ca$ .

$a \equiv b \pmod{n}$	integer $a$ and integer $b$ are congruent modulo non-zero integer $n$ ; that is $n (a-b)$ .
$a \bmod n$	the unique remainder in $[0, \dots, n-1]$ when integer $a$ is divided by positive integer $n$ .
$a^{-1} \bmod n$	for integer $a$ and positive integer $n$ such that $\gcd(a, n) = 1$ , the unique integer $b$ in $[1, \dots, n-1]$ such that $ab \equiv 1 \pmod{n}$ .
$L_b(n)$	the length in bits of a non-negative integer $n$ , or the smallest integer $l$ such that I2BSP( $n, l$ ) does not fail; that is, $L_b(n) = \lceil \log_2(n+1) \rceil$ , where I2BSP( $n, l$ ), defined in 6.2, converts integer $n$ to a bit string of length $l$ .
<i>AC.Decrypt</i>	decryption algorithm for an asymmetric cipher.
<i>AC.Encrypt</i>	encryption algorithm for an asymmetric cipher.
<i>AC.KeyGen</i>	key generation algorithm for an asymmetric cipher.
$ID_X$	bit string which uniquely identifies entity $X$ in some context.
$pk_d$	private decryption key.
$pk_s$	private signature generation key.
$pk_X$	private key belonging to the entity $X$ .
$pk_{X,d}$	private decryption key belonging to the entity $X$ .
$pk_{X,s}$	private signature generation key belonging to the entity $X$ .
$PK_e$	public encryption key.
$PK_v$	public signature verification key.
$PK_X$	public key belonging to the entity $X$ .
$PK_{X,e}$	public encryption key belonging to the entity $X$ .
$PK_{X,v}$	public signature verification key belonging to the entity $X$ .
<i>SS.KeyGen</i>	key generation algorithm for a signature scheme.
<i>SS.Sign</i>	signature generation algorithm for a signature scheme.
<i>SS.Verify</i>	signature verification algorithm for a signature scheme.

## 5 Finite fields and elliptic curves

### 5.1 Finite fields

This clause describes a very general framework for representing specific finite fields. A finite field specified in this way is called an explicitly given finite field, and it is determined by explicit data.

For a finite field  $F$  of cardinality  $p^e$ , where  $p$  is prime and  $e \geq 1$ , explicit data for  $F$  consists of  $p$  and  $e$ , along with a “multiplication table” which is a matrix  $T = (T_{ij})_{1 \leq i, j \leq e}$ , where each  $T_{ij}$  is an  $e$ -tuple, or an ordered list of  $e$  elements, over  $[0, \dots, p-1]$ .

The set of elements of  $F$  is the set of all  $e$ -tuples over  $[0, \dots, p-1]$ . The entries of  $T$  are themselves viewed as elements of  $F$ .

Addition in  $F$  is defined element-wise: if  $a = (a_1, \dots, a_e) \in F$  and  $b = (b_1, \dots, b_e) \in F$ , then  $a + b = c$ , where

$$c = (c_1, \dots, c_e) \text{ and } c_i = (a_i + b_i) \bmod p \ (1 \leq i \leq e).$$

A scalar multiplication operation for  $F$  is also defined element-wise: if  $a = (a_1, \dots, a_e) \in F$  and  $d \in [0, \dots, p-1]$ , then  $d \cdot a = c$ , where

$$c = (c_1, \dots, c_e) \text{ and } c_i = (d \cdot a_i) \bmod p \ (1 \leq i \leq e).$$

Multiplication in  $F$  is defined via the multiplication table  $T$ , as follows: if  $a = (a_1, \dots, a_e) \in F$  and  $b = (b_1, \dots, b_e) \in F$ , then

$$a \cdot b = \sum_{i=1}^e \sum_{j=1}^e [(a_i b_j \bmod p) T_{ij}]$$

where the products  $(a_i b_j \bmod p) T_{ij}$  are defined using the above rule for scalar multiplication, and where these products are summed using the above rule for addition in  $F$ . It is assumed that the multiplication table defines an algebraic structure that satisfies the usual axioms of a field; in particular, there exist additive and multiplicative identities, every element has an additive inverse, and every element besides the additive identity has a multiplicative inverse.

Observe that the additive identity of  $F$ , denoted  $0_F$ , is the all-zero  $e$ -tuple, and that the multiplicative identity of  $F$ , denoted  $1_F$ , is a non-zero  $e$ -tuple whose precise format depends on  $T$ .

NOTE 1 The field  $F$  is a vector space of dimension  $e$  over the prime field  $F'$  of cardinality  $p$ , where scalar multiplication is defined as above. The prime  $p$  is called the characteristic of  $F$ . For  $1 \leq i \leq e$ , let  $\theta_i$  denote the  $e$ -tuple over  $F'$  whose  $i$ -th component is 1, and all of whose other components are 0. The elements  $\theta_1, \dots, \theta_e$  form an ordered basis of  $F$  as a vector space over  $F'$ . Note that for  $1 \leq i, j \leq e$ , we have  $\theta_i \cdot \theta_j = T_{ij}$ .

NOTE 2 For  $e > 1$ , two types of standard bases are defined that are commonly used in implementations of finite field arithmetic, namely *polynomial basis* and *normal basis*.

- Polynomial basis:  $\theta_1, \dots, \theta_e$  are called a polynomial basis for  $F$  over  $F'$  if for some  $\theta \in F$ ,  $\theta_i = \theta^{e-i}$  for  $1 \leq i \leq e$ . Note that in this case,  $1_F = \theta_e$ .
- Normal basis:  $\theta_1, \dots, \theta_e$  are called a normal basis for  $F$  over  $F'$  if for some  $\theta \in F$ ,  $\theta_i = \theta^{p^{i-1}}$  for  $1 \leq i \leq e$ . Note that in this case,  $1_F = c \sum_{i=1}^e \theta_i$  for some  $c \in [1, \dots, p]$ ; if  $p = 2$ , then the only possible choice for  $c$  is 1; moreover, one can always choose a normal basis for which  $c = 1$ .

NOTE 3 The definition given here of an explicitly given finite field comes from ISO/IEC 18033-2.

## 5.2 Elliptic curves

An elliptic curve  $V$  over an explicitly given finite field  $F$  is a set of points  $P = (x, y)$ , where  $x$  and  $y$  are elements of  $F$  that satisfy a certain equation, together with the “point at infinity” which is denoted by  $O$ . For the purposes of this International Standard, the curve  $V$  is specified by two field elements  $a, b \in F$ , called the coefficients of  $V$ .

Let  $p$  be the characteristic of  $F$ . An elliptic curve  $V$  over  $F$  falls into one of the following three categories, which is determined by the value of  $p$ :

- $p = 2$ :  $b$  shall satisfy  $b \neq 0_F$ , and every point  $P = (x, y)$  on  $V$  (other than the point at infinity  $O$ ) shall satisfy an equation of the form  $y^2 + xy = x^3 + ax^2 + b$ ;
- $p = 3$ :  $a$  and  $b$  shall satisfy  $a \neq 0_F$  and  $b \neq 0_F$ , and every point  $P = (x, y)$  on  $V$  (other than  $O$ ) shall satisfy an equation of the form  $y^2 = x^3 + ax^2 + b$ ;
- $p > 3$ :  $a$  and  $b$  shall satisfy  $4a^3 + 27b^2 \neq 0_F$ , and every point  $P = (x, y)$  on  $V$  (other than  $O$ ) shall satisfy an equation of the form  $y^2 = x^3 + ax + b$ .

Elliptic curves are endowed with the addition operation  $+: V \times V \rightarrow V$ , defining for each pair  $(P, Q)$  of points on  $V$  a third point  $P + Q$ . With respect to this addition,  $V$  is an abelian group with identity element  $O$ . If  $P + Q = O$ , then  $Q$  is called the additive inverse of  $P$ , which is denoted by  $-P$ . The  $k$ -th multiple of a point  $P$  is given as  $kP$ , where  $kP = P + \dots + P$  ( $k$  summands) if  $k > 0$ ,  $kP = (-k)(-P)$  if  $k < 0$ , and  $kP = O$  if  $k = 0$ . The smallest positive  $k$  with  $kP = O$  is called the order of  $P$ .

There exist efficient algorithms to perform the group operation of an elliptic curve, but the implementation of such algorithms is out of the scope of this International Standard.

A point  $P$  (other than  $O$ ) on an elliptic curve can be represented in compressed, uncompressed, or hybrid form.

If  $P = (x, y)$ , then  $(x, y)$  is the *uncompressed* form of  $P$ . The *compressed* form of  $P$  is denoted by  $(x, \tilde{y})$  where  $\tilde{y} \in \{0, 1\}$ . The *hybrid* form of  $P = (x, y)$  is the triple  $(x, \tilde{y}, y)$ , where  $\tilde{y}$  is as in the compressed form. Given  $(x, \tilde{y})$ , the compressed form of  $P$ , there exist efficient procedures for point *decompression*, i.e., computing  $y$  from  $(x, \tilde{y})$ .

NOTE Information on the implementation of the elliptic curve group operations can be found in ISO/IEC 15946-1.

## 6 Conversion functions

### 6.1 Bits and strings

A bit is one of the two symbols '0' and '1'. A bit string is a sequence of bits. For  $l$  bits  $x_1, \dots, x_l$ , the bit string consisting of the  $l$  bits, appearing in the given order, is denoted by  $\langle x_1, \dots, x_l \rangle$ .

For a bit string  $x = \langle x_1, \dots, x_l \rangle$ , the length  $l$  of the string is denoted by  $|x|$ . The left most bit  $x_1$  is called the first, highest order or most significant bit of the string. Likewise, the right most bit  $x_l$  is called the last, lowest order or least significant bit of the string.

Given two bit strings  $x = \langle x_1, \dots, x_l \rangle$  and  $y = \langle y_1, \dots, y_m \rangle$ , the concatenation of  $x$  and  $y$  is defined by  $x \parallel y = \langle x_1, \dots, x_l, y_1, \dots, y_m \rangle$ .

For two bit strings of equal length,  $x$  and  $y$ , their bit-wise exclusive-or (XOR) is denoted by  $x \oplus y$ .

A null bit string, denoted by NULL, is a string of length 0.

## 6.2 Conversion between bit strings and integers

BS2IP( $x$ ) takes as input a bit string  $x = \langle x_{m-1}, \dots, x_0 \rangle$ , and outputs the unique integer value  $n$  defined by  $n = \sum_{i=0}^{m-1} (v_i 2^i)$ , where  $v_i = \begin{cases} 0, & \text{if } x_i = '0' \\ 1, & \text{if } x_i = '1' \end{cases}$ .

I2BSP( $n, l$ ) takes as input two non-negative integers  $n$  and  $l$ , and outputs the unique bit string  $x$  of length  $l$  such that  $n = \text{BS2IP}(x)$ , if such an  $x$  exists. Otherwise the function **fails**.

## 6.3 Conversion between finite field elements and integers/bit strings

FE2IP $_F$ ( $a$ ) takes as input an element  $a$  of a given finite field  $F$ , and outputs an integer value  $n$  as follows:

If the cardinality of  $F$  is  $q = p^m$ , where  $p$  is prime and  $m \geq 1$ , then an element  $a$  of  $F$  is an  $m$ -tuple  $(a_1, \dots, a_m)$ , where  $a_i \in [0, \dots, p)$  for  $1 \leq i \leq m$ , and the value  $n$  is defined as  $n = \sum_{i=1}^m a_i p^{i-1}$ .

FE2BSP $_F$ ( $a$ ) takes as input an element  $a$  of a given finite field  $F$ , and outputs the bit string I2BSP( $n, l$ ), where  $n = \text{FE2IP}_F(a)$  and  $l = \lceil \log_2 |F| \rceil$ .

BS2FEP $_F$ ( $x$ ) takes as input a bit string  $x$ , and outputs the unique field element  $a$  of  $F$  such that  $x = \text{FE2BSP}_F(a)$ , if such an  $a$  exists. Otherwise the function **fails**.

## 6.4 Conversion between points on elliptic curves and bit strings

EC2BSP $_V$ ( $P, fmt$ ) takes as input an element  $P$  on a given elliptic curve  $V$ , over an explicitly given finite field  $F$ , together with a format specifier  $fmt$ , which is one of the three symbolic values *compressed*, *uncompressed*, or *hybrid*, and outputs a bit string  $EP$  according to rules specified below.

