

# TECHNICAL REPORT



**Measurement methods of the complex relative permeability and permittivity of noise suppression sheet**

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ICS 29.100.10

ISBN 978-2-8322-9085-9

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## CONTENTS

FOREWORD.....	6
INTRODUCTION.....	8
1 Scope.....	9
2 Normative references .....	9
3 Terms, definitions and symbols.....	9
3.1 Terms and definitions.....	9
3.2 Symbols.....	9
4 General .....	10
5 Measurement methods .....	11
5.1 Inductance method .....	11
5.1.1 Measurement parameters .....	11
5.1.2 Measurement frequency and accuracy.....	11
5.1.3 Measurement principle.....	12
5.1.4 Test sample.....	14
5.1.5 Test fixture .....	14
5.1.6 Measurement environment.....	14
5.1.7 Measurement uncertainty.....	14
5.1.8 Measurement system.....	16
5.1.9 Measurement procedure .....	16
5.1.10 Example of measurement results .....	16
5.1.11 Remarks .....	17
5.2 Nicolson Ross Weir method .....	18
5.2.1 Principle .....	18
5.2.2 Measurement frequency and accuracy.....	20
5.2.3 Measurement parameters .....	20
5.2.4 Test sample.....	20
5.2.5 Measurement environment.....	21
5.2.6 Measurement uncertainty.....	21
5.2.7 Measurement system.....	22
5.2.8 Test fixture .....	22
5.2.9 Measurement procedure .....	22
5.2.10 Example of measurement results .....	23
5.2.11 Remarks .....	23
5.3 Short-circuited microstrip line method .....	24
5.3.1 Principle .....	24
5.3.2 Measurement frequency and accuracy.....	25
5.3.3 Measurement parameters .....	25
5.3.4 Test sample.....	25
5.3.5 Measurement environment.....	26
5.3.6 Measurement system.....	26
5.3.7 Test fixture (MSL jig) .....	26
5.3.8 Measurement procedure .....	27
5.3.9 Results (example).....	27
5.3.10 Remarks .....	28
5.4 Short-circuited coaxial line method .....	28
5.4.1 Principle .....	28

5.4.2	Measurement frequency and accuracy .....	29
5.4.3	Measurement parameters .....	30
5.4.4	Test sample .....	30
5.4.5	Measurement environments .....	30
5.4.6	Measurement system .....	30
5.4.7	Test fixture (coax jig) .....	31
5.4.8	Measurement procedure .....	31
5.4.9	Results (example) .....	32
5.4.10	Remarks .....	33
5.5	Shielded loop coil method .....	33
5.5.1	Measurement principle .....	33
5.5.2	Measurement frequency and accuracy .....	38
5.5.3	Measurement parameters .....	39
5.5.4	NSS sample dimension and recommendation .....	39
5.5.5	Measurement environment .....	40
5.5.6	Measurement system .....	40
5.5.7	Measurement procedure .....	40
5.5.8	Measurement results .....	41
5.5.9	Summary .....	44
5.6	Harmonic resonance cavity perturbation method .....	45
5.6.1	Theory .....	45
5.6.2	Permeability evaluation .....	46
5.6.3	Permittivity evaluation .....	53
Annex A (informative) Derivation of the complex relative permeability of the inductance method .....		59
Annex B (informative) Short-circuited microstrip line method .....		61
B.1	Fundamental calculation .....	61
B.2	Determination of $C_S$ and $G_S$ .....	62
B.3	Determination of demagnetization factor $N$ and coupling coefficient $\eta$ .....	64
B.4	Analysis with the software to determine the $\mu_r$ .....	64
Annex C (informative) Short-circuited coaxial line method .....		66
C.1	Fundamental calculation to determine $\mu_r$ .....	66
C.2	Open-circuited coaxial line .....	67
C.2.1	Measurement of effective permittivity $\varepsilon_r (\varepsilon'_r - j\varepsilon''_r)$ .....	67
C.2.2	Example of the complex permittivity .....	70
C.3	Remarks on lumped element approximation .....	71
Bibliography .....		73
Figure 1 – In-plane and perpendicular measurement direction of NSS sample .....		11
Figure 2 – Toroidal-shaped sample cut from the NSS .....		12
Figure 3 – Test fixture with a toroidal-shaped NSS sample .....		13
Figure 4 – Equivalent circuit model of the test fixture .....		13
Figure 5 – Schematic diagram of measurement system .....		16
Figure 6 – Measurement results of NSS samples .....		17
Figure 7 – Schematic diagram of a test fixture with a sample and signal flow graph .....		18
Figure 8 – Cross section of coaxial line with NSS .....		20
Figure 9 – Dimensions of test sample .....		21

Figure 10 – Schematic diagram of equipment system for measurement .....	22
Figure 11 – Specification for test fixture of a 7 mm coaxial transmission line .....	22
Figure 12 – Measurement results of noise suppression sheet .....	23
Figure 13 – Equivalent circuits for the MSL .....	25
Figure 14 – Rectangular shape of NSS sample .....	26
Figure 15 – Measurement system .....	26
Figure 16 – Short-circuited microstrip line test fixture (MSL jig).....	27
Figure 17 – Complex relative permeability of a NSS sample C with 0,236 mm thickness, as measured at $N = 0$ (and $\eta = 0,135 2$ ) and corrected by demagnetization factor $N = 0,037$ (and $\eta = 0,135 2$ ) .....	28
Figure 18 – Equivalent circuits for the coax jig .....	29
Figure 19 – Toroidal shape of NSS sample .....	30
Figure 20 – Measurement system .....	31
Figure 21 – Short-circuited coaxial line test fixture (coax jig).....	31
Figure 22 – Complex relative permeability of a NSS sample A with 0,29 mm thickness, as measured and corrected by the permittivity .....	32
Figure 23 – Complex relative permeability of a NSS sample B with 0,25 mm thickness, as measured and corrected by the effective permittivity .....	33
Figure 24 – Structure of shielded loop coil .....	34
Figure 25 – Shielded loop coil and NSS sample arrangement .....	34
Figure 26 – Whole structure of the measuring unit of the equipment .....	35
Figure 27 – DC magnetization curve .....	38
Figure 28 – Estimation of absolute value correction coefficient $M'_s$ .....	38
Figure 29 – Recommended shape of NSS sample .....	39
Figure 30 – Block diagram of measurement system .....	40
Figure 31 – Measured complex relative permeability as a function of the size of a NSS sheet (Sample A-01) .....	42
Figure 32 – Measured complex relative permeability as a function of the size of a NSS sheet (Sample B-01) .....	43
Figure 33 – Measured complex relative permeability of a NSS sheet as a function of DC bias field intensity (Sample A-02).....	43
Figure 34 – Measured complex relative permeability after absolute value calibration (Sample A-01) .....	44
Figure 35 – Measured complex relative permeability after absolute value calibration (Sample B-01) .....	44
Figure 36 – Electromagnetic flux to evaluate permeability in the harmonic resonance cavity resonator .....	47
Figure 37 – Example of the resonance characteristics change .....	47
Figure 38 – Cavity resonator for 3,6 GHz to 7,2 GHz .....	48
Figure 39 – Cavity resonator for 0,25 GHz to 2 GHz .....	48
Figure 40 – Examples of resonance frequencies .....	49
Figure 41 – Example of the resonance curves of a harmonic resonance cavity .....	49
Figure 42 – Examples of samples .....	50
Figure 43 – Measuring system .....	50
Figure 44 – Sample installation in the cavity for the permeability measurement .....	51
Figure 45 – Measured results of the permeability for Sample A and B and a copper rod .....	53

Figure 46 – Electromagnetic flux to evaluate permittivity in the harmonic resonance cavity resonator .....	53
Figure 47 – Sample installation in the cavity for the permittivity measurement .....	55
Figure 48 – Adjustment procedure and adjusted results .....	56
Figure 49 – Measured results of the permittivity for the two samples, A and B .....	58
Figure B.1 – Complex relative permeabilities of Sample C with 0,236 mm thickness for toroidal shape and rectangular shape corrected by $N = 0,037$ and $\eta = 0,135 2$ .....	64
Figure B.2 – Complex relative permeabilities of Sample C with 0,236 mm thickness for rectangular shape corrected by $N = 0, 0,018 5$ and $0,037$ with $\eta = 0,135 2$ .....	65
Figure B.3 – Complex relative permeabilities of Sample C with 0,236 mm thickness for rectangular shape corrected by $\eta = 0,225 3, 0,169$ and $0,135 2$ with $N = 0,037$ .....	65
Figure C.1 – Open-circuited coaxial line jig .....	68
Figure C.2 – Equivalent circuits for the open-circuited coaxial line .....	68
Figure C.3 – Complex relative permittivity of NSS Sample A with 0,29 mm thickness, as measured and corrected by the permeability .....	71
Figure C.4 – Complex relative permittivity of NSS Sample B with 0,25 mm thickness, as measured and corrected by the permeability .....	71
Figure C.5 – Dependence of phase shift $\beta l$ on frequency .....	72
Table 1 – Measurement method and frequency .....	10
Table 2 – Measurement sample table .....	42

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## MEASUREMENT METHODS OF THE COMPLEX RELATIVE PERMEABILITY AND PERMITTIVITY OF NOISE SUPPRESSION SHEET

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The text of this Technical Specification is based on the following documents:

Draft TR	Report on voting
51/1349/DTR	51/1356/RVDTR

Full information on the voting for its approval can be found in the report on voting indicated in the above table.

The language used for the development of this Technical Report is English.

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## INTRODUCTION

Noise suppression sheet (NSS) is used near the source of high frequency electromagnetic noise, path of noise propagation and source of emission. It is used like a patch and is different from an electromagnetic wave absorber in free space. IEC 62333-2 specifies five measurement methods in order to estimate the effect of NSS. To evaluate the effect by computer simulation, it is indispensable to know the frequency characteristics of both permeability and permittivity. And to make a rough estimate of the noise suppression effect of NSS, it is useful to understand effective permeability and effective permittivity, which are the permeability and permittivity of an actually used shape.

As most NSSs are flexible, and both complex relative permeability and complex relative permittivity have anisotropy, careful study and understanding of the principles are indispensable for the measurement of the frequency characteristics of permeability and permittivity.

There are various methods to measure permeability and permittivity under the frequency range where NSS is used. This document is intended to be used for the proper selection of the measurement method and the preparation of the test sample to achieve the above purpose when measuring permeability and permittivity, the two parameters which largely influence the noise suppression effect of the NSS.

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# MEASUREMENT METHODS OF THE COMPLEX RELATIVE PERMEABILITY AND PERMITTIVITY OF NOISE SUPPRESSION SHEET

## 1 Scope

This document provides guidelines on the methods for measuring the frequency characteristics of permeability and permittivity in the frequency range of 1 MHz to 6 GHz for a noise suppression sheet for each electromagnetic noise countermeasure.

## 2 Normative references

There are no normative references in this document.

## 3 Terms, definitions and symbols

### 3.1 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

- IEC Electropedia: available at <http://www.electropedia.org/>
- ISO Online browsing platform: available at <http://www.iso.org/obp>

#### 3.1.1

##### **noise suppression**

suppression which consists of signal decoupling, radiation suppression and attenuation of the transmission power of noise by an electronic product

Note 1 to entry: Each function above is achieved by absorption and/or shielding.

#### 3.1.2

##### **noise suppression sheet**

NSS

sheet which enables noise suppression and is composed of magnetic, dielectric or conductive material with electromagnetic losses

EXAMPLE Sheet made of soft magnetic metal powder and resin or rubber.

#### 3.1.3

##### **suppression ratio**

ratio of the noise level with and without suppression sheets

Note 1 to entry: The suppression ratio is classified into intra-decoupling ratio, inter-decoupling ratio, transmission attenuation power ratio and radiation suppression ratio. It is expressed in dB.

## 3.2 Symbols

$\mu_r$	complex relative permeability
$\mu_r'$	real part of complex relative permeability
$\mu_r''$	imaginary part of complex relative permeability
$\varepsilon_r$	complex relative permittivity

- $\epsilon'_r$  real part of complex relative permittivity
- $\epsilon''_r$  imaginary part of complex relative permittivity
- $Z$  impedance ( $\Omega$ )
- $\omega = 2\pi f$  angular frequency (rad/s)
- $I$  current (A)
- $B = \mu_0\mu_r H$  magnetic flux density (T)
- $H$  magnetic field strength (A/m)
- $\mu_0$  permeability of vacuum ( $4\pi \times 10^{-7}$  H/m)
- $f$  frequency

#### 4 General

Composite materials made by embedding magnetic metal flakes in a plastic sheet are widely used in PCs or mobile phone handsets. This sheet is well known as a noise suppression sheet (NSS) and is used to reduce unwanted signals in transmission lines or unwanted couplings between circuit elements in the devices described above.

Electromagnetic compatibility (EMC) designers recently have been using simulations for the design of the circuit boards for PCs and mobile phone handsets. In these simulations, it is important to know the complex relative permeability  $\mu_r$  and the complex relative permittivity  $\epsilon_r$  of NSS. This document shows the six measurement methods of  $\mu_r$  and  $\epsilon_r$  of NSS. The measurement frequency range is from 1 MHz to 6 GHz, as shown in Table 1. Figure 1 illustrates the in-plane and perpendicular measurement direction of Table 1.

**Table 1 – Measurement method and frequency**

Method Name	$\mu_r$ and $\epsilon_r$				Frequency				
	In-plane		Perpendicular		1 MHz to 10 MHz	100 MHz	1 GHz	10 GHz	100 GHz
	$\mu_r$	$\epsilon_r$	$\mu_r$	$\epsilon_r$					
5.1 Inductance	○				1 MHz to 1 GHz				
5.2 Nicolson Ross Weir	○	○					500 MHz to		
5.3 Short-circuited micro strip line	○				10 MHz to 10 GHz				
5.4 Short-circuited coaxial line	○	○			1 MHz to 18 GHz				
5.5 Shielded loop coil	○				1 MHz to 10 GHz				
5.6 Harmonic resonance cavity perturbation	○		○				250 MHz to 18 GHz		
		○		○				1,8 MHz	

Range of frequency (1 MHz to 6 GHz)

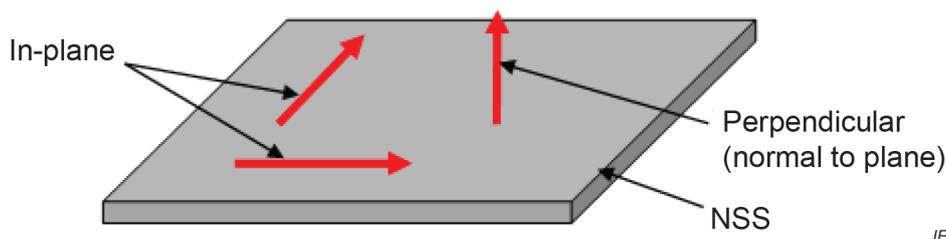


Figure 1 – In-plane and perpendicular measurement direction of NSS sample

## 5 Measurement methods

### 5.1 Inductance method

#### 5.1.1 Measurement parameters

The measurement parameters of a magnetic material are defined as follows:

$$\mu_r = \mu_r' - j\mu_r'' \quad (1)$$

where

$\mu_r'$  and  $\mu_r''$  are the real part and the imaginary part of the complex relative permeability, respectively.

#### 5.1.2 Measurement frequency and accuracy

The objective of this method is to evaluate the in-plane permeability of toroidal-shaped thin NSS samples shown in Figure 2 and is applicable for the measurements under the following conditions:

frequency	:	$1 \text{ MHz} \leq f \leq 1 \text{ GHz}$
relative permeability	:	$1 \leq \mu_r' \leq 1\,000$ $0 \leq \mu_r'' \leq 1\,000$
accuracy	:	value error $\pm 20\%$ for $\mu_r'$ value error $\pm 20\%$ for $\mu_r''$

The measurement frequency range is affected by the dimensions and the permeability values of the NSS sample. The higher the permeability, the lower the upper limit of the frequency range will be.

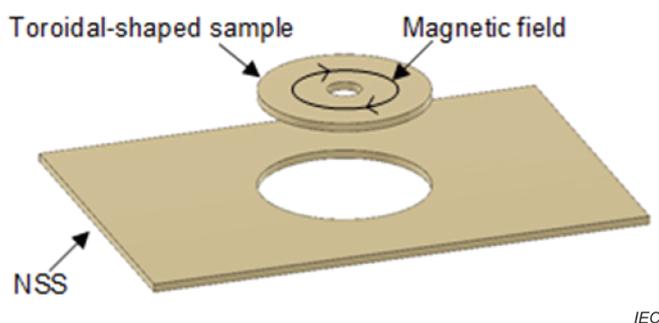


Figure 2 – Toroidal-shaped sample cut from the NSS

### 5.1.3 Measurement principle

The test fixture shown in Figure 3 forms the ideal one-turn inductor. The self-inductance is given by

$$\frac{Z}{j\omega} = \frac{1}{I} \int_S B ds \quad (2)$$

where

- $Z$  is the impedance ( $\Omega$ );
- $\omega = 2\pi f$  is the angular frequency (rad/s);
- $I$  is the current (A);
- $B = \mu_0 \mu_r H$  is the magnetic flux density (T);
- $H$  is the Magnetic field strength (A/m);
- $\mu_0$  is the permeability of vacuum ( $4\pi \times 10^{-7}$  H/m);
- $S$  is the surface shown in Figure 3.

Therefore, the complex relative permeability is

$$\mu_r = \frac{2\pi Z_m - Z_{sm}}{\mu_0 j\omega F} + 1 = \frac{2\pi Z_{NSS}}{\mu_0 j\omega F} + 1 \quad (3)$$

or

$$\mu_r' = \frac{2\pi x_m - x_{sm}}{\mu_0 \omega F} + 1 = \frac{2\pi x_{NSS}}{\mu_0 \omega F} + 1 \quad (4)$$

$$\mu_r'' = \frac{2\pi r_m - r_{sm}}{\mu_0 \omega F} = \frac{2\pi r_{NSS}}{\mu_0 \omega F} \quad (5)$$

where

- $Z_m = r_m + jx_m$  is the measured impedance with a sample;
- $Z_{sm} = r_{sm} + jx_{sm}$  is the measured impedance without a sample (in short state);
- $Z_{NSS} = r_{NSS} + jx_{NSS}$  is the impedance of a NSS sample;

$F = t \ln\left(\frac{b}{a}\right)$  is the shape factor of a sample, inner diameter  $a$ , outer diameter  $b$ , and thickness  $t$ .

$Z_{sm}$  is used to minimize errors due to residual impedance by compensation. The equivalent circuit model of the test fixture is shown in Figure 4.  $g_p + jb_p$  is the admittance of the test fixture and its effect can be neglected in a simplified case. Therefore, the impedance  $Z_{NSS}$  of a NSS sample is  $Z_m - Z_{sm}$ .

The derivation procedure is shown in detail in Annex A.

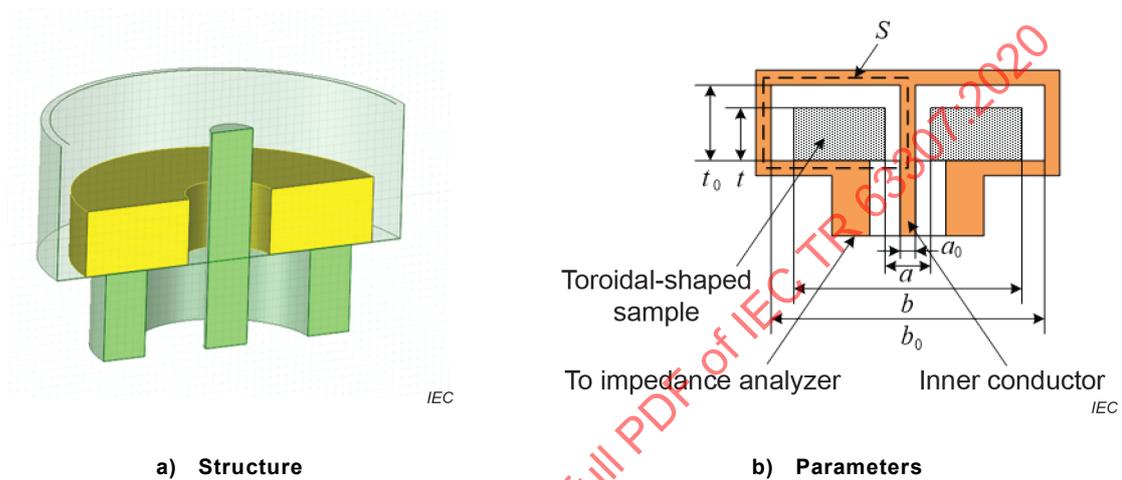


Figure 3 – Test fixture with a toroidal-shaped NSS sample

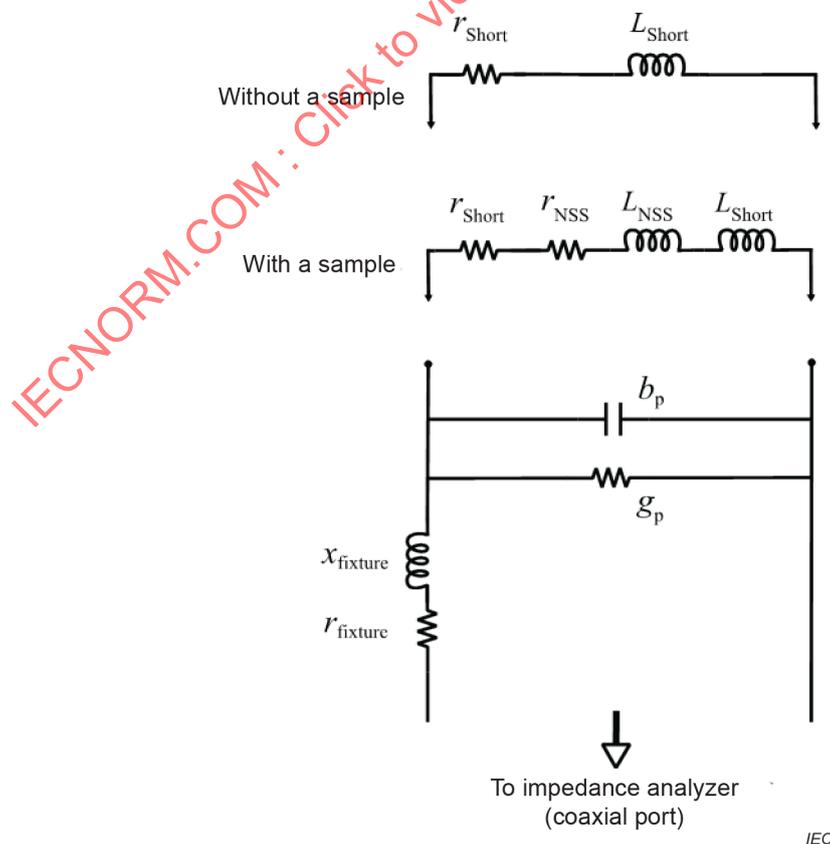


Figure 4 – Equivalent circuit model of the test fixture

#### 5.1.4 Test sample

The sample shall be fabricated in the shape of a toroidal ring. A good round sample can be obtained by a punching tool. The preferable sample size is as follows:

For the fixture of 24 mm diameter in 5.1.5:

inner diameter :  $a \geq 3,1$  mm  
 outer diameter :  $b \leq 8$  mm  
 thickness :  $t \leq 3$  mm

For the fixture of 30 mm diameter:

inner diameter :  $a \geq 5$  mm  
 outer diameter :  $b \leq 20$  mm  
 thickness :  $t \leq 8,5$  mm

Each parameter should be measured with a precision of less than 1/100 mm using a micrometer.

#### 5.1.5 Test fixture

The structure of the test fixture is shown in Figure 3. The test fixture is a conductive shield surrounding the central conductor and terminates in a short circuit. The connector of the test fixture is connected through the coaxial connector to the measurement equipment. The alignment error of the NSS sample from the centre affects the measurement results, so the use of a sample holder is recommended to place a sample coaxially. Examples of features of a test fixture are as follows:

diameter :  $b_0 = 24$  mm  
 height :  $t_0 = 30$  mm  
 resistance :  $r_{sm} = 100$  m $\Omega$   
 inductance :  $x_{sm}/\omega = 1,0$  nH

or

diameter :  $b_0 = 30$  mm  
 height :  $t_0 = 35$  mm  
 resistance :  $r_{sm} = 300$  m $\Omega$   
 inductance :  $x_{sm}/\omega = 5,5$  nH

The diameter of a centre conductor is  $a_0 = 3$  mm for both fixtures.

#### 5.1.6 Measurement environment

The fixture and the samples shall be kept in a clean and dry state. The room temperature and the relative humidity shall preferably be  $23$  °C  $\pm$   $5$  °C and less than 60 %.

#### 5.1.7 Measurement uncertainty

Measurement uncertainties of  $u'_r$  and  $\mu''$ ,  $u(\mu'_r)$  and  $u(\mu''_r)$ , are estimated as the combined standard uncertainty and given respectively by

$$u(\mu_r')^2 = \left(\frac{\partial \mu_r'}{\partial x_m}\right)^2 u(x_m)^2 + \left(\frac{\partial \mu_r'}{\partial x_{sm}}\right)^2 u(x_{sm})^2 + \left(\frac{\partial \mu_r'}{\partial a}\right)^2 u(a)^2 + \left(\frac{\partial \mu_r'}{\partial b}\right)^2 u(b)^2 + \left(\frac{\partial \mu_r'}{\partial t}\right)^2 u(t)^2 \quad (6)$$

$$u(\mu_r'')^2 = \left(\frac{\partial \mu_r''}{\partial r_m}\right)^2 u(r_m)^2 + \left(\frac{\partial \mu_r''}{\partial r_{sm}}\right)^2 u(r_{sm})^2 + \left(\frac{\partial \mu_r''}{\partial a}\right)^2 u(a)^2 + \left(\frac{\partial \mu_r''}{\partial b}\right)^2 u(b)^2 + \left(\frac{\partial \mu_r''}{\partial t}\right)^2 u(t)^2 \quad (7)$$

where  $u(x_m)$ ,  $u(x_{sm})$ ,  $u(r_m)$ ,  $u(r_{sm})$ ,  $u(a)$ ,  $u(b)$  and  $u(t)$  are standard uncertainties of  $x_m$ ,  $x_{sm}$ ,  $r_m$ ,  $r_{sm}$ ,  $a$ ,  $b$  and  $t$ , respectively. The sensitivity coefficients in Formulae (6) and (7) are as follows:

$$\frac{\partial \mu_r'}{\partial x_m} = \frac{2\pi}{\mu_0} \frac{1}{\omega F} \quad (8)$$

$$\frac{\partial \mu_r'}{\partial x_{sm}} = \frac{2\pi}{\mu_0} \left(-\frac{1}{\omega F}\right) \quad (9)$$

$$\frac{\partial \mu_r'}{\partial a} = \frac{2\pi}{\mu_0} \frac{x_m - x_{sm}}{\omega} \frac{t}{a F^2} \quad (10)$$

$$\frac{\partial \mu_r'}{\partial b} = \frac{2\pi}{\mu_0} \frac{x_m - x_{sm}}{\omega} \left(-\frac{t}{b F^2}\right) \quad (11)$$

$$\frac{\partial \mu_r'}{\partial h} = \frac{2\pi}{\mu_0} \frac{x_m - x_{sm}}{\omega} \left(-\frac{1}{t F}\right) \quad (12)$$

$$\frac{\partial \mu_r''}{\partial r_m} = \frac{2\pi}{\mu_0} \frac{1}{\omega F} \quad (13)$$

$$\frac{\partial \mu_r''}{\partial r_{sm}} = \frac{2\pi}{\mu_0} \left(-\frac{1}{\omega F}\right) \quad (14)$$

$$\frac{\partial \mu_r''}{\partial a} = \frac{2\pi}{\mu_0} \frac{r_m - r_{sm}}{\omega} \frac{t}{a F^2} \quad (15)$$

$$\frac{\partial \mu_r''}{\partial b} = \frac{2\pi}{\mu_0} \frac{r_m - r_{sm}}{\omega} \left(-\frac{t}{b F^2}\right) \quad (16)$$

$$\frac{\partial \mu_r''}{\partial h} = \frac{2\pi}{\mu_0} \frac{r_m - r_{sm}}{\omega} \left(-\frac{1}{t F}\right) \quad (17)$$

### 5.1.8 Measurement system

Figure 5 shows a schematic diagram of the measurement system. For the measurement of the magnetic properties, the information on the ratio of the current and voltage values and the phase difference between current and voltage are needed. An impedance analyzer, LCR meter or vector network analyzer (VNA) can be used for the measurement.

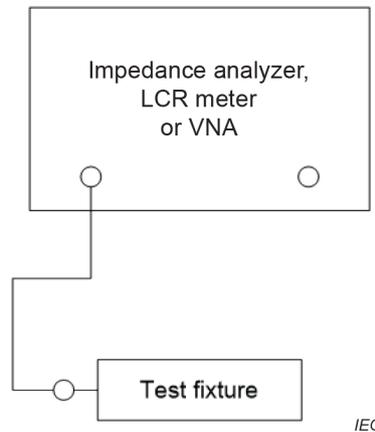


Figure 5 – Schematic diagram of measurement system

### 5.1.9 Measurement procedure

- 1) Calibrate the measurement equipment

When the measurement equipment is turned ON, the calibration shall be performed with the proper calibration kit to measure within its specified measurement accuracy. The measurement system shall be warmed up sufficiently before starting the calibration.

- 2) Connect the test fixture

Connect the connector of the test fixture to the coaxial connector of the previously calibrated measurement equipment.

- 3) Place the sample holder and measure the impedance  $Z_{sm}$

Place only the sample holder in the test fixture. Enter the measurement parameters, frequency range and oscillator output voltage level and other values, into the measurement equipment and measure the impedance  $Z_{sm}$  of the test fixture.

- 4) Place the NSS sample and measure the impedance  $Z_m$

Place the toroidal-shaped NSS sample with the sample holder in the test fixture coaxially and measure the impedance  $Z_m$  of the test fixture with a sample.

- 5) Calculate the relative permeability  $\mu'_r$  and  $\mu''_r$  and uncertainties  $u(\mu'_r)$  and  $u(\mu''_r)$

Calculate the values of  $\mu'_r$  and  $\mu''_r$  by using Formula (4) and Formula (5), respectively. The measurement uncertainties are also calculated by using Formula (6) to Formula (17).