1) If  $P = O$ , then  $EP = '0'$  (the '0' bit).

2) If  $P \neq O$ , then computing  $EP$  is dictated by the value of  $fmt$ . Specifically,

2.1) when  $fmt = \textit{hybrid}$ , that is  $P = (x, \tilde{y}, y)$ ,  $EP$  is defined as  $EP = \text{I2BSP}(6 + \tilde{y}, 3) \parallel \text{FE2BSP}_F(x) \parallel \text{FE2BSP}_F(y)$ ;

2.2) when  $fmt = \textit{uncompressed}$ , that is  $P = (x, y)$ ,  $EP$  is defined as  $EP = \text{I2BSP}(4, 3) \parallel \text{FE2BSP}_F(x) \parallel \text{FE2BSP}_F(y)$ ;

2.3) when  $fmt = \textit{compressed}$ , that is  $P = (x, \tilde{y})$ ,  $EP$  is defined as  $EP = \text{I2BSP}(2 + \tilde{y}, 3) \parallel \text{FE2BSP}_F(x)$ .

BS2ECP $_V$ ( $EP$ ) takes as input a bit string  $EP$ , and outputs a point  $P$ , in uncompressed form, on a given elliptic curve  $V$  such that  $EP = \text{EC2BSP}_V(P, fmt)$  for a format specifier  $fmt$ , if such a point  $P$  exists. Otherwise the function **fails**.

NOTE 1  $L_b$  is defined in Clause 4.

NOTE 2 Other than FE2BSP, BS2FEP, EC2BSP and BS2ECP, the conversion functions are defined in ISO/IEC 15946-1:2008, Clause 6 (see [12]).

## 7 Cryptographic transformations

### 7.1 Introduction

This clause describes several cryptographic transformations that will be referred to in subsequent clauses. The types of transformations are cryptographic hash functions and key derivation functions. For each type of transformation, the abstract input/output characteristics are given, and then specific implementations of these transformations that are allowed for use in this International Standard are specified.

### 7.2 Cryptographic hash functions

#### 7.2.1 Standard cryptographic hash functions

A (standard) cryptographic hash function is essentially a function that maps a bit string of variable length to a bit string of fixed length. More precisely, a cryptographic hash function *Hash* specifies

- a positive integer *Hash.Len* that denotes the length of the hash function output,
- a positive integer *Hash.MaxInputLen* that denotes the maximum length of the hash function input, and
- a function *Hash.Eval* that denotes the hash function itself, which maps bit strings of length at most *Hash.MaxInputLen* to bit strings of length *Hash.Len*.

The invocation of *Hash.Eval* fails if and only if the input length exceeds *Hash.MaxInputLen*.

When an input to a standard cryptographic hash function consists of several bit strings, these bit strings will be concatenated first, in the order these bit strings are given, to form a single bit string prior to the application of a hash operation.

For the purposes of this International Standard, the allowable standard cryptographic hash functions shall be those described in ISO/IEC 10118-2 and ISO/IEC 10118-3 (see [10]) with the following proviso:

- Whereas the hash functions in ISO/IEC 10118 are not defined for inputs exceeding a given length, a hash function in this International Standard is defined to fail for such inputs.

#### 7.2.2 Full domain cryptographic hash functions

##### 7.2.2.1 General

A full domain cryptographic hash function is a hash function that maps a bit string of arbitrary length to an integer in a fixed range. More precisely, a full domain cryptographic hash function *FDH* specifies

- a positive integer *FDH.Range* that defines the allowable range of the hash function output, i.e. the hash function outputs an integer in the range of  $[0, \dots, FDH.Range - 1]$ ,
- a positive integer *FDH.MaxInputLen* that denotes the maximum length of the hash function input, and
- a function *FDH.Eval* that denotes the hash function itself, which maps bit strings of length at most *FDH.MaxInputLen* to non-negative integers smaller than *FDH.Range*.

Analogous to a standard cryptographic hash function, when an input to a full domain cryptographic hash function consists of several bit strings, these bit strings will be concatenated first, in the order these bit strings are given, to form a single bit string prior to the application of a hash operation.

The invocation of *FDH.Eval* fails if the length of the hash function input exceeds *FDH.MaxInputLen*. It may also fail in other events that are dependent on specific implementations. An example of such a failure event is when internal operations of *FDH.Eval* transcend a pre-determined maximum allowable number of iterations without producing a valid output.

### 7.2.2.2 Allowable full domain cryptographic hash function (FDH1)

FDH1 is a family of full domain cryptographic hash functions parameterised by a system parameter denoted by *Hash* which is a (standard) cryptographic hash function, as is described in 7.2.1, with the property that its output length in bits, *Hash.Len*, is at least  $\lceil \log_2 FDH1.Range \rceil$ .

FDH1 inherits *Hash.MaxInputLen* as its own *FDH1.MaxInputLen* for the maximum length of input bit strings.

Given an input bit string  $x$ , *FDH1.Eval(x)* shall work as follows to produce an integer in the range of  $[0, \dots, FDH1.Range-1]$ . It shall indicate failure when the length of  $x$  exceeds  $(FDH1.MaxInputLen - 64)$ , or in an extremely rare event when the “while” loop iterates  $2^{64}$  times without bringing forth a valid integer output in the range of  $[0, \dots, FDH1.Range-1]$ .

1. If  $|x|+64 > FDH1.MaxInputLen$  then FDH1 **fails**.
2. *Counter* = 0.
3. While *Counter* <  $2^{64}$  do:
  - a. Compute  $y = Hash.Eval(x \parallel I2BSP(Counter, 64))$ ;
  - b. Set  $z$  to the  $\lceil \log_2 FDH1.Range \rceil$  left most / higher order bits of  $y$ ;
  - c. If  $BS2IP(z) < FDH1.Range$  then output  $BS2IP(z)$  and quit the procedure;
  - d. Increase the value of *Counter* by 1.
4. FDH1 **fails**.

## 7.3 Key derivation functions

A key derivation function is a function  $KDF(x, l)$  that takes as input a seed  $x$ , which is a bit string, and a positive integer  $l$ , and outputs a bit string of length  $l$ . The string  $x$  is of arbitrary length, although an implementation may define a (very large) maximum length for  $x$  and maximum size for  $l$ , and fail if these bounds are exceeded.

The key derivation functions that are allowed in this International Standard shall be KDF1 and KDF2, as described in ISO/IEC 18033-2, with the following proviso:

- The key derivation functions described in ISO/IEC 18033-2 map octet strings to octet strings, whereas in this International Standard, they map bit strings to bit strings. (An octet is a bit string of length 8.) Mapping between octet strings and bit strings is affected by conversions OS2BSP and BS2OSP which are defined in ISO/IEC 18033-2.

NOTE KDF1 and KDF2 are the same except that the internal counter of KDF1 starts at 0 whereas the internal counter of KDF2 starts at 1.

## 8 General model for signcryption

A signcryption mechanism *SC* consists of three algorithms, namely, a key generation algorithm, a signcryption algorithm and an unsigncryption algorithm.

- A key generation algorithm *SC.KeyGen* outputs a pair of matching public and private keys. The input to the key generation algorithm and the structure of public and private keys are dependent on the particular signcryption mechanism.

- A signcryption algorithm *SC.Signcrypt* performs a sequence of operations on an input and outputs a ciphertext. The input shall consist of
  - 1) a plaintext,
  - 2) a sender's public and private key pair,
  - 3) a recipient's public key,
  - 4) a label, and
  - 5) an option.

The plaintext, label and ciphertext are all bit strings, whereas the types and structures of public and private keys, as well as that of the option, are determined by the particular signcryption mechanism.

- An unsigncryption algorithm *SC.Unsigncrypt* performs a sequence of operations on an input and outputs either (ACCEPT, a plaintext) or (REJECT, NULL). The input shall consist of
  - 1) a ciphertext,
  - 2) a recipient's public and private key pair,
  - 3) a sender's public key,
  - 4) a label, and
  - 5) an option.

ACCEPT and REJECT in the output are symbolic values that indicate the acceptance and rejection of validity of the ciphertext in the input, respectively, and NULL is the null string.

Plaintexts may be of variable or fixed length, depending on the particular signcryption mechanism. If the signcryption mechanism can handle plaintexts of variable length, a parameter called *SC.MaxMsgLen* may be imposed by an implementation to an upper bound on the length of plaintexts. Otherwise if the signcryption mechanism can handle plaintexts of fixed length only, a parameter called *SC.MsgLen* is employed to define the plaintext length.

Part of the input to a signcryption/unsigncryption algorithm is a label and an option. Their functions are defined as follows.

- A *label* is a (possibly empty) bit string that participates in the signcryption of a plaintext, but need not be protected for confidentiality. An example of a label is a string of public data that is either explicit or implicit from context and required to be bound to the ciphertext. The length of a label may be variable, upper bounded only by an implementation dependant parameter *SC.LabelLen*.

The same label is required to be used by both the signcryption and unsigncryption algorithms in order for a recipient to correctly unsigncrypt a ciphertext.

Procedures for agreeing on a label for a specific signcryption mechanism or application are beyond the scope of this International Standard.

- An *option* is a (possibly empty) input argument that passes application and mechanism specific information to signcryption and unsigncryption algorithms. As an example, the elliptic curve based signcryption mechanism defined in this International Standard may use an option to indicate the desired format for encoding points on an elliptic curve. A second possible use of options is to pass system wide parameters specific to a signcryption mechanism. And a third possible use of options is

to pass application or mechanism specific information, such as private factors of composite moduli, to aid faster signcryption or unsigncryption.

An option used by an unsigncryption algorithm may be different from an option used by the signcryption algorithm. While information transmitted by an option may be used in signcryption or unsigncryption, the option itself is not directly involved in the signcryption or unsigncryption process.

Determination of these options for a specific signcryption mechanism or application is beyond the scope of this International Standard.

## 9 Discrete logarithm based signcryption mechanism (DLSC)

### 9.1 Introduction

In this clause a discrete logarithm based signcryption mechanism is defined. This mechanism is called DLSC. DLSC can handle plaintexts of variable length, upper bounded only by an implementation dependant parameter  $DLSC.MaxMsgLen$ .

**NOTE** DLSC is due to Zheng [23], with small tweaks due to Baek, Steinfeld and Zheng [3]. DLSC possesses security proofs for confidentiality and unforgeability. The security proof for confidentiality relies on the assumption for the Gap Diffie-Hellman problem and the random oracle model, whereas the security proof for unforgeability relies on the assumption for the Gap Discrete Logarithm problem and the random oracle model.

### 9.2 Specific requirements

Denote by  $(y_A, x_A)$  the public and private key pair of the sender, and by  $(y_B, x_B)$  the public and private key pair of the recipient. Both key pairs shall be generated, *independently of each other*, using the key generation algorithm as is described in 9.4. Furthermore, any entity that may have to send signcrypted messages and receive signcrypted messages shall have two independently generated key pairs. The first key pair shall be known as the sender key pair that shall only be used to signcrypt a message from that entity. The second key pair shall be known as the recipient key pair that shall only be used to unsigncrypt ciphertexts received by that entity.

### 9.3 System wide parameters

$l_q$	a positive integer that specifies the length in bits of prime $q$ .
$l_p$	a positive integer that specifies the length in bits of prime $p$ .
$q$	a random prime of $l_q$ bits in length, that is $L_b(q) = l_q$ .
$p$	a random prime of $l_p$ bits in length, that is $L_b(p) = l_p$ , such that $q$ is a prime factor of $p-1$ , that is, $q   (p-1)$ .
$g$	a random integer from $[2, \dots, p-1]$ with order $q$ modulo $p$ ; that is $q$ is the smallest positive exponent for which $g^q \equiv 1 \pmod{p}$ .
$G$	a key derivation function that takes as input a bit string and an integer, and outputs a bit string of length specified by the integer. (See 7.3)
$H$	a full domain cryptographic hash function that maps an input bit string of arbitrary length to an integer in $[0, \dots, q-1]$ . (See 7.2.2.)

The same algorithms for generating DSA domain parameters, as are described in Annex C of ISO/IEC 14888-3, shall be used to generate  $p$ ,  $q$  and  $g$ .