### 5.1.10 Example of measurement results

The measurement results of  $\mu'_r$  and  $\mu''_r$  for a NSS (sample A and B) are shown in Figure 6. The parameters of the sample are  $a = 3,00$  mm,  $b = 7,00$  mm and  $t = 0,20$  mm (sample A) or  $0,25$  mm (sample B), and the oscillator output voltage level, about  $0,1$  V, is selected in order not to affect the results.

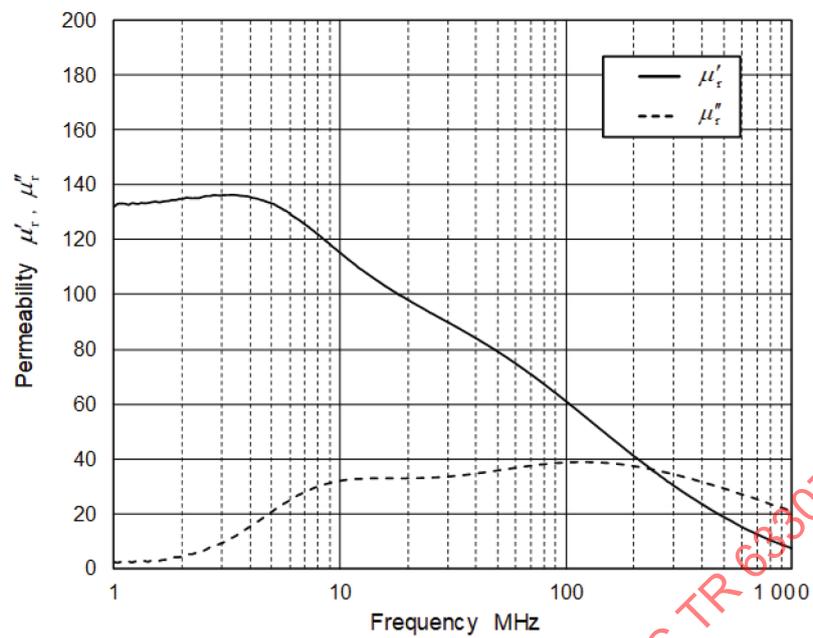
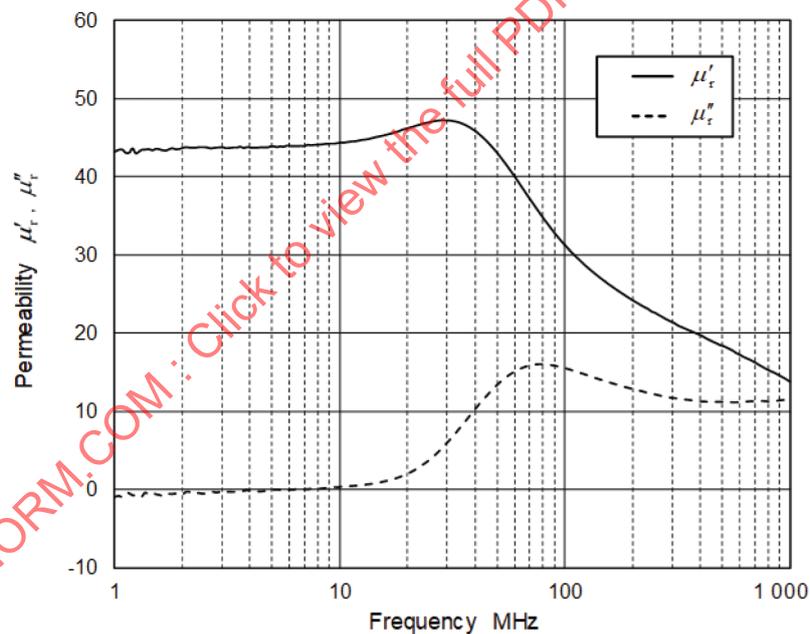
a) Sample A ( $t = 0,20\text{mm}$ )b) Sample B ( $t = 0,25\text{mm}$ )

Figure 6 – Measurement results of NSS samples

### 5.1.11 Remarks

Subclause 5.1 provides some helpful information on measuring the magnetic properties of toroidal-shaped NSS samples using the inductance method.

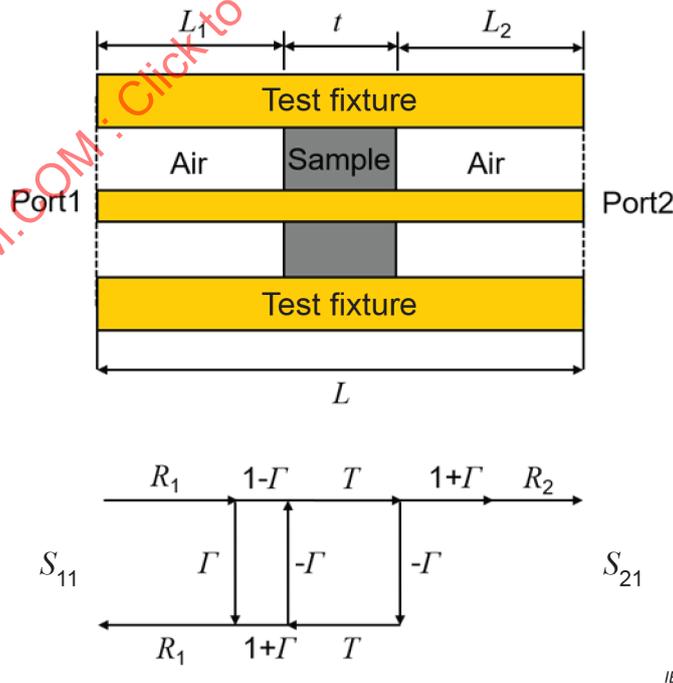
- 1) The test sample should be made correctly in a toroidal shape and placed in the test fixture coaxially.
- 2) The measurement accuracy depends on the measured impedance values and gets worse in low frequencies because the measurement error increases with a decrease in the frequency.

- 3) The use of an impedance analyzer is recommended to measure the impedance because the impedance analyzer has the advantages of higher accuracy and wider impedance measurement range than a network analyzer.
- 4) The measurement results of  $\mu'_r$  and  $\mu''_r$  may be obtained after measuring the impedance  $Z_{sm}$  and  $Z_m$  if the material analyzer is used. The measurement results of the impedance  $Z_{sm}$  and  $Z_m$  are not displayed because the software installed on the analyzer calculates and compensates the measurement results.
- 5) A sample with a low permeability or a thin thickness leads to measurement error. It is difficult to measure its permeability accurately due to the low impedance  $Z_{NSS}$  of a NSS sample. Stacking some samples is a better way to get the results needed.
- 6) When the permittivity of a NSS sample is high (more than about 10), current flows through the space between the NSS sample and the test fixture. This introduces an equivalent capacitance connected in parallel to the impedance of the sample  $Z_{NSS}$ . The resonance of this parallel LC circuit occurs at around 1 GHz or below and precise measurements will be difficult.

**5.2 Nicolson Ross Weir method**

**5.2.1 Principle**

The objective of this method is to evaluate the broadband properties of the complex relative permeability and permittivity of a noise suppression sheet by using a transmission line as coaxial line and waveguide. Measurement frequency ranges and accuracy depend on the test fixture and electromagnetic properties of a sample. This document describes a measurement method using a 7 mm coaxial transmission line. Complex relative permittivity and permeability are to be derived from the reflection and transmission coefficient of a sample inserted into a transmission line. Reflection and transmission coefficients are calculated from S-parameters  $S_{11}$  and  $S_{21}$  measured by a vector network analyzer. Figure 7 shows a schematic diagram of a test fixture with a sample and signal flow graph.



**Figure 7 – Schematic diagram of a test fixture with a sample and signal flow graph**

A signal is inserted from Port1.  $L$  and  $t$  are the length of a test fixture and sample  $L_1$  and  $L_2$  are the length from the respective reference plane to the sample faces.

From a signal flow graph, the S-parameters on a transmission line with sample are given by

$$S_{11} = R_1^2 \frac{\Gamma(1-T^2)}{1-T^2\Gamma^2} \quad (18)$$

$$S_{21} = R_1 R_2 \frac{T(1-\Gamma^2)}{1-T^2\Gamma^2} \quad (19)$$

$$R_i = \exp(-\gamma_0 L_i) \quad (i = 1, 2) \quad (20)$$

where

$\Gamma$  is the reflection coefficient at sample faces;

$T$  is the transmission coefficient of a sample;

$\gamma_0$  is the propagation constant of air;

$R_i$  is the transmission coefficient from the reference plane to the sample face at the respective ports.

Reflection coefficient  $\Gamma$  is defined by

$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} \quad (21)$$

$$Z_L = Z_0 \sqrt{\frac{\mu_r}{\epsilon_r}} \quad (22)$$

where

$Z_L$  and  $Z_0$  are the characteristic impedance of a sample and air in the transmission line.

The transmission coefficient and propagation constant of a sample on a transmission line are given by

$$T = \exp(-\gamma d) \quad (23)$$

$$\gamma = \gamma_0 \sqrt{\mu_r \epsilon_r} \quad (24)$$

where

$\gamma$  is the propagation constant of a sample.

From Formula (18) to Formula (24), the complex relative permeability and permittivity of a sample are calculated by

$$\mu_r = \left( \frac{1+\Gamma}{1-\Gamma} \right) \left( \frac{1}{\gamma_0 d} \ln \left( \frac{1}{T} \right) \right) \quad (25)$$

$$\varepsilon_r = \left( \frac{1-\Gamma}{1+\Gamma} \right) \left( \frac{1}{\gamma_0 d} \ln \left( \frac{1}{T} \right) \right) \quad (26)$$

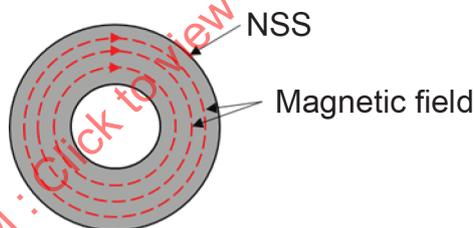
It shall be noted that the calculated value is divergent at integral multiples of half wavelength in a sample.

### 5.2.2 Measurement frequency and accuracy

The objective of this method is to measure the broadband electromagnetic properties of a sample. Measurement frequency ranges and accuracy depend on the test fixture and electromagnetic properties of a test sample. The lower frequency is limited by the smallest measurable phase shift through a sample. The upper frequency limit is determined by the excitation of higher order modes that invalidates the dominant-mode transmission line. (In the case of a 7 mm coaxial transmission line, the frequency range can be set from 500 MHz to 18 GHz.)

### 5.2.3 Measurement parameters

The objective of this method is to measure the in-plane properties of the complex relative permeability and permittivity by using a transmission line. However, the magnetic and dielectric perpendicular properties of a noise suppression sheet are not measured. Figure 8 shows the cross section of coaxial line with NSS.

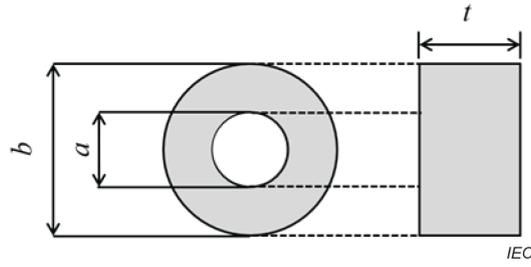


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Figure 8 – Cross section of coaxial line with NSS

### 5.2.4 Test sample

Figure 9 shows the dimensions of a test sample. The dimensions of a sample depend on the test fixture. The sample shall fully fill the cross section of the transmission line. In the case of a 7 mm coaxial transmission line, the sample shall be fabricated in the shape of a toroidal ring. The preferable sample size is shown in Figure 9:



Inner diameter of test sample:  $a = 3,04$  mm

Outer diameter of test sample:  $b = 7,00$  mm

Length of test sample:  $t \leq$  length of test fixture L.

**Figure 9 – Dimensions of test sample**

Each parameter should be measured with a precision of less than 1/100 mm using a micrometer. For measurement of a high complex relative permittivity material, a sample shall be manufactured more precisely because complex relative permittivity is influenced highly by the air gap between the sample and test fixture. The length of the sample should be such that the phase of  $S_{21}$  is less than half the wavelength.

### 5.2.5 Measurement environment

The test fixture and the samples shall be kept in a clean and dry state. The room temperature and the relative humidity shall preferably be  $23\text{ °C} \pm 5\text{ °C}$  and less than 60 %.

### 5.2.6 Measurement uncertainty

In the measurement uncertainties of  $\varepsilon'_r$ ,  $\varepsilon''_r$ ,  $\mu'_r$  and  $\mu''_r$ ,  $u(\varepsilon'_r)$ ,  $u(\varepsilon''_r)$ ,  $u(\mu'_r)$  and  $u(\mu''_r)$ , are estimated as the combined standard uncertainty and given respectively by

$$u(\mu'_r)^2 = \left( \frac{\partial \mu'_r}{\partial |S_{11}|} \right)^2 u(|S_{11}|)^2 + \left( \frac{\partial \mu'_r}{\partial \theta_{11}} \right)^2 u(\theta_{11})^2 + \left( \frac{\partial \mu'_r}{\partial |S_{21}|} \right)^2 u(|S_{21}|)^2 + \left( \frac{\partial \mu'_r}{\partial \theta_{21}} \right)^2 u(\theta_{21})^2 + \left( \frac{\partial \mu'_r}{\partial d} \right)^2 u(d)^2 + \left( \frac{\partial \mu'_r}{\partial G} \right)^2 u(G)^2 \quad (27)$$

$$u(\mu''_r)^2 = \left( \frac{\partial \mu''_r}{\partial |S_{11}|} \right)^2 u(|S_{11}|)^2 + \left( \frac{\partial \mu''_r}{\partial \theta_{11}} \right)^2 u(\theta_{11})^2 + \left( \frac{\partial \mu''_r}{\partial |S_{21}|} \right)^2 u(|S_{21}|)^2 + \left( \frac{\partial \mu''_r}{\partial \theta_{21}} \right)^2 u(\theta_{21})^2 + \left( \frac{\partial \mu''_r}{\partial d} \right)^2 u(d)^2 + \left( \frac{\partial \mu''_r}{\partial G} \right)^2 u(G)^2 \quad (28)$$

$$u(\varepsilon'_r)^2 = \left( \frac{\partial \varepsilon'_r}{\partial |S_{11}|} \right)^2 u(|S_{11}|)^2 + \left( \frac{\partial \varepsilon'_r}{\partial \theta_{11}} \right)^2 u(\theta_{11})^2 + \left( \frac{\partial \varepsilon'_r}{\partial |S_{21}|} \right)^2 u(|S_{21}|)^2 + \left( \frac{\partial \varepsilon'_r}{\partial \theta_{21}} \right)^2 u(\theta_{21})^2 + \left( \frac{\partial \varepsilon'_r}{\partial d} \right)^2 u(d)^2 + \left( \frac{\partial \varepsilon'_r}{\partial G} \right)^2 u(G)^2 \quad (29)$$

$$u(\varepsilon''_r)^2 = \left( \frac{\partial \varepsilon''_r}{\partial |S_{11}|} \right)^2 u(|S_{11}|)^2 + \left( \frac{\partial \varepsilon''_r}{\partial \theta_{11}} \right)^2 u(\theta_{11})^2 + \left( \frac{\partial \varepsilon''_r}{\partial |S_{21}|} \right)^2 u(|S_{21}|)^2 + \left( \frac{\partial \varepsilon''_r}{\partial \theta_{21}} \right)^2 u(\theta_{21})^2 + \left( \frac{\partial \varepsilon''_r}{\partial d} \right)^2 u(d)^2 + \left( \frac{\partial \varepsilon''_r}{\partial G} \right)^2 u(G)^2 \quad (30)$$

where

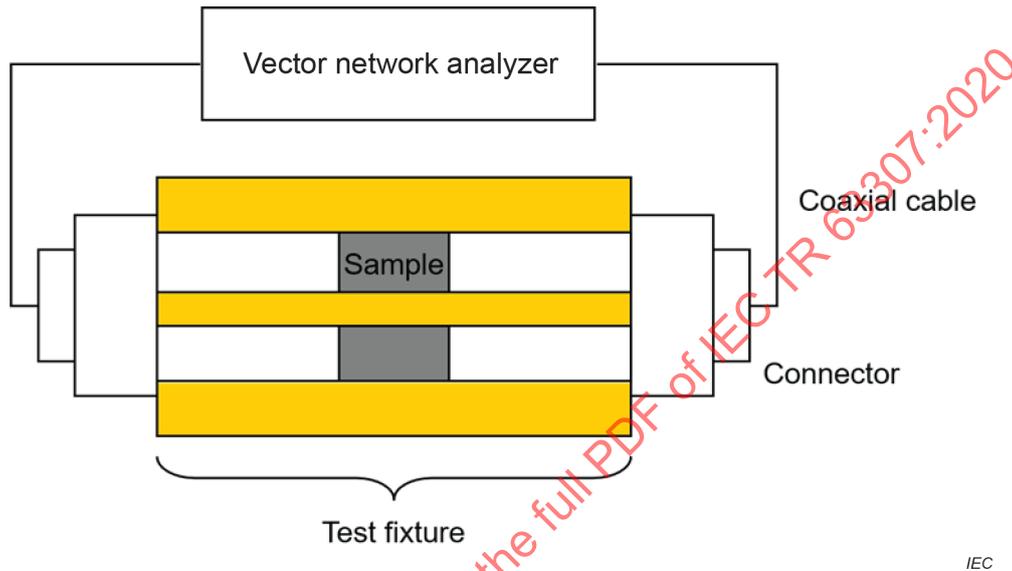
$\theta_{11}$  and  $\theta_{21}$  are the phases of the S-parameter;

$G$  is the air gap between the sample and test fixture.

The uncertainties used for the S-parameters depend on the vector network analyzer used for the measurements. This type of uncertainty analysis assumes that changes in independent variables are sufficiently small so that a Taylor series expansion is valid. There are many other uncertainty sources of lesser magnitude such as repeatability of connections and torquing of connectors. Estimates for these uncertainties could be added to the uncertainty budget sheet.

**5.2.7 Measurement system**

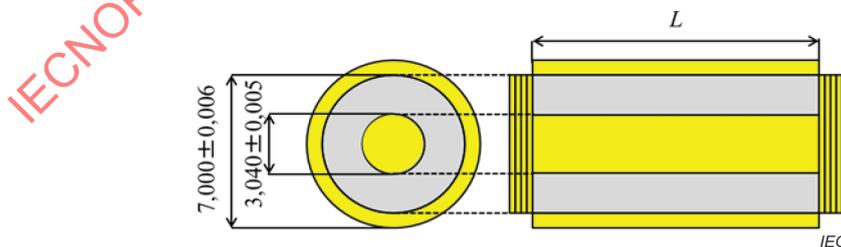
Figure 10 shows a schematic diagram of the equipment system for the measurement. For the measurement of the S-parameter, the vector network analyzer is connected to a test fixture.



**Figure 10 – Schematic diagram of equipment system for measurement**

**5.2.8 Test fixture**

Various transmission lines can be used as a test fixture. For example, Figure 11 shows a specification for a test fixture in the case of a 7 mm coaxial transmission line. The test fixture consists of an inner conductor and outer conductor. The length of the test fixture shall be longer than or equal to the length of the sample. A test fixture shall be connected to connectors which are connected to the vector network analyzer.



**Figure 11 – Specification for test fixture of a 7 mm coaxial transmission line**

**5.2.9 Measurement procedure**

- 1) When the network analyzer is turned ON, the calibration shall be performed with the proper calibration kit to measure within its specified measurement accuracy. The measurement system shall be warmed up sufficiently before starting the calibration.
- 2) The sample is inserted into the test fixture. Connect the connector of the test fixture to the connector of the previously calibrated network analyzer.

- 3) The S-parameters  $S_{11}$  and  $S_{21}$  of the test fixture with a sample are measured by using the network analyzer.
- 4) The values of the complex permeability and permittivity are calculated by using Formula (18), Formula (19), Formula (25) and Formula (26), respectively. The measurement uncertainties are estimated by using Formula (27) to Formula (30).

### 5.2.10 Example of measurement results

Figure 12 shows the measurement results of  $\epsilon'_r$ ,  $\epsilon''_r$ ,  $\mu'_r$  and  $\mu''_r$  for a noise suppression sheet with a thickness of 0,5 mm. A 7 mm coaxial transmission line is used for the measurement.

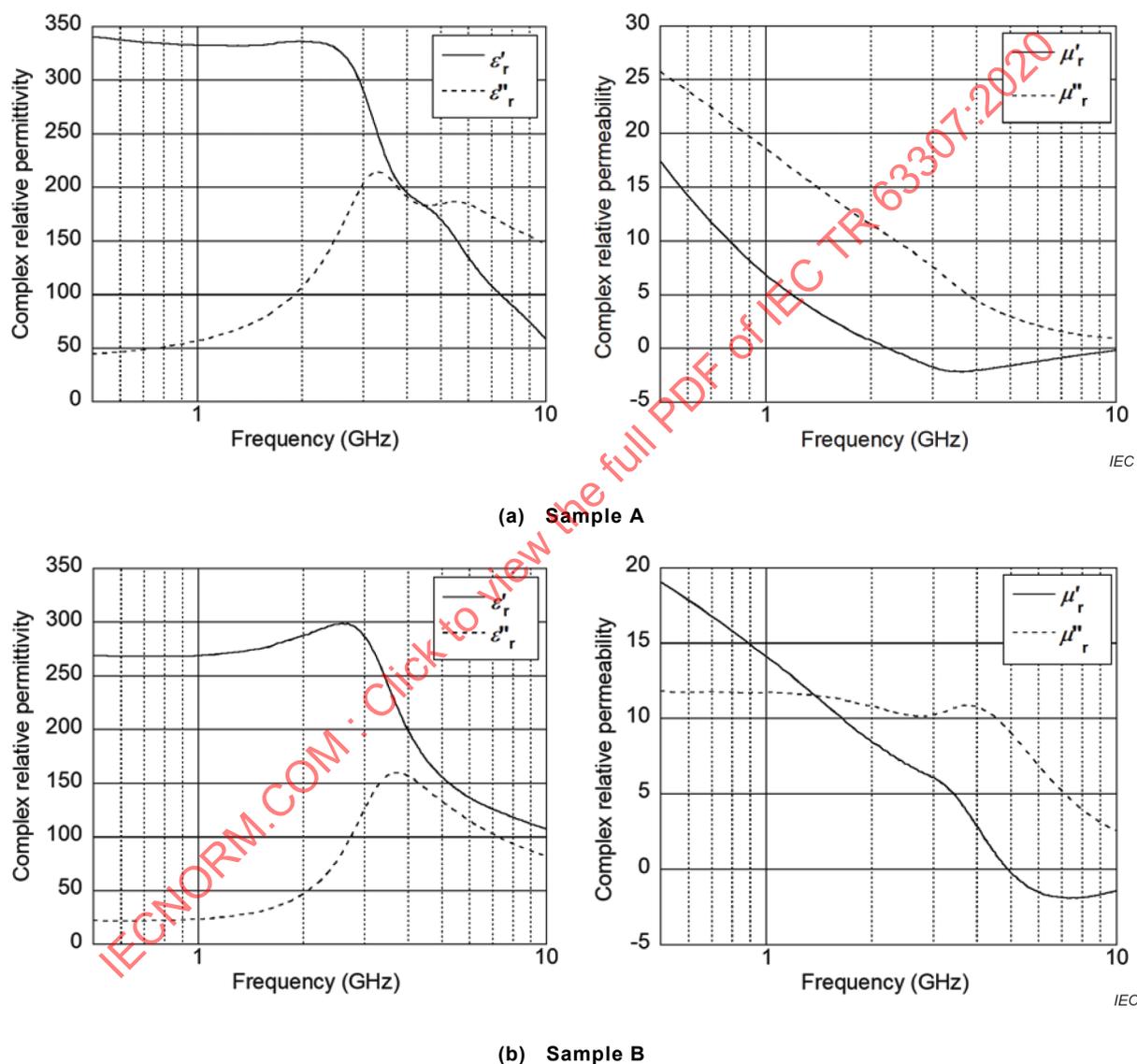


Figure 12 – Measurement results of noise suppression sheet

### 5.2.11 Remarks

Subclause 5.2 provides some helpful information on measuring the complex relative permittivity and permeability using the Nicolson Ross Weir method.

- 1) Coaxial transmission lines cover a broad frequency range, but a toroid-shaped sample is more difficult to manufacture. It shall be noted that complex relative permittivity is very much influenced by the air gap between a sample and test fixture.

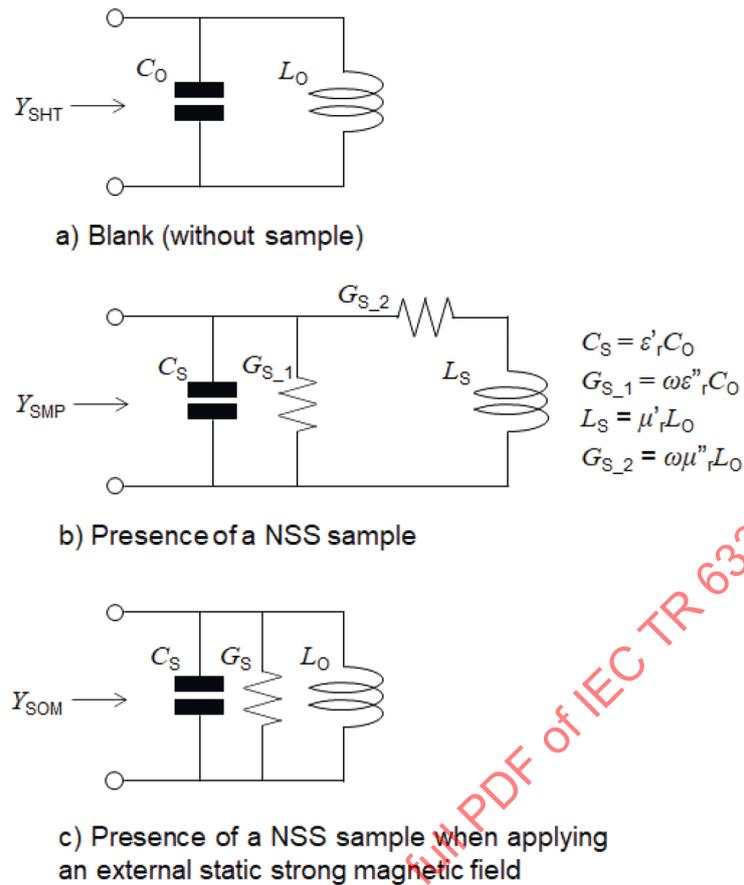
- 2) When measuring a sample with a thickness of more than half the wavelength using the Nicolson Ross Weir model, discontinuities can appear in the trace.
- 3) A guided jig made of low dielectric and loss tangent material such as styrene foam is effective to hold a sample inside the test fixture. When using the guided jig, measure a standard sample with known material constants such as polytetrafluoroethylene (PTFE) with the guided jig and confirm that the guided jig does not affect the measurement results.
- 4) It shall be noted that the complex relative permittivity of NSS can be affected by self-resonance of the sample or test fixture. Another size of sample or test fixture should be measured to confirm the effect of the self-resonance.

### 5.3 Short-circuited microstrip line method

#### 5.3.1 Principle

The measurement method evaluates the in-plane complex relative permeability of a rectangular shape sample of a noise suppression sheet (NSS) using a short circuit microstrip line (MSL) jig. The rectangular shaped NSS sample is placed at the MSL short-circuited end. In this measurement method, two  $S_{11}$  values of the MSL jig with sample are measured when an external static strong magnetic field is applied to the sample and when it is not applied to the sample, respectively; the permeability is then calculated. This method is denoted as a field method in this measurement.

The reference plane is denoted on the source side plane of the rectangular sample. The lumped element parallel LC equivalent circuits are assumed as shown in Figure 13. The  $S_{11}$  parameter is measured and analyzed to derive the permeability of the sample based on the lumped element approximation. Figure 13a) and Figure 13 b) are the equivalent circuits for the blank test fixture and for the sample loaded test fixture, respectively. Figure 13 c) shows the equivalent circuit for the test fixture with sample under the external static strong magnetic field when the (as-measured) complex relative permeability of the sample is assumed to be 1.  $Y$ ,  $C$ ,  $L$ , and  $G$  are the input admittance, capacitance, inductance, and conductance for the equivalent circuit in the MSL jig, respectively; the subscripts SHT, SMP, and SOM indicate the “short”, “sample” and “sample on magnet”; the subscripts “o” and “s” indicate the blank state (without sample) in the MSL jig and the presence of a sample in the MSL jig;  $\epsilon'_r$  and  $\epsilon''_r$  are the real and imaginary parts of complex relative permittivity;  $\mu'_r$  and  $\mu''_r$  are the real and imaginary parts of complex relative permeability; and  $\omega$  ( $= 2\pi f$ ) is the measurement frequency. The observed permeability of the sample essentially includes the demagnetization effect that originated in the rectangular shape of the sample. Consequently, the as-measured complex relative permeability should be corrected by the demagnetization factor  $N$  and coupling constant  $\eta$ . The details for the calculation are described in Annex B.



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Figure 13 – Equivalent circuits for the MSL

### 5.3.2 Measurement frequency and accuracy

The objective of this method is to evaluate NSS samples and is applicable for the measurements under the following conditions:

frequency:  $10 \text{ MHz} \leq f \leq 10 \text{ GHz}$

relative permeability:  $\mu'_r \leq 1\,000$ ,  $0 \leq \mu''_r \leq 1\,000$

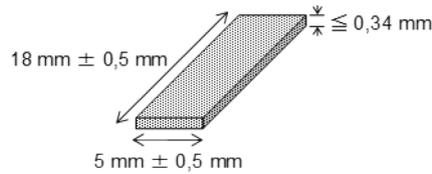
accuracy (repetitive): value error  $\pm 5 \%$

### 5.3.3 Measurement parameters

The in-plane complex relative permeability  $\mu'_r - j\mu''_r$  of the NSS sample is measured.

### 5.3.4 Test sample

A rectangular shape is prepared from the NSS sample as shown in Figure 14.