#### 9.4 Key generation algorithm

The key generation algorithm *DLSC.KeyGen* takes as input system wide parameters  $p$ ,  $q$  and  $g$ , and runs as follows to output a pair of matching public and private keys.

1. Generate a random integer  $x$  from  $[1, \dots, q-1]$ .
2. Compute  $y = g^x \bmod p$ , an integer in  $[2, \dots, p-1]$ .
3. Output  $(y, x)$  as a public and private key pair.

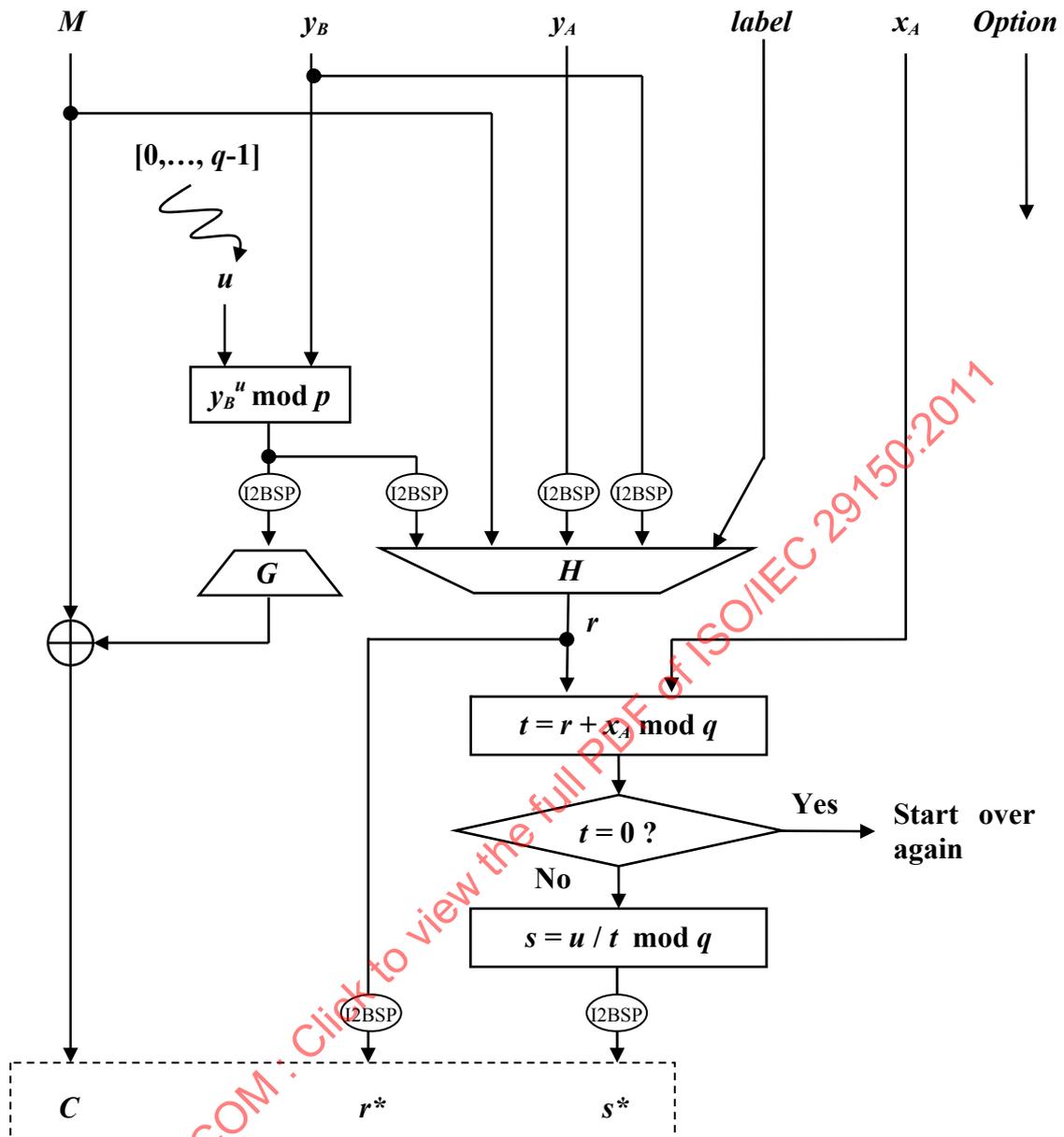
#### 9.5 Signcrypt algorithm

The signcrypt algorithm *DLSC.Signcrypt* takes as input a plaintext  $M$  (a bit string), a sender's public and private key pair  $(y_A, x_A)$ , a recipient's public key  $y_B$ , a *label* (a bit string), and an *option*. The sender shall perform the following steps to signcrypt the plaintext  $M$ . The resultant ciphertext is denoted by  $X$ .

1. If  $y_B$  is not an integer in the range of  $[2, \dots, p-1]$ , then **fail**.
2. Choose a random integer  $u$  from  $[1, \dots, q-1]$ .
3. Compute  $K = y_B^u \bmod p$ .
4. Compute  $C = G(\text{I2BSP}(K, l_p), |M|) \oplus M$ .
5. Compute  $r = H(\text{I2BSP}(K, l_p) \parallel M \parallel \text{I2BSP}(y_A, l_p) \parallel \text{I2BSP}(y_B, l_p) \parallel \text{label})$ .
6. If  $r + x_A \equiv 0 \pmod{q}$ , then return to Step 2.
7. Compute  $s = \frac{u}{r + x_A} \bmod q$ .
8. Compute  $r^* = \text{I2BSP}(r, l_q)$ .
9. Compute  $s^* = \text{I2BSP}(s, l_q)$ .
10. Set  $X = (C \parallel r^* \parallel s^*)$ .
11. Output  $X$ .

*DLSC.Signcrypt* is also illustrated in Figure 1.

NOTE It is assumed that system wide parameters defined in 9.3 are implicitly known to the signcrypt algorithm, or otherwise passed to the algorithm by such a means as the *option*.

Figure 1 — Signcrypting a plaintext with *DLSC.Signcrypt*

## 9.6 Unsignryption algorithm

The unsignryption algorithm *DLSC.Unsigncrypt* takes as input a ciphertext  $X$  (a bit string), a recipient's public and private key pair  $(y_B, x_B)$ , a sender's public key  $y_A$ , a *label* (a bit string), and an *option*. The recipient shall perform the following steps to unsigncrypt the ciphertext  $X$ .

1. If  $y_A$  is not an integer in the range of  $[2, \dots, p-1]$ , then **fail**.
2. Parse  $X$  as  $(C \parallel r^* \parallel s^*)$ , where  $|r^*| = |s^*| = l_q$ .  
If the parsing is unsuccessful, then **fail**.
3. Compute  $r = \text{BS2IP}(r^*)$ .
4. Compute  $s = \text{BS2IP}(s^*)$ .

5. If  $r$  is not in  $[0, \dots, q-1]$  or  $s$  is not in  $[1, \dots, q-1]$ , then **fail**.
6. Compute  $K = (g^r \cdot y_A)^{s \cdot x_B} \bmod p$ .
7. Compute  $M = G(\text{I2BSP}(K, l_p), |C|) \oplus C$ .
8. Compute  $v = H(\text{I2BSP}(K, l_p) \| M \| \text{I2BSP}(y_A, l_p) \| \text{I2BSP}(y_B, l_p) \| \text{label})$ .
9. If  $v = r$ , then output (ACCEPT,  $M$ ); otherwise output (REJECT, NULL), where ACCEPT and REJECT are symbolic values that indicate the acceptance and rejection of validity of the ciphertext, respectively, and NULL is the null string.

NOTE It is assumed that system wide parameters defined in 9.3 are implicitly known to the unsigncryption algorithm, or otherwise passed to the algorithm by such a means as the *option*.

## 10 Elliptic curve based signcryption mechanism (ECDLSC)

### 10.1 Introduction

In this clause an elliptic curve discrete logarithm based signcryption mechanism is defined. This mechanism is called ECDLSC. ECDLSC can handle plaintexts of variable length, upper bounded only by an implementation dependant parameter  $ECDLSC.MaxMsgLen$ .

NOTE ECDLSC is due to Zheng and Imai [23][24] with small tweaks due to Baek, Steinfeld and Zheng [3]. ECDLSC possesses security proofs for confidentiality and unforgeability. The security proof for confidentiality relies on the assumption for the Elliptic Curve Gap Diffie-Hellman problem and the random oracle model, whereas the security proof for unforgeability relies on the assumption for the Elliptic Curve Gap Discrete Logarithm problem and the random oracle model.

### 10.2 Specific requirements

Denote by  $(Y_A, x_A)$  the public and private key pair of the sender, and by  $(Y_B, x_B)$  the public and private key pair of the recipient. Both key pairs shall be generated, *independently of each other*, using the key generation algorithm as is described in 10.4. Furthermore, any entity that may have to send signcrypted messages and receive signcrypted messages shall have two independently generated key pairs. The first key pair shall be known as the sender key pair that shall only be used to signcrypt a message from that entity. The second key pair shall be known as the recipient key pair that shall only be used to unsigncrypt ciphertexts received by that entity.

### 10.3 System wide parameters

- |           |   |
|-----------|---|
| $m$       | a positive integer (required only if a binary field $GF(2^m)$ is employed).   |
| $l_p$     | a positive integer that specifies the length in bits of prime $p$ (required only if a prime field $GF(p)$ is employed). |
| $p$       | a prime of $l_p$ bits in length, that is $L_b(p) = l_p$ (required only if a prime field $GF(p)$ is employed).           |
| $GF(p^m)$ | a finite field in the form of either $GF(2^m)$ with $m > 1$ (a binary field) or $GF(p)$ with $p > 2$ (a prime field).   |
| $V$       | an elliptic curve over $GF(p^m)$ .  |
| $l_q$     | a positive integer that specifies the length in bits of prime $q$ .   |

$q$	a prime of $l_q$ bits in length, that is $L_b(q) = l_q$ .
$J$	a designated point on the elliptic curve $V$ with order $q$ . $J$ is also called a base point.
$fmt$	a format specifier whose value is chosen from $\{uncompressed, compressed, hybrid\}$ .
$G$	a key derivation function that takes as input a bit string and an integer, and outputs a bit string of length specified by the integer. (See 7.3)
$H$	a full domain cryptographic hash function that maps an input bit string of arbitrary length to an integer in $[0, \dots, q-1]$ . (See 7.2.2.)

NOTE Algorithms for generating elliptic curves, finding a point of large prime order on an elliptic curve and others are specified in ISO/IEC 15946-5.

#### 10.4 Key generation algorithm

The key generation algorithm  $ECDLSC.KeyGen$  takes as input system wide parameters  $V$ ,  $q$ , and  $J$ , and runs as follows to output a pair of matching public and private keys.

1. Generate a random integer  $x$  from  $[1, \dots, q-1]$ .
2. Compute  $Y = x \cdot J$ , a point on the elliptic curve  $V$ .
3. Output  $(Y, x)$  as a public and private key pair.

#### 10.5 Signcryption algorithm

The signcryption algorithm  $ECDLSC.Signcrypt$  takes as input a plaintext  $M$  (a bit string), a sender's public and private key pair  $(Y_A, x_A)$ , a recipient's public key  $Y_B$ , a *label* (a bit string), and an *option*. The sender shall perform the following steps to signcrypt the plaintext  $M$ . The resultant ciphertext is denoted by  $X$ .

1. If  $Y_B$  is not a point on the elliptic curve  $V$ , then **fail**.
2. Choose a random integer  $u$  from  $[1, \dots, q-1]$ .
3. Compute  $K = u \cdot Y_B$ .
4. Compute  $C = G(\text{EC2BSP}_V(K, fmt), |M|) \oplus M$ .
5. Compute  $r = H(\text{EC2BSP}_V(K, fmt) || M || \text{EC2BSP}_V(Y_A, fmt) || \text{EC2BSP}_V(Y_B, fmt) || \text{label})$ .
6. If  $r + x_A \equiv 0 \pmod{q}$ , then return to Step 2.
7. Compute  $s = \frac{u}{r + x_A} \pmod{q}$ .
8. Compute  $r^* = \text{I2BSP}(r, l_q)$ .
9. Compute  $s^* = \text{I2BSP}(s, l_q)$ .
10. Set  $X = (C || r^* || s^*)$ .
11. Output  $X$ .

$ECDLSC.Signcrypt$  is also illustrated in Figure 2.

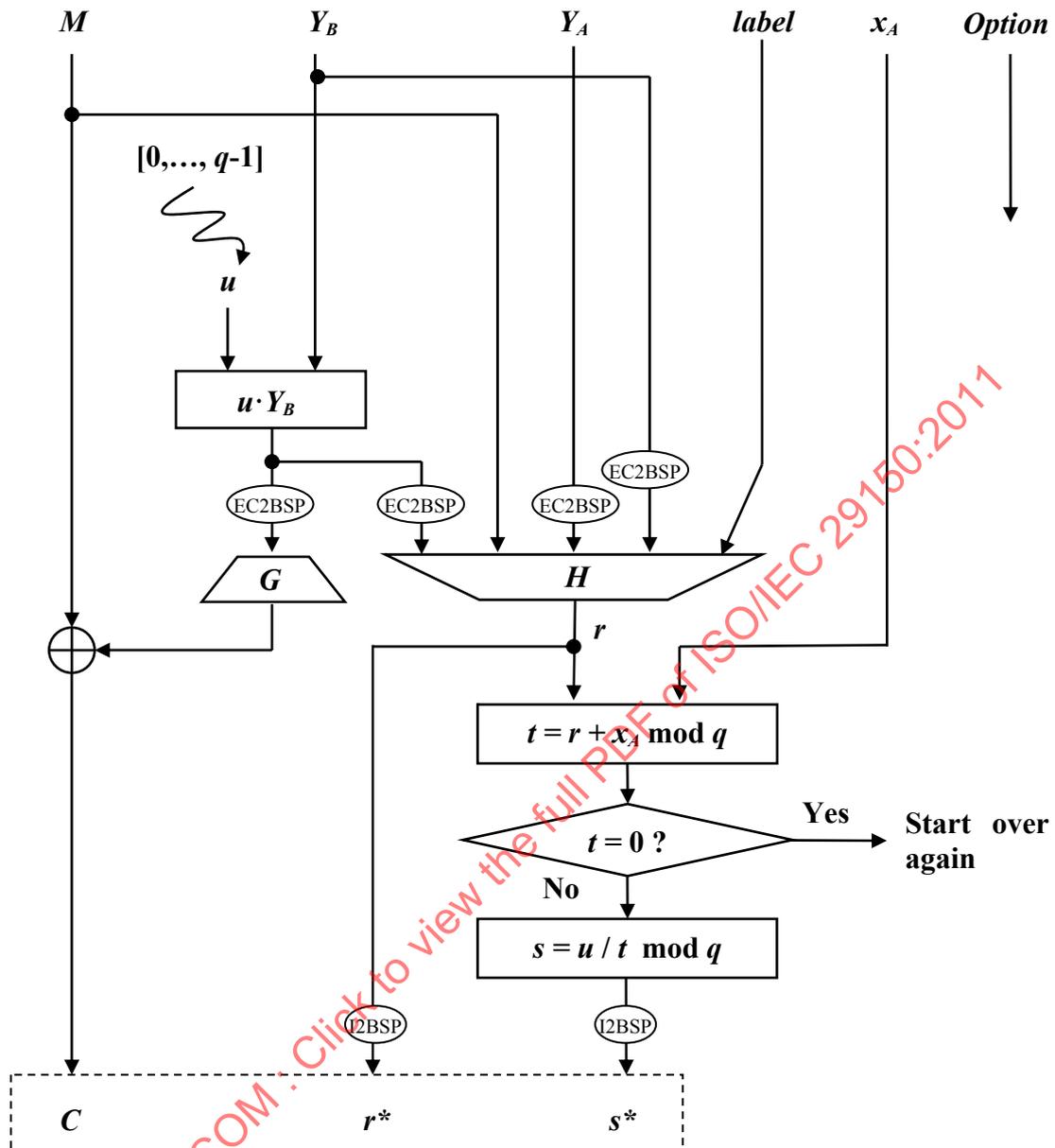
NOTE It is assumed that system wide parameters defined in 10.3 are implicitly known to the signcryption algorithm, or otherwise passed to the algorithm by such a means as the *option*. In addition, the format for encoding points on the elliptic curve, *fmt*, can be passed to the algorithm by the *option*.

### 10.6 Unsigncryption algorithm

The unsigncryption algorithm *ECDLSC.Unsigncrypt* takes as input a ciphertext  $X$  (a bit string), a recipient's public and private key pair  $(Y_B, x_B)$ , a sender's public key  $Y_A$ , a *label* (a bit string), and an *option*. The recipient shall perform the following steps to unsigncrypt the ciphertext  $X$ .

1. If  $Y_A$  is not a point on the elliptic curve  $V$ , then **fail**.
2. Parse  $X$  as  $(C || r^* || s^*)$ , where  $|r^*| = |s^*| = l_q$ .  
If the parsing is unsuccessful, then **fail**.
3. Compute  $r = \text{BS2IP}(r^*)$ .
4. Compute  $s = \text{BS2IP}(s^*)$ .
5. If  $r$  is not in  $[0, \dots, q-1]$  or  $s$  is not in  $[1, \dots, q-1]$ , then **fail**.
6. Compute  $K = s \cdot x_B \cdot (r \cdot J + Y_A)$ .
7. Compute  $M = G(\text{EC2BSP}_V(K, \text{fmt}), |C|) \oplus C$ .
8. Compute  $v = H(\text{EC2BSP}_V(K, \text{fmt}) || M || \text{EC2BSP}_V(Y_A, \text{fmt}) || \text{EC2BSP}_V(Y_B, \text{fmt}) || \text{label})$ .
9. If  $v = r$ , then output (ACCEPT,  $M$ ); otherwise output (REJECT, NULL), where ACCEPT and REJECT are symbolic values that indicate the acceptance and rejection of validity of the ciphertext, respectively, and NULL is the null string.

NOTE It is assumed that system wide parameters defined in 10.3 are implicitly known to the unsigncryption algorithm, or otherwise passed to the algorithm by such a means as the *option*. In addition, the format for encoding points on the elliptic curve, *fmt*, can be passed to the algorithm by the *option*.

Figure 2 — Signcrypting a plaintext with *ECDLSC.Signcrypt*

## 11 Integer factorization based signcrypton mechanism (IFSC)

### 11.1 Introduction

In this clause an integer factorization based signcrypton mechanism is defined. This mechanism is called IFSC. IFSC can handle plaintexts of fixed length determined by a parameter  $IFSC.MsgLen = l_M$ .

NOTE IFSC is due primarily to Malone-Lee and Mao [17], with improvements in security by Dodis, Freedman, Jarecki and Walfish [4]. IFSC possesses security proofs for confidentiality and unforgeability. The security proofs rely on the random oracle model and on the assumption that inverting the RSA function is difficult.

## 11.2 Specific requirements

Denote by  $[(N_A, e_A), (N_A, d_A)]$  the public and private key pair of the sender, and by  $[(N_B, e_B), (N_B, d_B)]$  the public and private key pair of the recipient. Both key pairs shall be generated, *independently of each other*, using the key generation algorithm as is described in 11.4. This mechanism allows an entity to use a single key pair for both signcryption and unsigncryption (i.e. an entity may use the same key pair as both its sender key pair to signcrypt messages originating from that entity and as its recipient key pair to unsigncrypt ciphertexts received by that entity).

## 11.3 System wide parameters

$l_r$	a positive integer that specifies the length of a random bit string $r$ chosen in the first step of the signcryption algorithm.
$l_H$	a positive integer that specifies the output length in bits of a standard cryptographic hash function $H$ .
$l_M$	a positive integer that specifies the length in bits of a plaintext, that is $IFSC.MsgLen = l_M$ .
$l$	a positive even integer that specifies the length in bits of an RSA modulus. $l$ satisfies $l = l_M + l_r + l_H$ .
$G$	a key derivation function that takes as input a bit string and an integer, and outputs a bit string of length specified by the integer.
$H_1, H_2$	two independent (standard) cryptographic hash functions each of which maps an input bit string of arbitrary length to a bit string of length $H_1.Len = H_2.Len = l_H$ .

## 11.4 Key generation algorithm

The key generation algorithm  $IFSC.KeyGen$  takes a system wide parameter  $l$  as input, and outputs a pair of matching public and private keys denoted by  $[(N, e), (N, d)]$ . These three positive integers  $N$ ,  $e$  and  $d$  are constrained by conditions specified below.

- $N$  is the product of two distinct primes  $p$  and  $q$  of  $l/2$  bits in length, that is  $L_b(p) = L_b(q) = l/2$ . The length of  $N$  is  $l$  bits.
- $e$  satisfies  $\gcd(e, (p-1)(q-1)) = 1$ .
- $d$  satisfies  $e \cdot d \equiv 1 \pmod{\lambda(N)}$ , where  $\lambda(N)$  is the least common multiple of  $(p-1)$  and  $(q-1)$ .

The exponent  $e$  in the public key is called a *public exponent*, and the exponent  $d$  in the private key a *private exponent*.

NOTE 1 Guidance for generating primes  $p$  and  $q$  can be found in ISO/IEC 18032.

NOTE 2 A relatively small prime such as 5, 17 or  $2^{16} + 1 = 65537$  can be selected as the public exponent  $e$  for faster signcryption and unsigncryption.

## 11.5 Signcryption algorithm

The signcryption algorithm  $IFSC.Signcrypt$  takes as input a plaintext  $M$  of  $l_M$  bits in length, a sender's private key  $(N_A, d_A)$ , a recipient's public key  $(N_B, e_B)$ , a *label* (a bit string), and an *option*. The sender shall perform the following steps to signcrypt the plaintext  $M$ . The resultant ciphertext is denoted by  $X$  whose length is  $l+1$  in bits.

1. Choose uniformly at random a bit string  $r$  of length  $l_r$ .
2. Compute  $c = H_1(M \parallel r \parallel \text{label})$ .
3. Compute  $w = G(c, l_M + l_r) \oplus (M \parallel r)$ .
4. Compute  $s = H_2(w) \oplus c$ .
5. If  $\text{BS2IP}(w \parallel s) \geq N_A$ , return to Step 1.
6. Compute  $t = [\text{BS2IP}(w \parallel s)]^{d_A} \bmod N_A$ .
7. If  $t \geq N_B$ , then set  $f = 1$ ; otherwise set  $f = 0$ .
8. Compute  $u = t - f \cdot 2^{l-1}$ .
9. Compute  $v = u^{e_B} \bmod N_B$ .
10. Compute  $C_1 = \text{I2BSP}(f, 1)$ .
11. Compute  $C_2 = \text{I2BSP}(v, l)$ .
12. Set  $X = (C_1 \parallel C_2)$ .
13. Output  $X$ .

*IFSC.Signcrypt* is also illustrated in Figure 3.

**NOTE** It is assumed that system wide parameters defined in 11.3 are implicitly known to the signcrypt algorithm, or otherwise passed to the algorithm by such a means as the *option*. The *option* can also be used to pass the prime factors of  $N_A$  which are required to speed up the exponentiation with the private exponent  $d_A$  in Step 6, using the Chinese Remainder Theorem (see [15], 4.3.2 Modular Arithmetic, [19] and ISO/IEC 14888-2:2008, 5.3).

## 11.6 Unsigncrypt algorithm

The unsigncrypt algorithm *IFSC.Unsigncrypt* takes as input a ciphertext  $X$  (a bit string), a recipient's private key  $(N_B, d_B)$ , a sender's public key  $(N_A, e_A)$ , a *label* (a bit string), and an *option*. The recipient shall perform the following steps to unsigncrypt the ciphertext  $X$ .

1. Parse  $X$  as  $(C_1 \parallel C_2)$ , where  $|C_1| = 1$  and  $|C_2| = l$ .  
If the parsing is unsuccessful, then **fail**.
2. Compute  $f = \text{BS2IP}(C_1)$ .
3. Compute  $v = \text{BS2IP}(C_2)$ .
4. Compute  $u = v^{d_B} \bmod N_B$ .
5. Compute  $t = u + f \cdot 2^{l-1}$ .
6. If  $t \geq N_A$  then **fail**.
7. Compute  $y = t^{e_A} \bmod N_A$ .
8. Parse  $\text{I2BSP}(y, l)$  as  $(w \parallel s)$ , where  $|w| = l_M + l_r$  and  $|s| = l_H$ .
9. Compute  $c = H_2(w) \oplus s$ .