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Long axis:  $18 \text{ mm} \pm 0,5 \text{ mm}$   
 Short axis:  $5 \text{ mm} \pm 0,1 \text{ mm}$   
 Thickness:  $t \leq 0,34 \text{ mm}$

**Figure 14 – Rectangular shape of NSS sample**

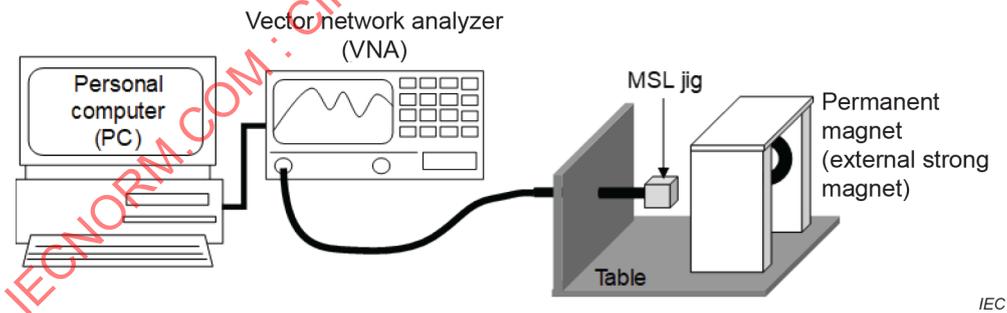
It is necessary that the rectangular shape sample be uniform (homogeneous) without cracks, cuts, and rupture surface irregularities. The accurate value of the permeability of the sample depends on its accurate thickness.

**5.3.5 Measurement environment**

The fixture and the samples shall be kept in a clean and dry state. The room temperature and the relative humidity shall preferably be  $23 \text{ °C} \pm 5 \text{ °C}$  and less than 60 %, respectively. It is desirable to secure a place where the temperature and the humidity are constant, or in a space where equipment (including the jig) and cables are deployed in a housing with constant temperature and humidity. Introduced variables such as temperature changes or jig detachment because of handling should be minimized.

**5.3.6 Measurement system**

The apparatus of the permeability measurement system is shown in Figure 15. The MSL jig is connected to a vector network analyzer (VNA) via a coaxial cable, and the VNA communicates through a personal computer (PC). The electric signal from the VNA is analyzed by the PC installed software for permeability. When the permeability of samples is measured, a permanent magnet is used.

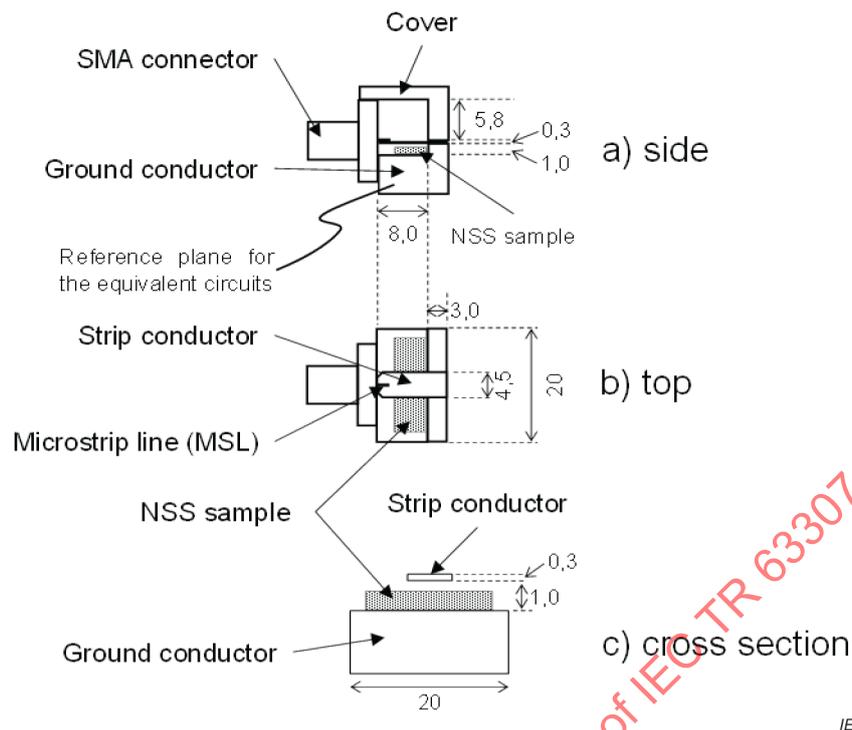


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**Figure 15 – Measurement system**

**5.3.7 Test fixture (MSL jig)**

Figure 16 shows a short-circuited test fixture (MSL jig) and sample installation. The MSL jig consists of a short-circuited microstrip line, and another end of the microstrip line is connected to the SMA connector. The rectangular shape sample is uniformly and tightly placed at the corner of the short end. When a gap between the ground conductor of the short-circuited end and the sample is too large, the correct result cannot be obtained. A table that supports the MSL jig and a permanent magnet are also prepared (see Figure 16).



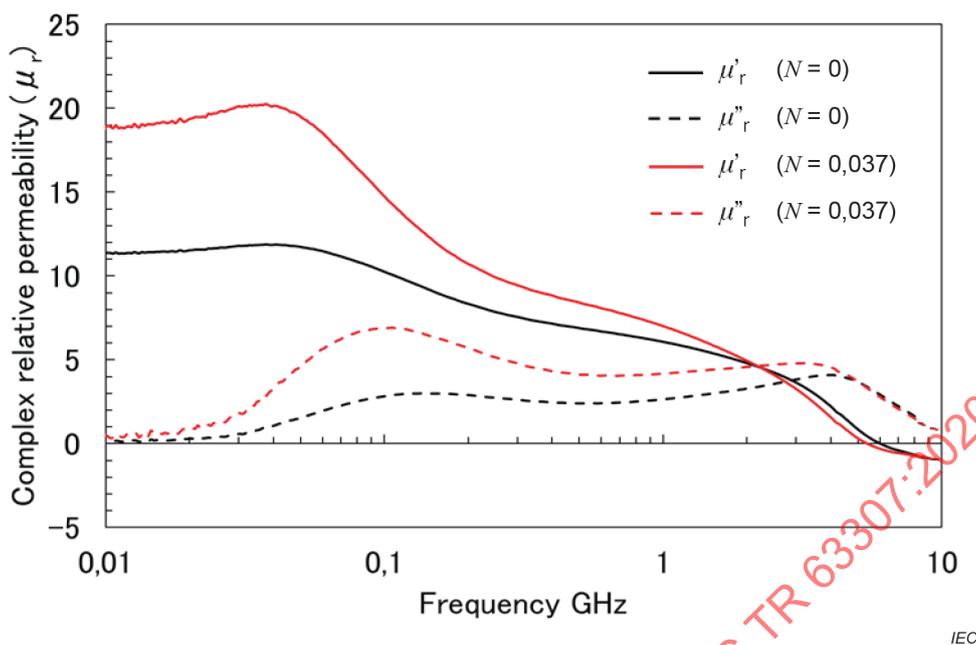
**Figure 16 – Short-circuited microstrip line test fixture (MSL jig)**

### 5.3.8 Measurement procedure

- 1) Set up the VNA, frequency range ( $10 \text{ MHz} \leq f \leq 10 \text{ GHz}$ ). For example: VNA set up parameters, measurement points: 401, IF bandwidth: 1 kHz, power:  $-17 \text{ dBm}$ , average: 5.
- 2) Set the measurement parameter of VNA to  $S_{11}$ .
- 3) Connect a coaxial cable and the VNA.
- 4) Calibrate the connected coaxial cable using calibration kits (open, short, and load).
- 5) Connect the coaxial cable end and the test fixture (MSL jig).
- 6) Measure  $S_{11}$  of the blank state of the MSL jig and store as  $S_{11\_SHT}$ .
- 7) Measure  $S_{11}$  of the NSS rectangular shape sample placed in the MSL jig by applying an external static strong magnetic field and store as  $S_{11\_SOM}$ .
- 8) Measure  $S_{11}$  of the NSS rectangular shape sample placed in the test fixture by removing the external static strong magnetic field and store as  $S_{11\_SMP}$ .

### 5.3.9 Results (example)

Figure 17 shows the measurement and corrected results of the complex relative permeability for a NSS sample C with 0,236 mm thickness. The measurement results are corrected by demagnetization factor  $N$  and coupling coefficient  $\eta$ .



**Figure 17 – Complex relative permeability of a NSS sample C with 0,236 mm thickness, as measured at  $N = 0$  (and  $\eta = 0,135 \text{ 2}$ ) and corrected by demagnetization factor  $N = 0,037$  (and  $\eta = 0,135 \text{ 2}$ )**

### 5.3.10 Remarks

- 1) This method belongs to the field method which compares  $S_{11}$  parameters with the strong static magnetic field and without it, with the result that the influence of permittivity on the permeability measurement is small.
- 2) The saturated magnetization of NSS samples depends on the magnetic metal materials in the NSS. The magnetic metal materials sometimes show ferromagnetic resonance without saturating magnetization at 5 000 Oe, with the result that the imaginary part ( $\mu''_r$ ) of the permeability becomes a negative value at around 10 GHz. In this case, to observe reasonable results, further strong magnetic field will be required to saturate the NSS sample.
- 3) The magnetization of the NSS (or magnetic) sample is necessary to saturate more than 90 % at the applied strong static magnetic field (approximately 5 000 Oe).

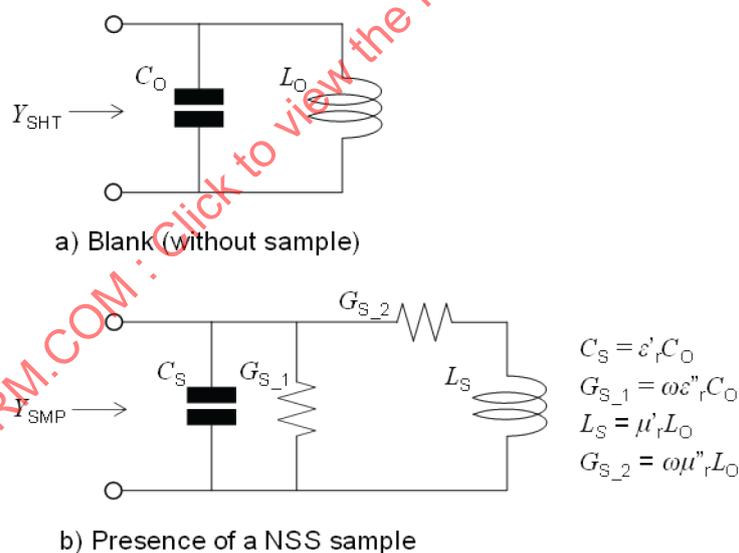
## 5.4 Short-circuited coaxial line method

### 5.4.1 Principle

The measurement method evaluates the in-plane complex relative permeability  $\mu_r$  of a NSS sample with a toroidal shape using a short circuit coaxial line (denoted coax) jig. In this method, the lumped element approximation is employed for the data analysis. This method is called a "remove" method, in which two  $S_{11}$  values corresponding to the blank (without sample) and to the NSS sample are compared. The demagnetization in toroidal shape samples is not considered (i.e., zero) because the sample with shape is endless and fully occupied for the magnetic material.

In general, the permittivity of the NSS sample affects the permeability of the sample. The influence of the permittivity on the permeability becomes pronounced when increasing the thickness of the sample. Experimentally in this method, when the sample thickness is 0,3 mm or less, the influence can be almost ignored. In contrast, when it is more than 0,3 mm, the permittivity shall be corrected by the permeability. The complex relative permittivity  $\varepsilon_r$  of the NSS sample can be measured by the open-circuited coaxial line as indicated in Annex C, and then the permeability can be corrected by the obtained permittivity. However, if the sample thickness exceeds the above acceptable value, the permeability cannot be corrected appropriately. This is because the lumped element approximation in this method cannot be described. To describe the lumped element approximation, the phase shift  $\beta t$  is calculated and required to be less than 0,8 rad, where  $\beta$  is the phase constant ( $= (2\pi(\varepsilon_r\mu_r)^{1/2}f)/c$ ),  $t$  is the sample thickness,  $f$  is the frequency, and  $c$  is the light speed in a vacuum. The  $\varepsilon_r$  is measured by the open-circuited coaxial line (see Annex C). That is, if the  $\beta t$  is less than 0,8 rad in the measurement frequency band, the permeability is appropriately corrected by the obtained permittivity.

The reference plane for the measurement is the source side plane of toroidal sample. The lumped element parallel LC equivalent circuit is assumed as shown in Figure 18. Figure 18a) and Figure 18b) are the equivalent circuits for the blank state (without sample) and the presence of the sample in the coax jig, respectively.  $Y$ ,  $C$ ,  $L$ , and  $G$  are the input admittance, capacitance, inductance, and conductance for the equivalent circuit in the coax jig; the subscripts SHT and SMP indicate the “short” and “sample”; subscripts “o” and “s” indicate the blank state and presence of sample in the coax jig;  $\varepsilon'_r$  and  $\varepsilon''_r$  are the real and imaginary parts of the complex relative permittivity;  $\mu'_r$  and  $\mu''_r$  are the real and imaginary parts of the complex relative permeability; and  $\omega$  ( $= 2\pi f$ ) is the measurement frequency. The details for the calculation are described in Annex C.



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**Figure 18 – Equivalent circuits for the coax jig**

#### 5.4.2 Measurement frequency and accuracy

The objective of this method is to evaluate NSS samples and is applicable for the measurements under the following conditions:

frequency:  $1 \text{ MHz} \leq f \leq 10 \text{ GHz}$

relative permeability:  $\mu'_r \leq 1\,000$ ,  $0 \leq \mu''_r \leq 1\,000$

accuracy (repetitive): value error  $\pm 5 \%$

The lowest frequency can be expanded with a thicker sample. If the permittivity effect is negligible with a thinner sample, the highest frequency could be expanded up to 18 GHz.

#### 5.4.3 Measurement parameters

The in-plane complex relative permeability  $\mu'_r - j\mu''_r$  of NSS samples is measured.

#### 5.4.4 Test sample

A toroidal shape prepared from a NSS sample is shown in Figure 19.

Inner diameter:  $3^{+0,05}_0$  mm

Outer diameter:  $7^0_{-0,05}$  mm

Thickness: To be determined to describe the lumped element approximation, depending on the maximum frequency (typically,  $t \leq 0,3$  mm).

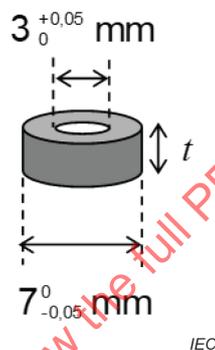


Figure 19 – Toroidal shape of NSS sample

#### 5.4.5 Measurement environments

The fixture and the samples shall be kept in a clean and dry state. The room temperature and the relative humidity shall preferably be  $23\text{ °C} \pm 5\text{ °C}$  and less than 60 %, respectively. The temperature slightly affects the measurement results. Especially, the effect is provably large below 1 GHz. Therefore, it is desirable to secure the place where the temperature and the humidity are constant, or the space where equipment (including the jig) and cables are deployed in a housing with constant temperature and humidity. Introduced variables such as temperature changes or jig detachment because of handling should be minimized.

#### 5.4.6 Measurement system

The apparatus of the permeability measurement system is shown in Figure 20. The coax jig is connected to a vector network analyzer (VNA) via a coaxial cable, and the VNA communicates through a personal computer (PC). The electric signal from the VNA is analyzed by software on the PC to determine permeability.

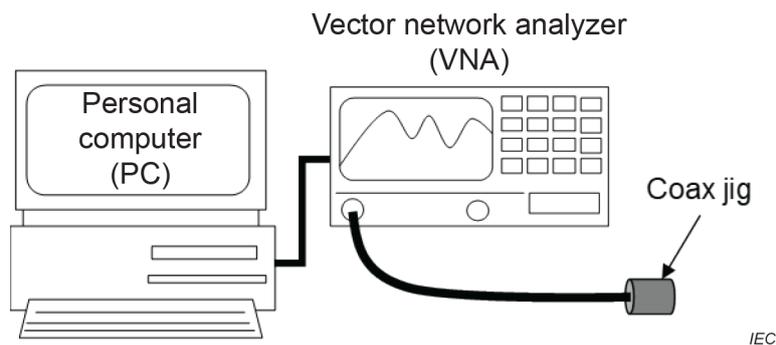


Figure 20 – Measurement system

#### 5.4.7 Test fixture (coax jig)

Figure 21 shows the cross-sectional diagram of the practical test fixture coax jig in detail. The coax jig is connected to an APC-7 adapter and then the other side of the APC-7 adapter is connected to the SMA connector. The toroidal shape sample having the same diameter dimensions as APC-7 is tightly inserted at the end of the short-circuited coaxial line. Measure  $S_{11\_SHT}$  and  $S_{11\_SMP}$  corresponding to the blank and to the loaded test fixture, respectively.

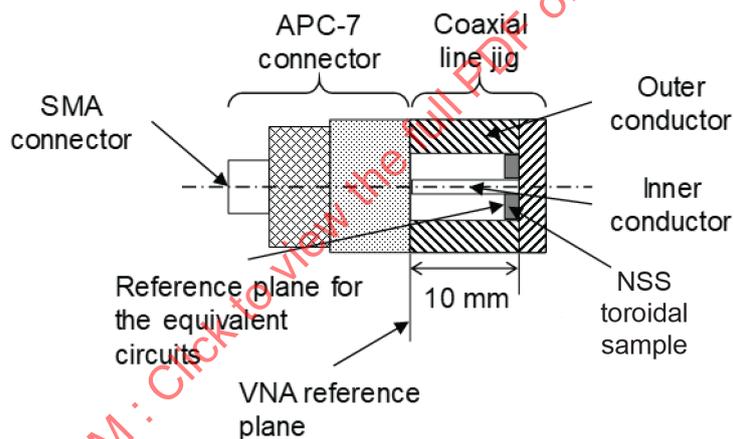


Figure 21 – Short-circuited coaxial line test fixture (coax jig)

#### 5.4.8 Measurement procedure

- 1) Set up the VNA, frequency range ( $1 \text{ MHz} \leq f \leq 10 \text{ GHz}$ ). For example, VNA set up parameters, measurement points: 401, IF bandwidth: 1 kHz, power:  $-17 \text{ dBm}$ , average: 5.
- 2) Set the measurement parameter of VNA to  $S_{11}$ .
- 3) Connect a coaxial cable and VNA.
- 4) Calibrate the connected coaxial cable including APC-7 using calibration kits (open, short, and load).
- 5) Connect the coaxial cable end (APC-7) and the test fixture (coax jig).
- 6) Measure  $S_{11}$  of the blank state of the coax jig and store as  $S_{11\_SHT}$ .
- 7) Measure  $S_{11}$  of the NSS toroidal shape sample placed in the coax jig and store as  $S_{11\_SMP}$ .

### 5.4.9 Results (example)

Figure 22 and Figure 23 show the measurement corrected results of the complex relative permeability for NSS sample A with 0,29 mm thickness and sample B with 0,25 mm thickness. The measurement results (as measured  $\mu'_r$  and  $\mu''_r$ ) are corrected by the permittivity. The corrected results are almost the same as the measured results. In these samples with thickness, the permittivity almost does not affect the complex permeability. In the low frequency region between 0,001 GHz and 0,005 GHz, the measurement spectra ( $\mu'_r$  and  $\mu''_r$ ) are distorted and/or noisy. The distortion degree depends on the sample and the size precision (dimension accuracy) of the toroidal shape (see 5.4.4). However, this region approaches the measurement limit for this method using the coax jig.

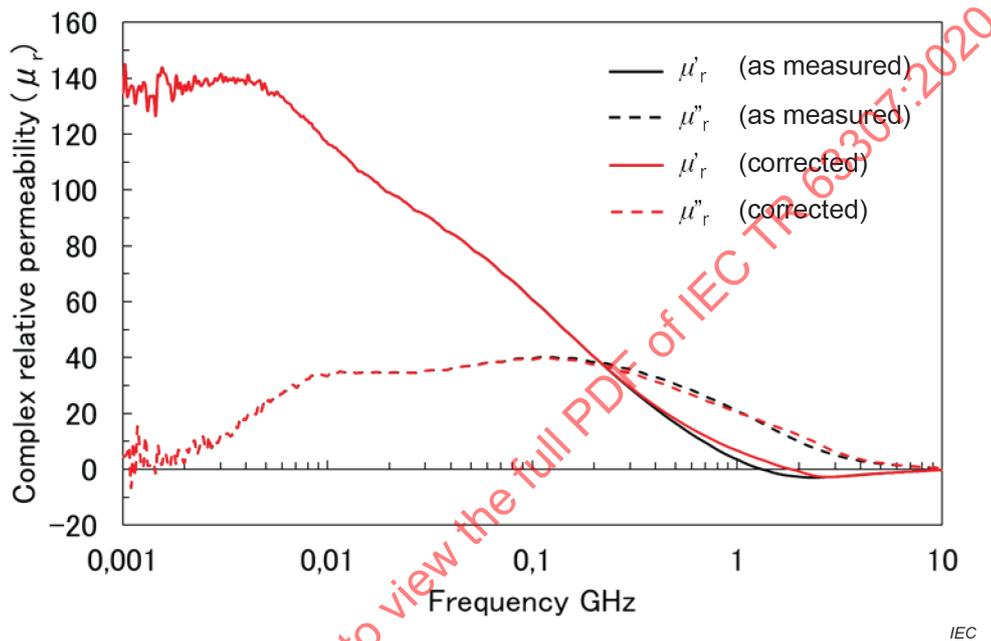
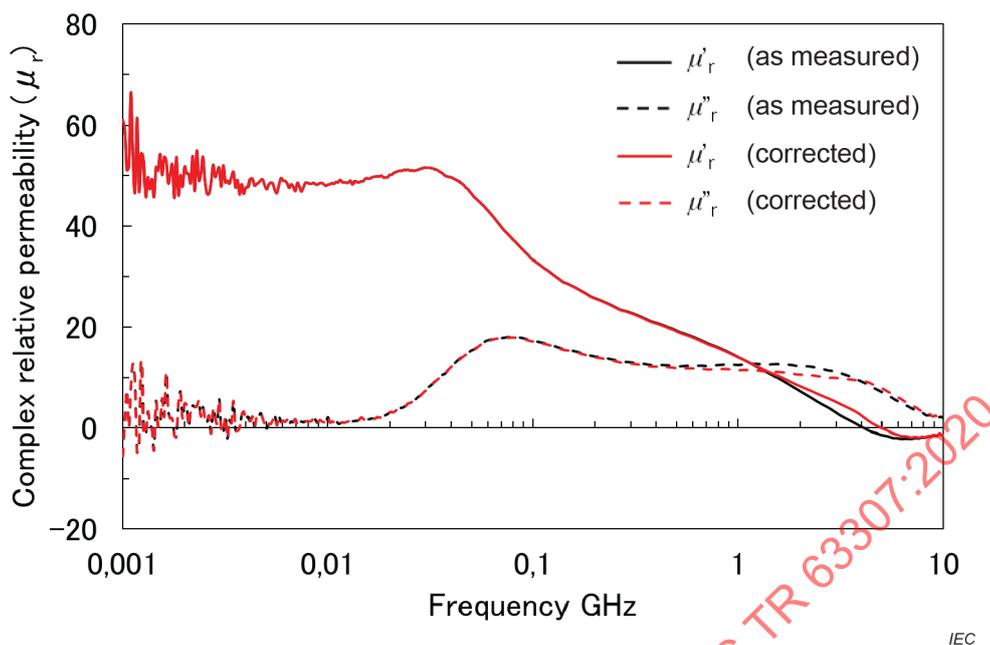


Figure 22 – Complex relative permeability of a NSS sample A with 0,29 mm thickness, as measured and corrected by the permittivity



**Figure 23 – Complex relative permeability of a NSS sample B with 0,25 mm thickness, as measured and corrected by the effective permittivity**

#### 5.4.10 Remarks

The complex relative permeability of samples is measured. As mentioned before, the measurement spectra are distorted and/or noisy in the low frequency region. This distortion degree depends on the sample and the size precision of the toroidal shape. This suggests the measurement limit for this method. The influence of the permittivity on the permeability for the sample is also investigated (see Annex C). In fact, when a sample with a thickness  $\leq 0,3$  mm is measured, the effect is very small at the measurement frequency region less than 1 GHz. A slight effect is seen around 1 GHz or more. This effect is smaller for thinner NSS samples. An experimental confirmation is necessary for the upper limit thickness of NSS below which the permittivity does not affect the permeability.

### 5.5 Shielded loop coil method

#### 5.5.1 Measurement principle

##### 5.5.1.1 General description

The shielded loop coil is a one-turn coil that will enclose the NSS in the coil window and pick up flux voltage as a signal from the NSS driven by an external AC magnetic field  $H_{AC}$ . The source of the AC magnetic field is a Transverse Electromagnetic (TEM) cell that encloses the shielded loop and the NSS near the surface of the ground conductor. By applying an RF signal to the TEM cell, the AC magnetic field  $H_{AC}$  is generated to the right angle of the strip conductor. The magnetic relative permeability is derived from the change in the transmission parameter  $S_{21}$  from the TEM cell to the shielded loop in the state where the ferromagnetic nature of the NSS is killed by applying a strong DC magnetic field, and in the state where no DC magnetic field is applied.

##### 5.5.1.2 Shielded loop coil

Figure 24 shows the structure of the shielded loop coil. The shielded loop coil consists of three metal layers that allow protection of unnecessary voltage injection from the stray AC electric field component  $E_{AC}$  around the coil. Accordingly the shielded loop coil is sensitive only to the magnetic component out of the electromagnetic signal.

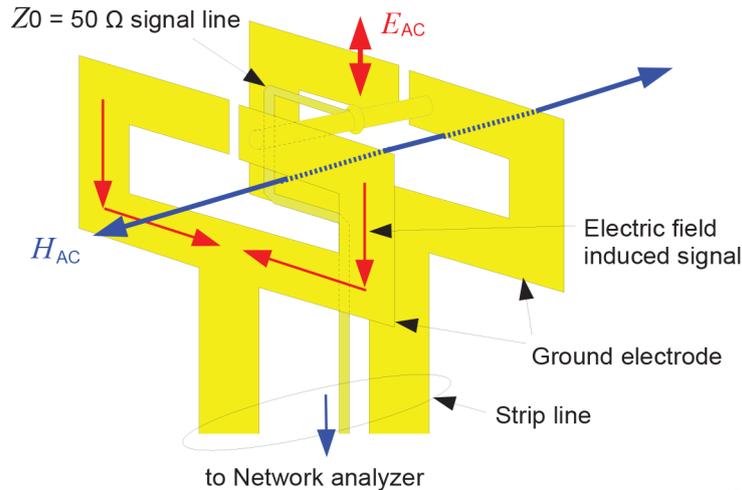


Figure 24 – Structure of shielded loop coil

Figure 25a) explains the shielded loop coil and NSS sample arrangement. The NSS is subjected to a uniform AC magnetic field  $H_{AC}$  in the direction parallel to the NSS sample surface and perpendicularly to the coil plane. Accordingly the shielded loop coil will measure complex relative permeability along the in-plane direction of the NSS.

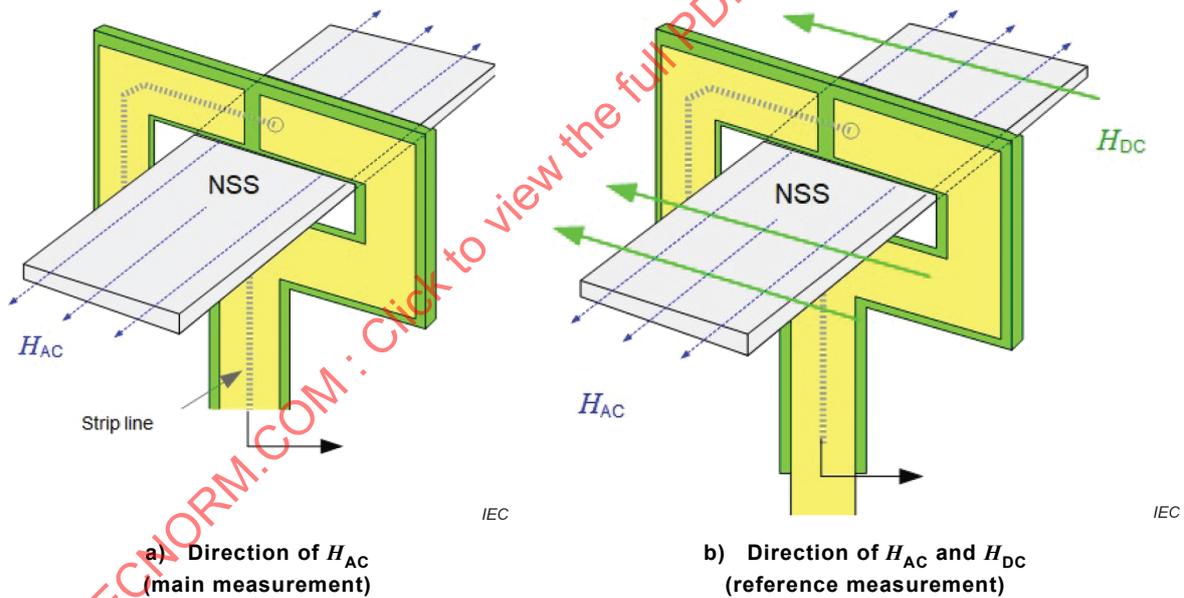


Figure 25 – Shielded loop coil and NSS sample arrangement

### 5.5.1.3 AC and DC magnetic field application

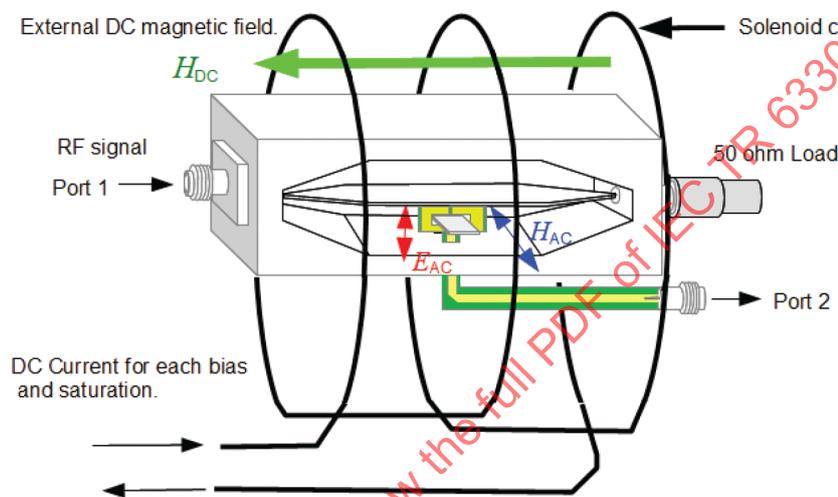
Figure 26 shows the whole structure of the measuring unit of the equipment. The shielded loop coil and NSS sample are placed near the surface of the ground conductor of an RF cavity having an open TEM cell structure on the side. A terminal of the TEM cell is connected to Port 1 of a vector network analyzer that generates the RF signal. The other terminal of the TEM cell is connected to a 50 Ω load resistor.