10. Compute  $z = G(c, l_M + l_r) \oplus w$ .
11. Parse  $z$  as  $(M \parallel r)$ , where  $|M| = l_M$  and  $|r| = l_r$ .
12. If  $H_1(M \parallel r \parallel label) = c$ , then output (ACCEPT,  $M$ ); otherwise output (REJECT, NULL), where ACCEPT and REJECT are symbolic values that indicate the acceptance and rejection of validity of the ciphertext, respectively, and NULL is the null string.

NOTE It is assumed that system wide parameters defined in 11.3 are implicitly known to the unsigncryption algorithm, or otherwise passed to the algorithm by such a means as the *option*. The *option* can also be used to pass the prime factors of  $N_B$  which are required to speed up the exponentiation with the private exponent  $d_B$  in Step 4, using the Chinese Remainder Theorem (see [15], 4.3.2 Modular Arithmetic, [19] and ISO/IEC 14888-2:2008, 5.3).

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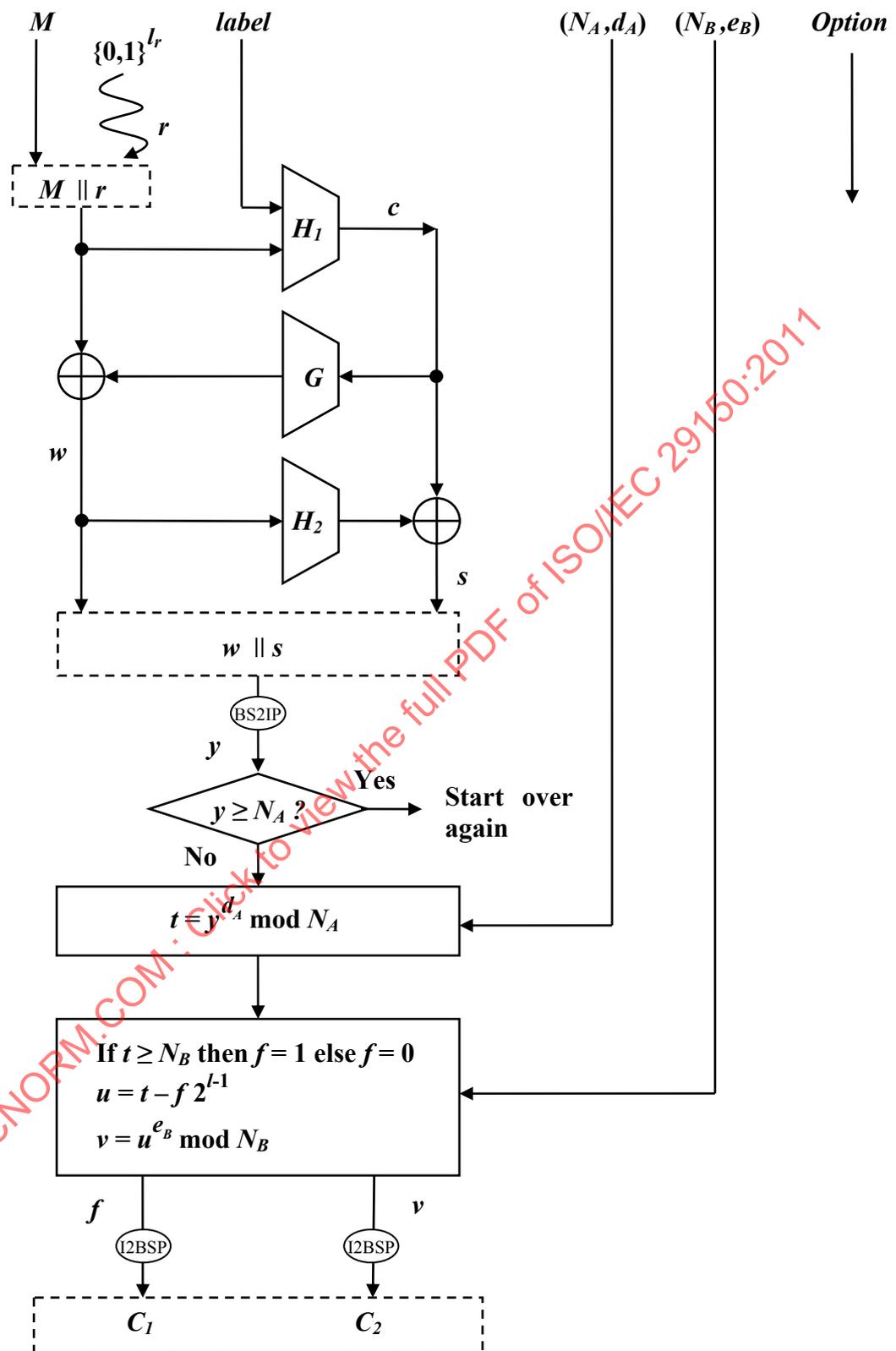


Figure 3 — Signcrypting a plaintext with *IFSC.Signcrypt*

## 12 Encrypt-then-sign-based mechanism (EtS)

### 12.1 Introduction

In this clause a signcryption mechanism based on the combination of an asymmetric encryption scheme and a digital signature scheme is defined. This mechanism is called EtS.

NOTE EtS is analysed by An, Dodis and Rabin[1]. EtS possesses proofs for confidentiality and unforgeability. The security proofs rely on the assumptions that the public-key encryption scheme is IND-CCA2 secure and that the digital signature scheme is strongly unforgeable.

### 12.2 Specific requirements

The EtS requires an asymmetric encryption scheme which shall be from ISO/IEC 18033-2. This asymmetric cipher will consist of three algorithms: a key generation  $AC.KeyGen$ , an encryption algorithm  $AC.Encrypt$ , and a decryption algorithm  $AC.Decrypt$ :

- The key generation algorithm  $AC.KeyGen()$  outputs a public and private key pair  $(PK, pk)$ .
- The encryption algorithm  $AC.Encrypt(PK, label, M, option)$  that takes as input a public key  $PK$ , a  $label$ , a plaintext  $M$ , and an encryption  $option$ , and outputs a ciphertext  $C$ . The encryption option controls part of the execution of the encryption algorithm and the form of the ciphertext.
- The decryption algorithm  $AC.Decrypt(pk, label, C)$  that takes as input a private key  $pk$ , a  $label$ , and a ciphertext  $C$ , and outputs a plaintext  $M$ . The decryption algorithm may **fail** under some circumstances.

The EtS requires a digital signature scheme which shall be taken from ISO/IEC 9796 or ISO/IEC 14888. This scheme will consist of three algorithms: a key generation algorithm  $SS.KeyGen$ , a signature generation algorithm  $SS.Sign$ , and a signature verification algorithm  $SS.Verify$ :

- The key generation algorithm  $SS.KeyGen()$  outputs a public and private key pair  $(PK, pk)$ .
- The signature generation algorithm  $SS.Sign(pk, M)$  takes as input a private key  $pk$  and a message  $M$ , and outputs a signed message  $\sigma$ .
- The signature verification algorithm  $SS.Verify(PK, \sigma)$  takes as input a public key  $PK$  and a signed message  $\sigma$ , and outputs either a message  $M$  or will **fail**.

The signcryption mechanism will inherit all the specific requirements of the asymmetric encryption scheme and digital signature scheme used in the EtS mechanism.

We also require that there exists a bit string  $ID_A$  which uniquely identifies a user  $A$  within some context.

NOTE This may be their public key value as this can be thought of as uniquely identifying a user via their public key certificate.

### 12.3 Key generation algorithm

Each user shall have a public and private key pair for signcryption consisting of an asymmetric encryption key pair and a digital signature key pair. This signcryption key pair may be used for both signcryption and unsigncryption. These keys are computed by the signcryption key generation algorithm as follows:

1.  $(PK_e, pk_d) = AC.KeyGen()$ .
2.  $(PK_v, pk_s) = SS.KeyGen()$ .

3.  $PK=(PK_e\|PK_v)$ .
4.  $pk=(pk_d\|pk_s)$ .
5. Output  $(PK, pk)$ .

#### 12.4 Signcryption algorithm

The signcryption algorithm *EtS.Signcrypt* takes as input a plaintext  $M$ , a sender  $A$ 's public and private key pair  $(PK_A, pk_A)$ , a recipient  $B$ 's public key  $PK_B$ , the sender's identifier  $ID_A$ , the recipient's identifier  $ID_B$ , a *label*, and an *option*. The sender shall perform the following steps to signcrypt the plaintext  $M$ . The resultant ciphertext is denoted by  $X$ .

1. Parse  $PK_A$  as  $(PK_{A,e}\|PK_{A,v})$  and  $pk_A$  as  $(pk_{A,d}\|pk_{A,s})$ .
2. Parse  $PK_B$  as  $(PK_{B,e}\|PK_{B,v})$ .
3. Compute  $C=AC.Encrypt(PK_{B,e}, M\|ID_A, label, option)$ .
4. Compute  $X=SS.Sign(pk_{A,s}, C\|ID_B)$ .
5. Output  $X$ .

#### 12.5 Unsigncryption algorithm

The unsigncryption algorithm *EtS.Unsigncrypt* takes as input a ciphertext  $X$ , a sender  $A$ 's public key  $PK_A$ , a recipient  $B$ 's public and private key pair  $(PK_B, pk_B)$ , the sender's identifier  $ID_A$ , the recipient's identifier  $ID_B$ , a *label*, and an *option*. The recipient shall perform the following steps to unsigncrypt the ciphertext  $X$ .

1. Parse  $PK_A$  as  $(PK_{A,e}\|PK_{A,v})$ .
2. Parse  $PK_B$  as  $(PK_{B,e}\|PK_{B,v})$  and  $pk_B$  as  $(pk_{B,d}\|pk_{B,s})$ .
3. Compute  $X'=SS.Verify(PK_{A,v}, X)$ .
4. If *SS.Verify fails* then **fail**.
5. Parse  $X'$  as  $(C\|ID'_B)$ .
6. If  $ID'_B \neq ID_B$  then **fail**.
7. Compute  $Y=AC.Decrypt(pk_{B,d}, label, C)$ .
8. If *AC.Decrypt fails* then **fail**.
9. Parse  $Y$  as  $(M\|ID'_A)$ .
10. If  $ID'_A \neq ID_A$  then **fail**.
11. Output  $M$ .

## Annex A (normative)

### Object identifiers

#### A.1 Formal definition

```
Signcryption {iso(1) standard(0) signcryption(29150) asn1-module(0)
signcryption-mechanisms(0) version(1)}
```

```
DEFINITIONS EXPLICIT TAGS ::= BEGIN
```

```
IMPORTS id-sha1, id-sha256, id-sha384, id-sha512, HashFunctionAlgs FROM
DedicatedHashFunctions {iso(1) standard(0) hash-functions(10118) part(3)
asn1-module(1) dedicated-hash-functions(0)};
```

```
OID ::= OBJECT IDENTIFIER
```

```
-- Synonyms --
```

```
id-kdf OID ::= {iso(1) standard(0) encryption-algorithms(18033) part(2)
key-derivation-function(5)}
```

```
id-kdf-kdf1 OID ::= {id-kdf kdf1(1)}
```

```
id-kdf-kdf2 OID ::= {id-kdf kdf2(2)}
```

```
is29150 OID ::= {iso(1) standard(0) signcryption(29150)}
```

```
mechanism OID ::= {is29150 mechanisms(1)}
```

```
signcryption-mechanism-dlsc OID ::= {mechanism dlsc(1) }
```

```
signcryption-mechanism-ecdsc OID ::= {mechanism ecdsc(2)}
```

```
signcryption-mechanism-ifsc OID ::= {mechanism ifsc(3)}
```

```
signcryption-mechanism-ets OID ::= {mechanism ets(4)}
```

```
SCHashFunction ALGORITHM ::= {
{OID id-sha1 PARMS NullParms} |
{OID id-sha256 PARMS NullParms } |
{OID id-sha384 PARMS NullParms } |
{OID id-sha512 PARMS NullParms },
... -- expect more hash functions here
}
```

```
SCKDFfunction ALGORITHM ::= {
{OID id-kdf-kdf1 PARMS SCHashFunction} |
{OID id-kdf-kdf2 PARMS SCHashFunction},
... -- expect additional KDF functions here
}
```

```
SCparameters ::= SEQUENCE {
kdf SCKDFfunction,
hash SCHashFunction
```

```

}

SigncryptMechanism ALGORITHM ::= {
  {OID signcrypt-mechanism-dlsc   PARMS SCparameters} |
  {OID signcrypt-mechanism-ecdsc  PARMS SCparameters} |
  {OID signcrypt-mechanism-ifsc   PARMS SCparameters} |
  {OID signcrypt-mechanism-ets    PARMS SCparameters}
}

NullParms ::= NULL

-- Cryptographic algorithm identification --

ALGORITHM ::= CLASS {
  &id   OBJECT IDENTIFIER UNIQUE,
  &Type OPTIONAL
} WITH SYNTAX {OID &id [PARMS &Type]}

END -- Signcrypt --

```

## A.2 Use of subsequent object identifiers

Each of the signcrypt mechanisms specified in this International Standard uses a key derivation function. Therefore, the signcrypt mechanism object identifier may include the object identifier of one of the key derivation identifiers specified in ISO/IEC 18033-2 and any associated parameters.