Accordingly a traveling electromagnetic field is generated in the RF cavity, and the magnetic component  $H_{AC}$  of the field is used to measure the complex relative permeability. The electric component  $E_{AC}$  of the field will not disturb the relative permeability measurement thanks to the physical nature of the shielded loop coil to suppress electric-field induced voltage, as illustrated

in Figure 24. The TEM cell is matched to the characteristic impedance of  $Z_0 = 50 \Omega$  and applies a uniform magnetic field to the NSS over the entire measurement frequency range. The reflection signal  $S_{11}$  from the TEM cell is negligible because the TEM cell is matched to  $Z_0 = 50 \Omega$ .

For calibration purposes, the DC magnetic field  $H_{DC}$  is applied to the in-plane direction at the right angle to the AC magnetic field  $H_{AC}$ , as illustrated in Figure 25b). A DC magnetic field generator (e.g. solenoid coil) applies the DC magnetic field  $H_{DC}$  from outside the TEM cell, as shown in Figure 26.

Note that the relative directions of  $H_{AC}$ ,  $H_{DC}$  and  $E_{AC}$  are the same throughout Figure 24 to Figure 26, with respect to the shielded loop coil and NSS sample directions.



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**Figure 26 – Whole structure of the measuring unit of the equipment**

#### 5.5.1.4 Theory of complex relative permeability measurement

##### 5.5.1.4.1 General

The complex relative permeability  $\mu_r = \mu'_r - \mu''_r$  can be obtained in principle from the frequency dependent transmission coefficient  $S_{21}$  of the S-parameter as it corresponds to the time rate of the magnetic flux linkage through the window of the shielded loop coil (flux voltage). The magnetic flux consists of air core flux and ferromagnetic flux. Two types of measurement are performed in order to separate the two kinds of fluxes.

##### 5.5.1.4.2 Reference measurement

Transmission coefficient  $S_{21S}$  is measured under the application of the frequency dependent AC magnetic field  $H_{AC}$  where the NSS is saturated with a strong external DC magnetic field  $H_{DC} = H_{sat}$ . This measurement extracts the signal from the air core flux and the stray signal from the dielectric and resistive materials associated with the measurement unit. Reflection coefficient  $S_{22S}$  of the shielded loop coil is also measured to calibrate the impedance of the coil with the NSS sample having a non-magnetic nature.

##### 5.5.1.4.3 Main measurement

Transmission coefficient  $S_{21N}$  is measured under the application of the frequency dependent AC magnetic field  $H_{AC}$  where  $H_{DC} = 0$ . This measurement extracts the ferromagnetic signal of

interest and all signals given by the reference measurement. Therefore the difference between the main and reference measurements corresponds to the ferromagnetic signal of interest. Reflection coefficient  $S_{22N}$  of the shielded loop coil is also measured to calibrate the impedance of the coil with the NSS sample having a ferromagnetic nature.

Accordingly, the complex relative permeability,  $\mu_r = \mu'_r - \mu''_r$  is given by the Formula (31).

$$\mu_r = \frac{S_c}{S_m} \left[ \frac{S_{21N}}{S_{21S}} \frac{1 - S_{22S}}{1 - S_{22N}} - 1 \right] + 1 \quad (31)$$

where

- $S_m$  is the cross-sectional area of the NSS sample placed at the centre of the shielded loop coil;
- $S_c$  is the cross-sectional area of the effective aperture window of shielded loop coil;
- $S_{21S}$  is the transmission coefficient  $S_{21}$  measured when the NSS sample is saturated by an external DC magnetic field  $H_{DC} = H_{sat}$  (for example, using a solenoid coil);
- $S_{21N}$  is the transmission coefficient  $S_{21}$  measured when the external DC magnetic field is removed ( $H_{DC} = 0$ ) and the NSS sample is unsaturated;
- $S_{22S}$  is the reflection coefficient  $S_{22}$  measured when the NSS sample is saturated by a strong external DC magnetic field  $H_{DC} = H_{sat}$  (for example, using a solenoid coil);
- $S_{22N}$  is the reflection coefficient  $S_{22}$  measured when the external DC magnetic field is removed ( $H_{DC} = 0$ ) and the NSS sample is unsaturated.

#### 5.5.1.4.4 RF calibration

Accuracy of measurement can be improved by taking account of the self-resonance nature of the shielded loop coil especially when the frequency approaches the self-resonance frequency of the shielded loop coil. Measure the impedance of the shielded loop coil without NSS to obtain inductance  $L_0$ , capacitance  $C_0$  and self-resonance angular frequency  $\omega_0$ . The relation  $\omega_0^2 = 1 / L_0 C_0$  stands. Then the complex relative permeability is calculated using Formula (32).

$$\mu_r = \frac{S_c}{S_m} \left[ \frac{S_{21N}}{S_{21S}} \frac{1 - S_{22S} - S_{21S}}{1 - S_{22N} - S_{21N}} \frac{1}{1 + \left[ \frac{1 - S_{22S} - S_{21S}}{1 - S_{22N} - S_{21N}} - 1 \right] \frac{\omega^2}{\omega_0^2}} - 1 \right] + 1 \quad (32)$$

where,

- $\omega$  is the angular frequency  $\omega = 2\pi f$ ;
- $\omega_0$  is the self-resonance angular frequency of shielded loop coil:  $\omega_0^2 = 1 / L_0 C_0$ ;
- $L_0$  is the inductance of the shielded loop coil;
- $C_0$  is the capacitance of the shielded loop coil.

#### 5.5.1.4.5 Magnetic calibration (absolute value calibration)

Following the RF calibration in 5.5.1.4.4, 5.5.1.4.5 describes the magnetic calibration (absolute value calibration) of the complex relative permeability of the NSS sample. This calibration allows magnetic leakage flux compensation that returns outside the NSS but inside the shielded loop

coil window. A frequency-independent scalar calibration constant is derived and used in the calibration procedure.

Figure 27 shows the DC magnetization curve of a NSS sample. Magnetization  $M$  is saturated to the saturation magnetic moment  $M_s$  when the DC magnetic field  $H_{DC}$  becomes more than the anisotropy field  $H_k$ . There is a known ferromagnetic theory applicable to the magnetic saturation range ( $H_{DC} \gg H_k$ ).

$$M_s = (H_k + H_{DC}) \mu_0 \mu_r \quad (33)$$

Based on Formula (33), the absolute value of the complex relative permeability can be calibrated by the following procedure.

- 1) Measure relative permeability using Formula (32) with DC magnetic field  $H_{bias_i}$  ( $i = 1, 2, 3, \dots$ ,  $H_{DC} = H_{bias_i} \ll H_{sat}$ ), instead of  $H_{DC} = 0$ .  $H_{bias_i}$  is usually set several times the  $H_k$ . Thus obtained, the relative real and imaginary part relative permeability are called  $\mu'_{rob}$  and  $\mu''_{rob}$ , respectively, in 5.5.1.4.5.
- 2) Calculate the product of the real part of complex relative permeability  $\mu'_{rob}$  and  $(H_{bias_i} + H_k)$ , namely  $(H_{bias_i} + H_k) \cdot \mu'_{rob}$ . This product should be equal to the saturated magnetization  $M_s$  as the  $H_{bias_i}$  strengthens because of Formula (33). However, the product will be less than the  $M_s$  however strong the  $H_{bias_i}$  can be, because of the leakage flux that returns outside the NSS but inside the shielded loop coil window.
- 3) Draw the  $M_s$  versus the  $1/(H_{bias_i} + H_k)$  plot as shown in Figure 28.
- 4) Extrapolate the plot to cross the vertical axis to find  $M'_s$  as the estimate of the saturated magnetization when an infinitely high  $H_{bias}$  is applied.
- 5) Find the calibration coefficient  $M_s / M'_s$ . The calibrated complex relative permeability is obtained by multiplying this calibration coefficient  $M_s / M'_s$  to the real part  $\mu'_{rob}$  and imaginary part  $\mu''_{rob}$  of the complex relative permeability.

$$\mu_r = (M_s / M'_s) \cdot (\mu'_{rob} - j\mu''_{rob}) \quad (34)$$

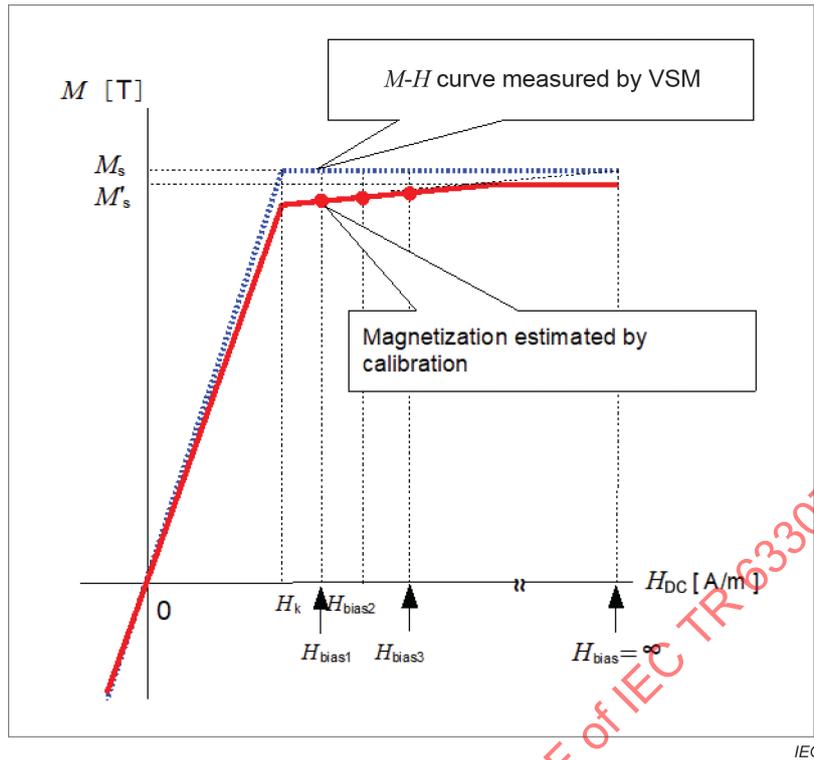


Figure 27 – DC magnetization curve

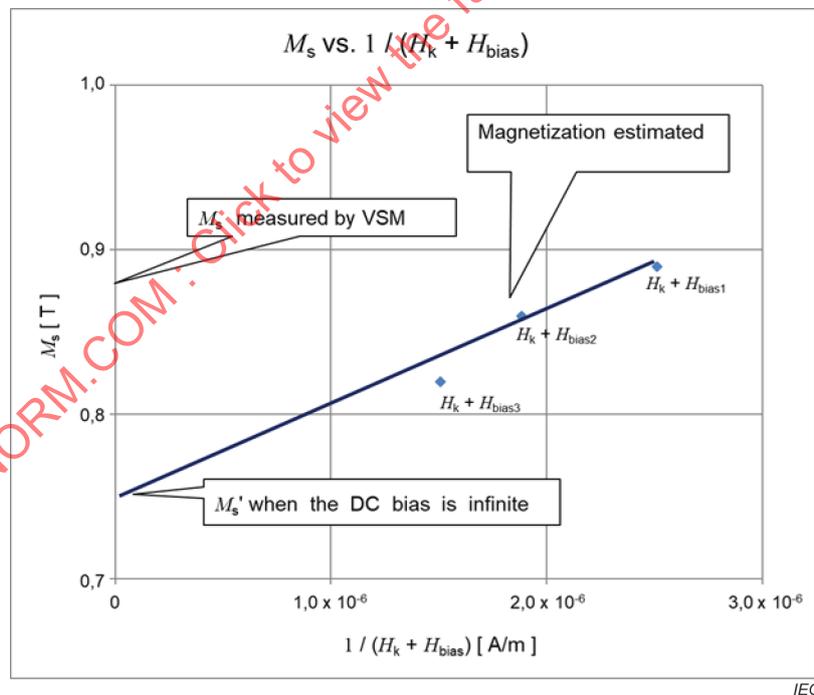


Figure 28 – Estimation of absolute value correction coefficient  $M'_s$

### 5.5.2 Measurement frequency and accuracy

This method is useful to evaluate the relative permeability of a thin-film and sheet-like magnetic material. The measurement frequency range is as follows. Highly accurate data can be obtained along the hard axis of magnetization if a NSS sample has magnetic anisotropy in the plane.

Frequency range:  $1 \text{ MHz} \leq f \leq 10 \text{ GHz}$

Accuracy: value error  $\pm 5\%$

### 5.5.3 Measurement parameters

$$\mu'_r, \mu''_r \text{ and } \mu_r$$

where:

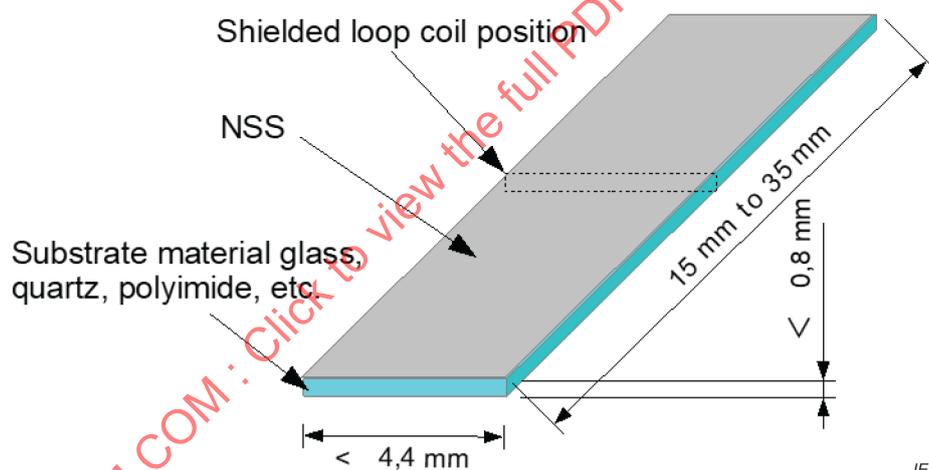
$$\mu_r = \mu'_r - \mu''_r$$

### 5.5.4 NSS sample dimension and recommendation

Figure 29 explains the NSS sample dimension. The NSS sample should be sized to be inserted into the window of the shielded loop coil. The NSS sample can be attached to glass, quartz, or polyimide substrate. Avoid conductive material as the substrate.

Since the cross-sectional area of the NSS sample  $S_m$  (width x thickness, excluding the substrate) is used for Formula (31) and (32), it is necessary to measure the NSS sample width and thickness within an error of 5/100 mm or less in order to maintain measurement accuracy.

The NSS sample is for  $H_k < 7\,958$  [A/m].