In addition, both mechanisms DLSC and ECDLSC employ a full domain cryptographic hash function, whereas mechanism IFSC employs two independent standard cryptographic hash functions. Since a full domain cryptographic hash function can be obtained from a standard cryptographic hash function by applying the procedure FDH1 specified in 7.2.2.2, the signcrypt mechanism object identifier may further include the object identifier of one of the hash algorithm identifiers specified in ISO/IEC 10118-3[10] and any associated parameters.

## Annex B (informative)

### Security considerations

#### B.1 Introduction

This Annex first discusses generic weaknesses of the signcryption mechanisms defined in this International Standard (Clause B.2). These generic weaknesses exist due to number theoretic assumptions and cryptographic hash functions on which the signcryption mechanisms depend for their security. It then proceeds to discuss security properties of cryptographic transformations which are used by the signcryption mechanisms (Clause B.3). This is followed by discussions on the random oracle model which is required for proving the security properties of these mechanisms (Clause B.4). Finally security properties of the signcryption mechanisms are discussed (Clauses B.5-B.8).

Security properties of a signcryption mechanism include those pertaining to confidentiality and unforgeability.

In this Annex, a *polynomial time algorithm/attacker* means one whose running time is bounded from above by a polynomial in the size of its input or a security parameter.

#### B.2 Generic weaknesses

Like all cryptographic mechanisms that rely for their security on computational complexity assumptions, such as the Discrete Logarithm assumption in Clause B.5, the Elliptic Curve Discrete Logarithm assumption in Clause B.6, and the Factorization assumption in Clause B.7, the signcryption mechanisms defined in this International Standard become insecure in an event when the underlying computational complexity assumptions no longer hold, due to such advancements as an algorithmic breakthrough in integer factorization or solving discrete logarithms (see for examples [16][18]), or the development of a practical quantum computer (see [20]).

In addition, all the signcryption mechanisms are subject to attacks that run in sub-exponential time (see [16][18]), although such attacks become impractical when public keys are sufficiently large.

Furthermore, as all the signcryption mechanisms use cryptographic hash functions defined in ISO/IEC 10118-2 and ISO/IEC 10118-3 (see [10]), a weakness in these allowable cryptographic hash functions may lead to the insecurity of the signcryption mechanisms.

#### B.3 Cryptographic transformations

This International Standard uses the following cryptographic transformations that are described in other standards:

- Standard cryptographic hash functions (ISO/IEC 10118-2 and ISO/IEC 10118-3, with a proviso that is not related to security);
- Cryptographic key derivation functions (see ISO/IEC 18033-2:2006, 6.2).

Security properties of these cryptographic transformations are addressed in those respective standards.

In addition, this International Standard defines a cryptographic transformation called a full domain cryptographic hash function in 7.2.2. The specific allowable full domain cryptographic hash function FDH1 described in 7.2.2.2 is obtained by chopping off lower order/right most bits of the output of a standard cryptographic hash function, followed by testing whether the resultant output, when being regarded as an

integer, is within a required range. The resultant output is valid only if it is within the required range. As FDH1 does not alter the original cryptographic hash function, nor does it expand the output length, FDH1 inherits all the security properties of the original cryptographic hash function.

## B.4 Random oracle model

Every signcryption mechanism described in this International Standard employs some or all of the following three types of cryptographic transformations: key derivation functions, standard cryptographic hash functions and full domain cryptographic hash functions. It is assumed that these cryptographic functions all behave like a *random oracle*.

The above assumption on key derivation and cryptographic hash functions is an example of the so-called *random oracle methodology*.

## B.5 Provable security of DLSC

### Confidentiality

*The Discrete Logarithm problem.* Let  $g$  be an integer from  $[1, \dots, p-1]$  with order  $q$  modulo  $p$  and let  $a$  be chosen uniformly at random from  $[1, \dots, q-1]$ . On input  $g^a \bmod p$ , an adversary either outputs  $a$  or declares failure. *The Discrete Logarithm assumption* states that the probability for a polynomial time adversary to successfully output  $a$  is negligibly small.

*The Diffie-Hellman problem.* Let  $g$  be an integer from  $[1, \dots, p-1]$  with order  $q$  modulo  $p$  and let  $a$  and  $b$  be integers chosen uniformly at random from  $[1, \dots, q-1]$ . On input  $g^a \bmod p$  and  $g^b \bmod p$ , an adversary either outputs the Diffie-Hellman key  $K = g^{ab} \bmod p$  or declares failure. *The Diffie-Hellman assumption* states that the probability for a polynomial time adversary to successfully output  $K = g^{ab} \bmod p$  is negligibly small.

*The Gap Diffie-Hellman problem.* Let  $g$  be an integer from  $[1, \dots, p-1]$  with order  $q$  modulo  $p$  and let  $a$  and  $b$  be integers chosen uniformly at random from  $[1, \dots, q-1]$ . An adversary takes  $g^a \bmod p$  and  $g^b \bmod p$  as input and is granted access to a *Decisional Diffie-Hellman oracle*  $O^{DDH}$ . The adversary either outputs the Diffie-Hellman key  $K = g^{ab} \bmod p$  or declares failure.

The *Decisional Diffie-Hellman oracle*  $O^{DDH}$  takes as input  $(h, h^u \bmod p, h^v \bmod p, z)$ , and outputs either '1' when  $z = h^{uv} \bmod p$ , or '0' otherwise, where  $h$  and  $z$  are from  $[1, \dots, p-1]$  and  $u$  and  $v$  are from  $[1, \dots, q-1]$ . It is permissible for  $h$  to be the same as  $g$ .

The *Gap Diffie-Hellman assumption* states that the probability for a polynomial time adversary to successfully output the Diffie-Hellman key  $K = g^{ab} \bmod p$  is negligibly small.

*The adaptive chosen ciphertext attacker.* There are two aspects about an adaptive chosen ciphertext attacker, namely (1) what the goal of the attacker is, and (2) what the attacker is allowed to do.

The goal of the attacker is to break the confidentiality of messages communicated between Alice the sender and Bob the recipient. Specifically, the attacker wishes to find some (partial) information on a target ciphertext between Alice and Bob.

The attacker can record ciphertexts communicated between Alice and Bob. The attacker has access to both Alice's public key and Bob's public key. In addition the attacker is allowed to use Alice's signcryption algorithm *DLSC.Signcrypt* as a "flexible signcryption oracle" and Bob's unsigncryption algorithm *DLSC.Unsigncrypt* as a

“flexible unsigncryption oracle”. With the flexible signcryption oracle, the attacker is allowed to pick, as a query to the oracle, any plaintext and any valid public key at will, including Bob the recipient’s public key. Upon receiving the plaintext and the public key from the attacker, Alice dutifully performs signcryption on the plaintext with her own private key and the public key from the attacker. She then returns the resultant ciphertext to the attacker as an answer to the query.

With the flexible unsigncryption oracle, the attacker is allowed to pick, as a query to the oracle, any ciphertext (other than the target ciphertext) and any valid public key at will, including Alice the sender’s public key. Upon receiving the ciphertext and the public key from the attacker, Bob dutifully performs unsigncryption on the ciphertext with his own private key and the public key from the attacker. He then returns the resultant plaintext to the attacker as an answer to the query.

It is assumed that when the public key in a query to the flexible signcryption oracle or the flexible unsigncryption oracle is not the fixed public key of Alice or that of Bob, the attacker has full access to the matching private key.

*Formal security proof for confidentiality.* [3] provides a mathematical proof for the fact that with DLSC, a polynomial time adaptive chosen ciphertext attacker described above, whose running time is limited by a polynomial in  $L_b(p)$ , has only a negligibly small chance in successfully breaking the confidentiality of messages between a sender and a recipient, under the assumptions for the random oracle model and the Gap Diffie-Hellman problem.

### Unforgeability

*The Gap Discrete Logarithm problem.* Let  $g$  be an integer from  $[1, \dots, p-1]$  with order  $q$  modulo  $p$  and let  $a$  be an integer chosen uniformly at random from  $[1, \dots, q-1]$ . An adversary takes  $g^a \bmod p$  as input and is granted access to a *restricted Decisional Diffie-Hellman oracle*  $O^{rDDH}$ . The adversary either outputs the exponent  $a$  or declares failure.

The restricted Decisional Diffie-Hellman oracle  $O^{rDDH}$  takes as input  $(g, g^a \bmod p, h^v \bmod p, z)$ , and outputs either ‘1’ when  $z = h^{av} \bmod p$ , or ‘0’ otherwise, where  $h$  and  $z$  are from  $[1, \dots, p-1]$  and  $v$  is from  $[1, \dots, q-1]$ . It is permissible for  $h$  to be the same as  $g$ . Note that the difference between a Decisional Diffie-Hellman oracle  $O^{DDH}$  and a restricted Decisional Diffie-Hellman oracle  $O^{rDDH}$  is that the first two items in the input of  $O^{rDDH}$  are fixed to  $g$  and  $g^a \bmod p$ .

The *Gap Discrete Logarithm assumption* states that the probability for a polynomial time adversary to successfully output the exponent  $a$  is negligibly small.

*The adaptive chosen message attacker.* There are two aspects about an adaptive chosen message attacker: (1) what the goal of the attacker is, and (2) what the attacker is allowed to do.

The goal of the attacker is to forge a valid ciphertext from Alice the sender to a recipient of the attacker’s choice.

The attacker has access to Alice’s public key and is allowed to use Alice’s signcryption algorithm DLSC.Signcrypt as a “flexible signcryption oracle”. In addition, the attacker is allowed to pick, as a query to the oracle, any plaintext and any valid public key at will (other than Alice’s public key). The attacker has access to the private key that matches the public key. Upon receiving the plaintext and the public key from the attacker, Alice dutifully performs signcryption on the plaintext with her own private key and the public key from the attacker. She then returns the resultant ciphertext to the attacker as an answer to the query.

*Formal security proof for unforgeability.* [3] provides a mathematical proof for the fact that with DLSC, a polynomial time adaptive chosen message attacker described above, whose running time is limited by a polynomial in  $L_b(p)$ , has only a negligibly small chance in successfully forging a valid ciphertext from Alice to

any recipient, for a new plaintext with which the attacker has not queried Alice's signcryption algorithm, under the assumptions for the random oracle model and the Gap Discrete Logarithm problem.

## B.6 Provable security of ECDLSC

The Discrete Logarithm, the Diffie-Hellman, the Gap Diffie-Hellman and the Gap Discrete Logarithm problems all have their equivalent on elliptic curves.

ECDLSC has the same provable security properties with confidentiality and unforgeability as those of DLSC, under the same assumption for the random oracle model and the assumption on the elliptic curve equivalent of the Gap Diffie-Hellman and Gap Discrete Logarithm problems.

## B.7 Provable security of IFSC

*The Factorization problem.* Let  $N$  be a composite integer. On input  $N$ , an adversary either outputs prime factors of  $N$  or declares failure. *The Factorization assumption* states that for a sufficiently large  $N$ , the probability for a polynomial time adversary to successfully output factors of  $N$  is negligibly small.

*The RSA Inversion problem.* Let  $N$  be an RSA modulus and  $e$  be a public exponent. Also let  $C = M^e \bmod N$  be the RSA ciphertext for a randomly chosen plaintext  $M$ . On input  $C$ , an adversary either outputs  $M$  or declares failure. *The RSA (inversion) assumption* states that the probability for a polynomial time adversary to successfully output  $M$  is negligibly small.

### Confidentiality

*The adaptive chosen ciphertext attacker.* There are two aspects about an adaptive chosen ciphertext attacker, namely (1) what the goal of the attacker is, and (2) what the attacker is allowed to do.

The goal of the attacker is to break the confidentiality of messages communicated between Alice the sender and Bob the recipient. Specifically, the attacker wishes to find some (partial) information on a target ciphertext between Alice and Bob.

The attacker can record ciphertexts communicated between Alice and Bob. The attacker has access to both Alice's public key and Bob's public key. In addition the attacker is allowed to use Alice's signcryption algorithm *IFSC.Signcrypt* as a "flexible signcryption oracle" and Bob's unsigncryption algorithm *IFSC.Unsigncrypt* as a "flexible unsigncryption oracle". With the flexible signcryption oracle, the attacker is allowed to pick, as a query to the oracle, any plaintext and any valid public key at will, including Bob the recipient's public key. Upon receiving the plaintext and the public key from the attacker, Alice dutifully performs signcryption on the plaintext with her own private key and the public key from the attacker. She then returns the resultant ciphertext to the attacker as an answer to the query.

With the flexible unsigncryption oracle, the attacker is allowed to pick, as a query to the oracle, any ciphertext (other than the target ciphertext) and any valid public key at will, including Alice the sender's public key. Upon receiving the ciphertext and the public key from the attacker, Bob dutifully performs unsigncryption on the ciphertext with his own private key and the public key from the attacker. He then returns the resultant plaintext to the attacker as an answer to the query.

It is assumed that when the public key in a query to the flexible signcryption oracle or the flexible unsigncryption oracle is not the fixed public key of Alice or that of Bob, the attacker has full access to the matching private key.

*Formal security proof for confidentiality.* [4] (see also [17]) provides a mathematical proof for the fact that with IFSC, a polynomial time adaptive chosen ciphertext attacker described above, whose running time is limited by a polynomial in  $l$ , has only a negligibly small chance in successfully breaking the confidentiality of messages between a sender and a recipient. The proof relies on the random oracle model and on the assumption that the RSA inversion problem is hard.

## Unforgeability

*The adaptive chosen message attacker.* There are two aspects about an adaptive chosen message attacker: (1) what the goal of the attacker is, and (2) what the attacker is allowed to do.

The goal of the attacker is to forge a valid ciphertext from Alice the sender to a recipient of the attacker's choice.

The attacker has access to Alice's public key and both private and public keys of any recipient. Furthermore the attacker is allowed to use Alice's signcryption algorithm *IFSC.Signcrypt* as a "flexible signcryption oracle". Specifically, the attacker is allowed to pick, as a query to the oracle, any plaintext and any valid public key at will. Upon receiving the plaintext and the public key from the attacker, Alice dutifully performs signcryption on the plaintext with her own private key and the public key from the attacker. She then returns the resultant ciphertext to the attacker as an answer to the query.

*Formal security proof for unforgeability.* [4] (see also [17]) provides a mathematical proof for the fact that with the IFSC, a polynomial time adaptive chosen message attacker described above, whose running time is limited by a polynomial in  $l$ , has only a negligibly small chance in successfully forging a valid ciphertext from Alice to any recipient for a new plaintext with which the attacker has not queried Alice's signcryption algorithm. The proof relies on the random oracle model and on the assumption that the RSA inversion problem is hard.

## B.8 Provable security of EtS

The security of the EtS is based on the security of the underlying digital signature scheme and the underlying public-key encryption scheme. It does not require the use of the random oracle model, although the security of a specific signcryption scheme constructed in this manner may still only be proven secure in the random oracle model if either the underlying public-key encryption scheme or the underlying digital signature scheme are proven secure in the random oracle model.

The mechanism gives a secure method for combining a public-key encryption scheme and a digital signature scheme in a manner that preserves the security of both elements. More naive methods of combining public-key encryption and digital signature schemes may not give rise to a signcryption scheme with the same strict security guarantees. In certain cases, the combination of public-key encryption and digital signature schemes may lead to a scheme which is insecure even if the underlying schemes are secure.

## Confidentiality

*The adaptive chosen ciphertext attacker.* There are two aspects about an adaptive chosen ciphertext attacker, namely (1) what the goal of the attacker is, and (2) what the attacker is allowed to do.

The goal of the attacker is to break the confidentiality of messages communicated between Alice the sender and Bob the recipient. Specifically, the attacker wishes to find some (partial) information on a target ciphertext between Alice and Bob.

The attacker can record ciphertexts communicated between Alice and Bob. The attacker has access to both Alice's public key and Bob's public key. In addition the attacker is allowed to use Alice's signcryption algorithm *EtS.Signcrypt* as a "flexible signcryption oracle" and Bob's unsigncryption algorithm *EtS.Unsigncrypt* as a "flexible unsigncryption oracle". With the flexible signcryption oracle, the attacker is allowed to pick, as a query to the oracle, any plaintext and any valid public key at will, including Bob the recipient's public key. Upon receiving the plaintext and the public key from the attacker, Alice dutifully performs signcryption on the plaintext with her own private key and the public key from the attacker. She then returns the resultant ciphertext to the attacker as an answer to the query.

With the flexible unsigncryption oracle, the attacker is allowed to pick, as a query to the oracle, any ciphertext (other than the target ciphertext) and any valid public key at will, including Alice the sender's public key. Upon receiving the ciphertext and the public key from the attacker, Bob dutifully performs unsigncryption on the ciphertext with his own private key and the public key from the attacker. He then returns the resultant plaintext to the attacker as an answer to the query.

*Formal security proof for confidentiality.* [1] provides a mathematical proof for the fact that with EtS, a polynomial-time adaptive chosen ciphertext attacker described above, whose running time is limited by a polynomial in  $L_b(p)$ , has only a negligible small chance in successfully breaking the confidentiality of messages between a sender and a recipient, under the assumption that the underlying public-key encryption scheme is secure against adaptive chosen ciphertext attacks.

### **Unforgeability**

*The adaptive chosen message attacker.* There are two aspects about an adaptive chosen message attacker: (1) what the goal of the attacker is, and (2) what the attacker is allowed to do.

The goal of the attacker is to forge a valid ciphertext from Alice the sender to a recipient of the attacker's choice.

The attacker has access to Alice's public key and is allowed to use Alice's signcryption algorithm *EtS.Signcrypt* as a "flexible signcryption oracle". In addition, the attacker is allowed to pick, as a query to the oracle, any plaintext and any valid public key at will. Upon receiving the plaintext and the public key from the attacker, Alice dutifully performs signcryption on the plaintext with her own private key and the public key from the attacker. She then returns the resultant ciphertext to the attacker as an answer to the query.

*Formal security proof for unforgeability.* [1] provides a mathematical proof for the fact that with EtS, a polynomial-time adaptive chosen message attacker described above, whose running time is limited by a polynomial in  $L_b(p)$ , has only a negligible small chance in successfully forging a valid ciphertext from Alice to any recipient, for a new plaintext with which the attacker has not queried Alice's signcryption algorithm, under the assumption that the underlying signature scheme is secure against adaptive chosen message attacks.

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## Annex C (informative)

### Guidance on use of the mechanisms

#### C.1 Introduction

The purpose of this annex is to provide guidance on the use of the signcryption mechanisms defined in this International Standard. To aid the selection of a specific signcryption mechanism, a comparison table of the first three signcryption mechanisms is provided in Clause C.2. Common requirements of all the four signcryption mechanisms are discussed in Clause C.3. Use of each mechanism requires the choice of certain parameters, and recommendations regarding sizes/lengths of these parameters are provided in Clauses C.4-C.7.

Suggested sizes for parameters in Tables C.2-C.5 in Clauses C.4-C.7 shall be considered to be the minimum sizes that are required to achieve corresponding security levels.

#### C.2 Selection of mechanism

All the four signcryption mechanisms specified in this International Standard, i.e. the discrete logarithm based signcryption mechanism (DLSC), the elliptic curve based signcryption mechanism (ECDLSC), the integer factorization based signcryption mechanism (IFSC), and the encrypt-then-sign based mechanism (EtS) possess provable security under appropriate assumptions. (See Annex B). However, some mechanisms are more suitable than others for particular applications. When selecting a mechanism for use, facts and observations given in [3], [17], [23] and [24], and those listed below should be taken into consideration.

**Table C.1 — Properties of signcryption mechanisms**

Mechanism	DLSC	ECDLSC	IFSC
Dominant computation by sender	1 exponentiation	1 scalar product	2 exponentiations (1 with a public exponent; 1 with a private exponent)
Dominant computation by recipient	1 product of 2 exponentiations (1.17 exponentiations)	1 summand of 2 scalar products (1.17 scalar products)	2 exponentiations (1 with a public exponent; 1 with a private exponent)
Speed of signcryption / unsigncryption (1: fastest; 3: slowest)	2	1	3
Message expansion, Length of ciphertext (in bits)	$2l_q,$ $ M  + 2l_q$	$2l_q,$ $ M  + 2l_q$	$l_r + l_H + 1,$ $l_M + l_r + l_H + 1 = l + 1$
Applicable to both short and long messages	Yes	Yes	Short messages only
Non-repudiation	Interactive or trusted 3 <sup>rd</sup> party	Interactive or trusted 3 <sup>rd</sup> party	Non-interactive
System wide public keys required	Yes	Yes	No
License possibly required	Yes	Yes	Yes

- a) An algorithm attributed to E. G. Strauss that computes  $g^a h^b$ , the product of two exponentiations, faster than the straightforward exponentiation-then-multiplication can be found in [15], Answer to Exercise 4.6.4-36, Pages 696-697 (see also [2] for a comparison of related algorithms). The algorithm can be adapted to compute  $aX + bY$ , the summand of two scalar products on an elliptic curve, faster than the straightforward scalar multiplication-then-addition method [21] (see also [22] for techniques that require a smaller number of registers.)
- b) When the lengths of moduli are equal, computational time for exponentiation or scalar product is determined mainly by the length of exponents. The exponents for DLSC and ECDLSC are of  $l_q$  bits in length. For IFSC a small prime such as 5, 17, or  $2^{16} + 1 = 65537$  may be selected as a public exponent  $e$ , although the corresponding private exponent  $d$  is necessarily large ( $l$  bits in length). When such small public exponents are chosen, comparison of computational time between IFSC, DLSC and ECDLSC can be carried out by focusing on the length of private exponents/keys.
- c) Non-repudiation settlement is said to be interactive if a repudiation dispute cannot be settled by a judge who is not fully trusted by the sender or the recipient, without invoking either an interactive or a non-interactive but inefficient, zero-knowledge proof protocol between the judge and the recipient.

### C.3 Common requirements

All the mechanisms require the use of public key infrastructures for management of users' public keys. Public key infrastructures are defined in ISO/IEC 11770-1 and ISO/IEC 9594.

All the mechanisms require the selection of a standard cryptographic hash function, which is used directly in the integer factorization based signcryption, and indirectly in the other two signcryption mechanisms to build a full domain cryptographic hash function. It is recommended to use standard cryptographic hash functions specified in ISO/IEC 10118-2 and ISO/IEC 10118-3.

In addition, all the signcryption mechanisms require the use of a key derivation function. KDF1 and KDF2 defined in ISO/IEC 18033-2 are recommended.

### C.4 Selecting sizes of parameters for DLSC

Sizes for the following parameters shall be considered:

$l_p$  the length in bits of prime  $p$ ; that is  $l_p = L_b(p) = \lceil \log_2(p+1) \rceil$ .

$l_q$  the length in bits of prime  $q$ ; that is  $l_q = L_b(q) = \lceil \log_2(q+1) \rceil$ .

**Table C.2 — Parameter sizes for DLSC**

Security level (in bits)	80	112	128	192	256
$l_p$	1 024	2 048	3 072	7 680	15 360
$l_q$	160	224	256	384	512

NOTE Table C.2 is based on ISO/IEC 14888-3:2006, 5.1.3.1.

### C.5 Selecting sizes of parameters for ECDLSC

It is recommended that either a prime field  $GF(p)$ , where  $p$  is a prime, or a binary field  $GF(2^m)$ , where  $m$  is a positive integer, be selected to serve as the underlying finite field for an elliptic curve.

When a prime field  $GF(p)$  is employed, sizes for the following parameters shall be considered:

$l_p$  the size in bits of prime  $p$  when the underlying finite field is a prime field  $GF(p)$ ; that is  $l_p = L_b(p) = \lceil \log_2(p+1) \rceil$ .

$l_q$  the length in bits of prime  $q$ ; that is  $l_q = L_b(q) = \lceil \log_2(q+1) \rceil$ .

**Table C.3 — Parameter sizes for ECDLSC over a prime field  $GF(p)$**

Security level (in bits)	80	112	128	192	256
$l_p$	192	224	256	384	521
$l_q$	160	224	256	384	512

When a binary field  $GF(2^m)$  is employed, sizes for the following parameters shall be considered:

$m$  a positive integer indicating the size of the underlying binary field  $GF(2^m)$ .

$l_q$  the length in bits of prime  $q$ ; that is  $l_q = L_b(q) = \lceil \log_2(q+1) \rceil$ .

**Table C.4 — Parameter sizes for ECDLSC over a binary field  $GF(2^m)$**

Security level (in bits)	80	112	128	192	256
$m$	163	233	283	409	571
$l_q$	160	224	256	384	512

NOTE Tables C.3 and C.4 are based on FIPS 186-3, Appendix D (See [5]). Examples of elliptic curves in the same document are recommended.

### C.6 Selecting sizes of parameters for IFSC

Sizes for the following parameters shall be considered:

$l$  the length in bits of an RSA modulus.

$l_r$  the length in bits of a random number  $r$  generated in the first step of the signcryption algorithm.

$l_H$  the length in bits of the output of a standard cryptographic hash function  $H$ .

Table C.5 — Parameter sizes for IFSC

Security level (in bits)	80	112	128	192	256
$l$	1 024	2 048	3 072	7 680	15 360
$l_r$	80	112	128	192	256
$l_H$	160	224	256	384	512

NOTE 1  $l = l_M + l_r + l_H$ , where  $l_M$  is the length in bits of plaintexts.

NOTE 2 Parameter  $l$  in Table C.5 is chosen to be identical to parameter  $l_p$  in Table C.2, based on the assumption that factorization and discrete logarithm problems have a similar degree of hardness.

### C.7 Selecting sizes of parameters for EtS

The security of EtS is based on the security of the underlying public-key encryption scheme and signature scheme. The construction is secure if it is instantiated with a secure public-key encryption scheme and a secure signature scheme. Parameter sizes should be selected for the encryption and signature key pairs in such a way that security is guaranteed for these schemes. The reader should refer to literature on selecting parameter sizes for the underlying schemes when selecting parameter sizes for this signcryption scheme.

## Annex D (informative)

### Examples

#### D.1 Introduction

This Annex contains worked examples of the operation of the four signcryption mechanisms specified in this International Standard, these being the discrete logarithm based signcryption mechanism (DLSC), the elliptic curve based signcryption mechanism (ECDLSC), and the integer factorization based signcryption mechanism (IFSC) and the encrypt-then-sign based mechanism (EtS). In the examples, integers and bit strings in typewriter font are expressed in hexadecimal notation, unless otherwise specified. Integers are right-justified in an appropriate field, and bit strings are left-justified so that their lengths in bits are a multiple of four. Spaces and line breaks are inserted for better readability.

#### D.2 Example for DLSC

##### System wide parameters

DLSC has seven system wide parameters:  $l_q, l_p, q, p, g, G$  and  $H$ . This example assumes that  $l_q = 224$  and  $l_p = 2048$ . In addition,  $G$  is instantiated by the key derivation function KDF2 (see 7.3) with a 32-bit counter starting at 1, and  $H$  by the full domain hash function FDH1 (see 7.2.2.2). Furthermore, SHA-224 as specified in Amendment 1 to ISO/IEC 10118-3:2004 assumes the role of the underlying cryptographic hash function for both KDF2 and FDH1. The values of the remaining three system wide parameters  $q, p$  and  $g$  are represented below in hexadecimal notation.

$q =$  801C0D34 C58D93FE 99717710 1F80535A 4738CEBC BF389A99  
B36371EB

$p =$  AD107E1E 9123A9D0 D660FAA7 9559C51F A20D64E5 683B9FD1  
B54B1597 B61D0A75 E6FA141D F95A56DB AF9A3C40 7BA1DF15  
EB3D688A 309C180E 1DE6B85A 1274A0A6 6D3F8152 AD6AC212  
9037C9ED EFDA4DF8 D91E8FEF 55B7394B 7AD5B7D0 B6C12207  
C9F98D11 ED34DBF6 C6BA0B2C 8BBC27BE 6A00E0A0 B9C49708  
B3BF8A31 70918836 81286130 BC8985DB 1602E714 415D9330  
278273C7 DE31EFDC 7310F712 1FD5A074 15987D9A DC0A486D  
CDF93ACC 44328387 315D75E1 98C641A4 80CD86A1 B9E587E8  
BE60E69C C928B2B9 C52172E4 13042E9B 23F10B0E 16E79763  
C9B53DCF 4BA80A29 E3FB73C1 6B8E75B9 7EF363E2 FFA31F71  
CF9DE538 4E71B81C 0AC4DFFE 0C10E64F

$g =$  AC4032EF 4F2D9AE3 9DF30B5C 8FFDAC50 6CDEBE7B 89998CAF  
74866A08 CFE4FFE3 A6824A4E 10B9A6F0 DD921F01 A70C4AFA  
AB739D77 00C29F52 C57DB17C 620A8652 BE5E9001 A8D66AD7  
C1766910 1999024A F4D02727 5AC1348B B8A762D0 521BC98A  
E2471504 22EA1ED4 09939D54 DA7460CD B5F6C6B2 50717CBE  
F180EB34 118E98D1 19529A45 D6F83456 6E3025E3 16A330EF  
BB77A86F 0C1AB15B 051AE3D4 28C8F8AC B70A8137 150B8EEB  
10E183ED D19963DD D9E263E4 770589EF 6AA21E7F 5F2FF381  
B539CCE3 409D13CD 566AFBB4 8D6C0191 81E1BCFE 94B30269  
EDFE72FE 9B6AA4BD 7B5A0F1C 71CFFF4C 19C418E1 F6EC0179  
81BC087F 2A7065B3 84B890D3 191F2BFA

### Public and private key pairs

The sender's public and private key pair  $(y_A, x_A)$  and the recipient's public and private key pair  $(y_B, x_B)$  are assigned the following values in hexadecimal notation.

$y_A =$  0C3618A2 2B37A58E EC74D9B7 AAFA24E9 E2A32415 FD13BF19  
 91D79864 48E8CF56 23B074C0 5ED99F85 AC75D0DE 7FF4131D  
 7854210C 2C88FB41 6211D6E8 0D37ECF1 5F2A8536 8F8953F7  
 03FCCFD1 972ED722 0A0AA9FD A1AC3FC0 85641081 D07B2C0C  
 93226456 EB9FB8DE BBA46080 8806AA70 E4543604 8898C7ED  
 0FCA25EF 4D796D18 D80D97AA 89C1DB49 371FF49C 2BB1FBA4  
 CCC0690D BD2E66AC FCC9C1D4 DA8F5CCC C5795C23 8160F903  
 815FA73C 1D84459D 5380D508 02815E74 29A411D3 5899B97D  
 DE4D800B FF7C84FF 2E7796BD 23B61DF9 FD4F1CCE A84CF110  
 EBD03FF2 454851E1 E4B0C2C3 D360D427 63C5B48A E2132DFB  
 BC19AB95 E1FC2331 B792C6DD 5A71B120

$x_A =$  51941AE6 01418614 86A16DEE 6B133EA7 2513AF12 462D7A49  
 0A53F4BB

$y_B =$  1E94AEF7 E5E5AACA E51E3C8B BA22F33D 27DA5939 A616F7C0  
 19CCC3ED 295EF62B 230E26A3 B21AA147 1413B4D8 4D46E779  
 B5450067 C16C6783 20B5908D 2B47A35C 7EAC9DB6 CC550F5F  
 6DAC06EB BF949CFE 1C1C2551 BB4AE046 E9FB4CAB 0B462C9A  
 A7F0E88B 3E03F1BB F9DF8877 22300F75 14F6E0D1 9868E55A  
 2A25D2FE 0C2E4B35 42188587 D9AE4A0C 1A618760 BA7D6DB1  
 4DE2CC2C 7614FC98 4A2EE754 0A3FBF8 CA794125 578D4843  
 E319B0DB 84763D06 4B0ABD44 C4D84202 31DF3F96 8686B702  
 C0BDF981 93E3D8DE 0E95DCA7 B610D66E 9B5296C7 AF84ED3F  
 FB437158 BCF499B6 C624820B 858006FB E32E7F8E E0DDA1B7  
 3A406113 D071722D AD469C26 7B1C9599

$x_B =$  11FB849F 5EF90A5A DA6444DC A522EDA2 8C4D4ADA 81D378C7  
 5B0458EA

### Message and label

The message  $M$  is 'This is the message to be signcrypted' and the encryption label is '0001', without the quotation marks. Their hexadecimal values are as follows.

$M =$  54686973 20697320 74686520 6D657373 61676520 746F2062  
 65207369 676E6372 79707465 64

$label =$  30303031

### Values in signcrypton process

The following sequence of values in hexadecimal notation trace key intermediate variables leading to the resultant ciphertext  $X$  when the signcrypton algorithm *DLSC.Signcrypt* is applied to the message  $M$ .

$u =$  595970EF CBAFB118 EB0E8171 816E8901 671E3E11 CF9BD976  
 609FDDA9

$K =$  A11EDC14 3F0C2E2F D0495BD2 BCEB6DF4 5655FB91 EA0F06A2  
 6786B100 E1ED1A58 BD5BCCD2 60D34114 8701F21B 0373D302

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903E4193 89ED4858 D38FDB93 11607F8A 44CBA98B 32FDA4EC  
 2F93AF19 4D50AB37 59AA7E7D 3204EBFE BB61CFAD 21356C1F  
 928911F6 7C1FD9E9 1D79AFC0 772BFC82 481386BF DCD599D5  
 17C88050 D5461F37 AD43A9BB 8F012A21 860B78CB 86ED0591  
 49226F08 A5D98458 E4538453 DBE5CD63 865543DA BF9CA670  
 6810EB83 8871206E 84166DCD 880F3A45 3035D818 02DF02AD  
 D4B60E08 C37098EA EA99D886 A0698CDB 0E22B3A7 16E68FAD  
 A1D565EE F8BFF693 85E8C4BF A115ED9E DA7E69DC B9AF35F1  
 B82B86AF BACA5BFC F0EDEC1F DFA0AD76

$G(I2BSP(K, l_p), |M|) =$

0D243616 72903B4E 2F6B9917 E9DA0086 D3BAF174 00AEF710  
 720EB31C DF534B7F 92616FE3 CA

$C =$  594C5F65 52F9486E 5B03FC37 84BF73F5 B2DD9454 74C1D772  
 172EC075 B83D280D EB111B86 AE

Input to  $H =$

A11EDC14 3F0C2E2F D0495BD2 BCEB6DF4 5655FB91 EA0F06A2  
 6786B100 E1ED1A58 BD5BCCD2 60D34114 8701F21B 0373D302  
 903E4193 89ED4858 D38FDB93 11607F8A 44CBA98B 32FDA4EC  
 2F93AF19 4D50AB37 59AA7E7D 3204EBFE BB61CFAD 21356C1F  
 928911F6 7C1FD9E9 1D79AFC0 772BFC82 481386BF DCD599D5  
 17C88050 D5461F37 AD43A9BB 8F012A21 860B78CB 86ED0591  
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