Measurement direction:	In-plane direction only. Both isotropic and anisotropic materials can be measured. Perpendicular direction to the sample surface (thickness direction) is not recommended.
NSS sample width:	4,4 mm or less.
NSS sample thickness:	0,8 mm or the less including substrate thickness (to be inserted in the measurement window).
NSS sample length:	4,0 mm or more (15 mm to 35 mm is recommended).

**Figure 29 – Recommended shape of NSS sample**



- 3) Insert the NSS sample in the measurement unit as shown in Figure 30 by the arrow Step1.
- 4) Slide the solenoid coil in the Step2 direction until the end to cover the measurement unit.
- 5) Start a relative permeability measurement using the application software on the PC.
- 6) Perform a set of reference and main measurements. Note that the only difference between the two measurements is the presence/absence of the external DC magnetic field  $H_{DC}$ . Completion of this step gives complex relative permeability without magnetic calibration (absolute value calibration) based on Formula (32).
- 7) Apply magnetic calibration (absolute value calibration) as described in the steps 1) to 5) in 5.5.1.4.5. Completion of this step gives complex relative permeability with magnetic calibration (absolute value calibration) based on Formula (34).

### 5.5.7.2 Example of detailed absolute value calibration procedure

- 1) Make sure that  $M_s$  and  $H_k$  of the NSS sample are measured before the relative permeability measurement using a VSM or similar equipment.
- 2) Set several DC external magnetic field intensities  $H_{bias_i}$  of the user's choice in the range of  $H_k < H_{bias_i} \ll H_{sat}$ .

- 3) Measure the complex relative permeability by applying the same procedure as the main measurement.

In Figure 27, three bias points ( $i = 1, 2, 3$ ) are selected, and the corresponding DC external magnetic fields  $H_{dc} = H_{bias_1}$ ,  $H_{bias_2}$  and  $H_{bias_3}$  are applied to the NSS sample to measure relative permeability  $\mu'_{r1}$ ,  $\mu'_{r2}$  and  $\mu'_{r3}$ , respectively.

- 4) Calculate the estimate of saturated magnetization  $M'_{si}$  at each bias point ( $i = 1, 2, 3$ ), using Formula (33). Formula (35) is the same as Formula (33) in principle with a popular SI unit conversion.

$$M'_{si} = (H_k + H_{bias_i}) \cdot \mu'_{ri} / 10\,000 \text{ [T]} \quad (i = 1, 2, 3) \quad (35)$$

- 5) Plot each  $M'_{si}$  on the graph whose horizontal axis is  $1 / (H_k + H_{bias_i})$  and vertical axis is  $M'_{si}$  [T] (Figure 25). Let  $M'_s$  be the estimate of saturated magnetization which can be found by extrapolating the plot to the point where  $1 / (H_k + H_{bias_i}) = 0$ . If the plots do not align on a straight line, use the least squares method to estimate the zero point.
- 6) Find the calibration coefficient as  $M_s / M'_s$ . The calibrated complex relative permeability is obtained by multiplying this calibration coefficient  $M_s / M'_s$  to the real part  $\mu'_{rob}$  and imaginary part  $\mu''_{rob}$  of the complex relative permeability, as shown in Formula (34).

### 5.5.8 Measurement results

Figure 31 to Figure 35 show the measured results of the complex relative permeability. Table 2 lists the sample details. Sample A-01 was measured in a range from 1 MHz to 13,5 GHz. The sample sizes are 4 mm × 4 mm and 4 mm × 35 mm, respectively.

$$\mu'_{r'}, \mu''_{r'}, \text{ and } \mu_r$$

NOTE The legends in each figure give the meaning of each line color.

The different relative permeability profiles of the two samples of a same material and the different sizes of 4 mm × 4 mm and 4 mm × 35 mm provide a comparison of the influence of the demagnetizing field due to the sample shape.

The maximum of the real part of the complex relative permeability of the 4 mm × 4 mm sample is 44. It is 112 for the 4 mm × 35 mm sample.

Figure 32 shows the real part of the complex relative permeability of the noise suppression sheet Sample B-01 measured at 1 MHz to 13,5 GHz. The sample size was 4 mm × 4 mm and 4 mm × 35 mm, respectively.

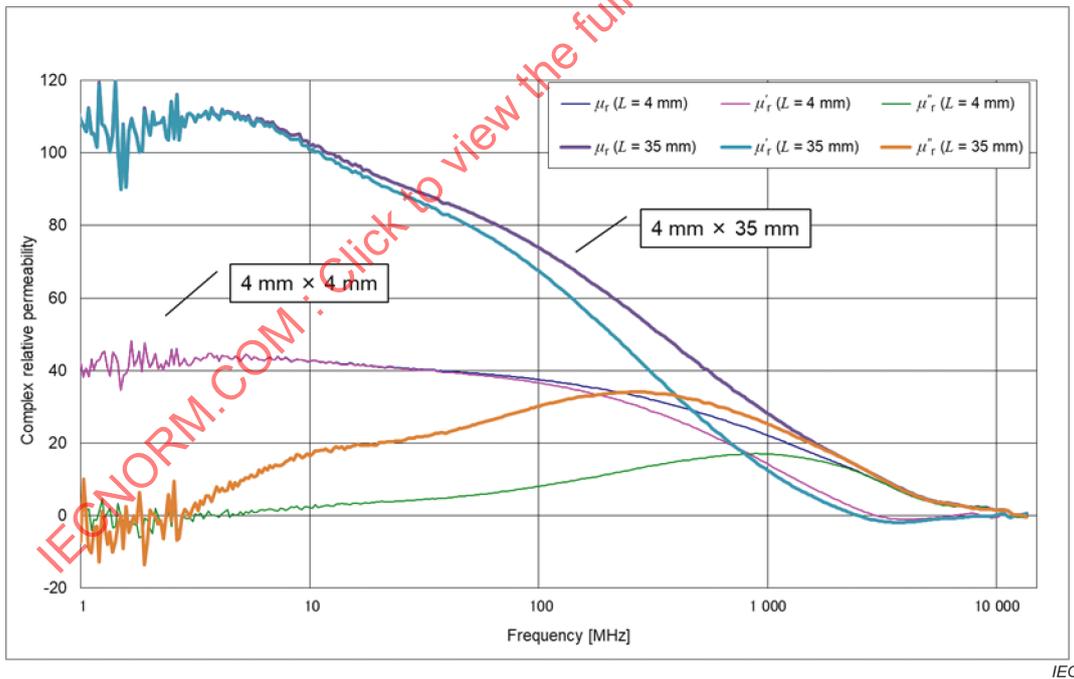
The maximum of the real part of the complex relative permeability of the 4 mm × 4 mm sample is about 25 and the relative permeability of the 4 mm × 35 mm sample is 54.

As with Sample A, two samples of a same material and different sizes are compared to see the influence of the demagnetizing field.

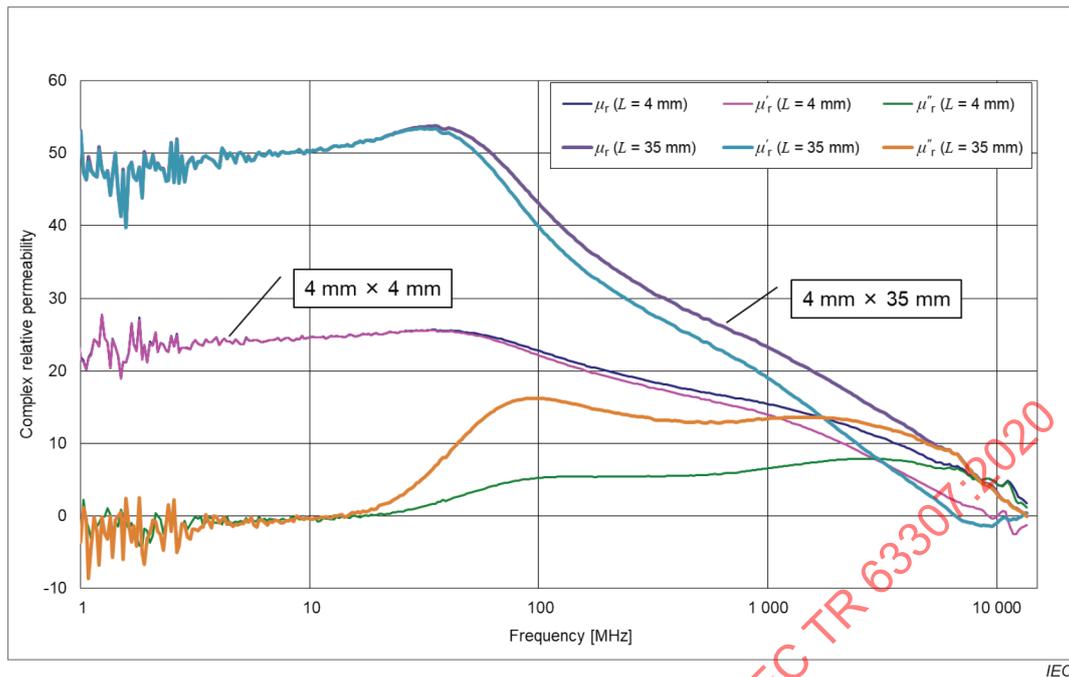
Figure 33 shows the DC bias magnetic field dependence of the complex relative permeability of the noise suppression sheet Sample A-02 measured between 1 MHz to 13,5 GHz. The sample size is 4 mm × 15 mm.

**Table 2 – Measurement sample table**

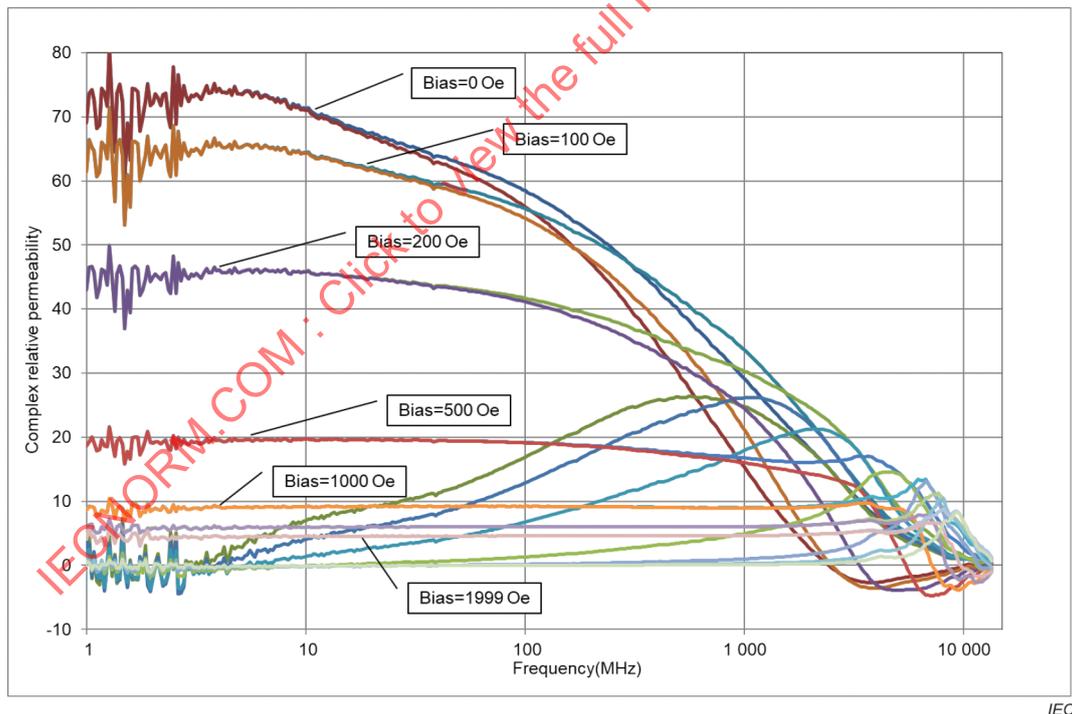
Sample name	Sample size	Thickness	Figure no.
Sample A-01	4 mm × 4 mm	100 μm	Figure 31
Sample A-01	4 mm × 35 mm	100 μm	Figure 31/Figure 34
Sample A-02	4 mm × 15 mm	200 μm	Figure 33
Sample B-01	4 mm × 4 mm	100 μm	Figure 32
Sample B-01	4 mm × 35 mm	100 μm	Figure 32/Figure 35



**Figure 31 – Measured complex relative permeability as a function of the size of a NSS sheet (Sample A-01)**



**Figure 32 – Measured complex relative permeability as a function of the size of a NSS sheet (Sample B-01)**



**Figure 33 – Measured complex relative permeability of a NSS sheet as a function of DC bias field intensity (Sample A-02)**

Figure 34 and Figure 35 show the calibrated complex relative permeability of two types of the Samples A-01 and B-01 obtained by applying the bias magnetic field as described in 5.5.1.4.5.

The noise on the low frequency side increases due to the sensitivity of the coil.

This system can also filter low frequency noise for removal.

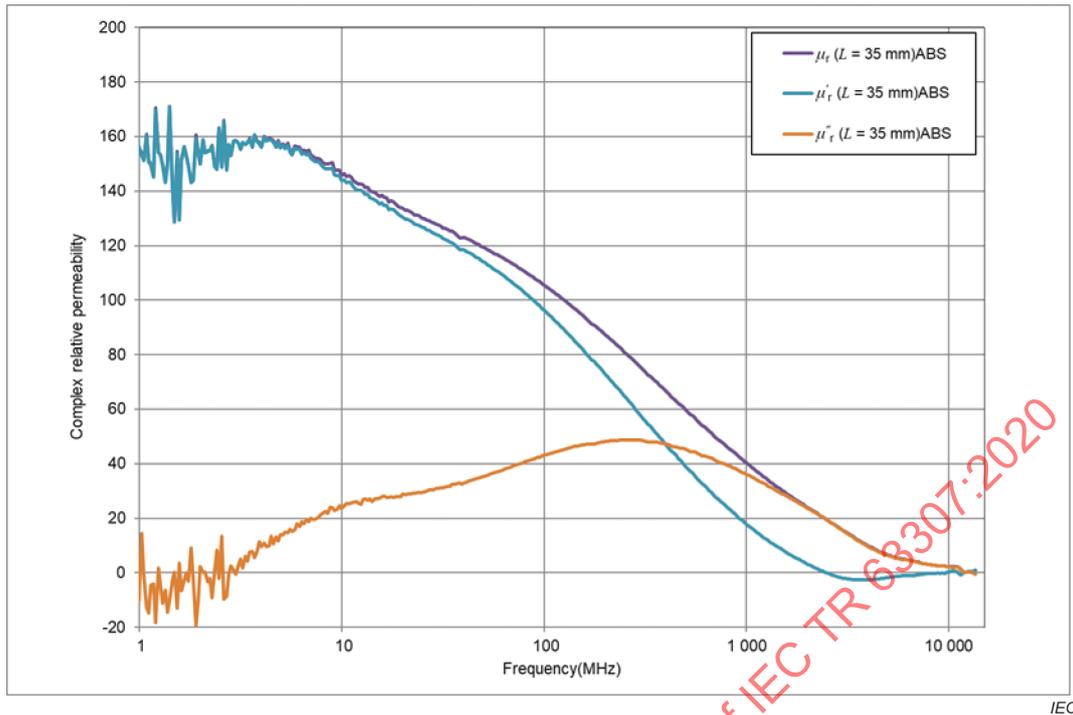


Figure 34 – Measured complex relative permeability after absolute value calibration (Sample A-01)

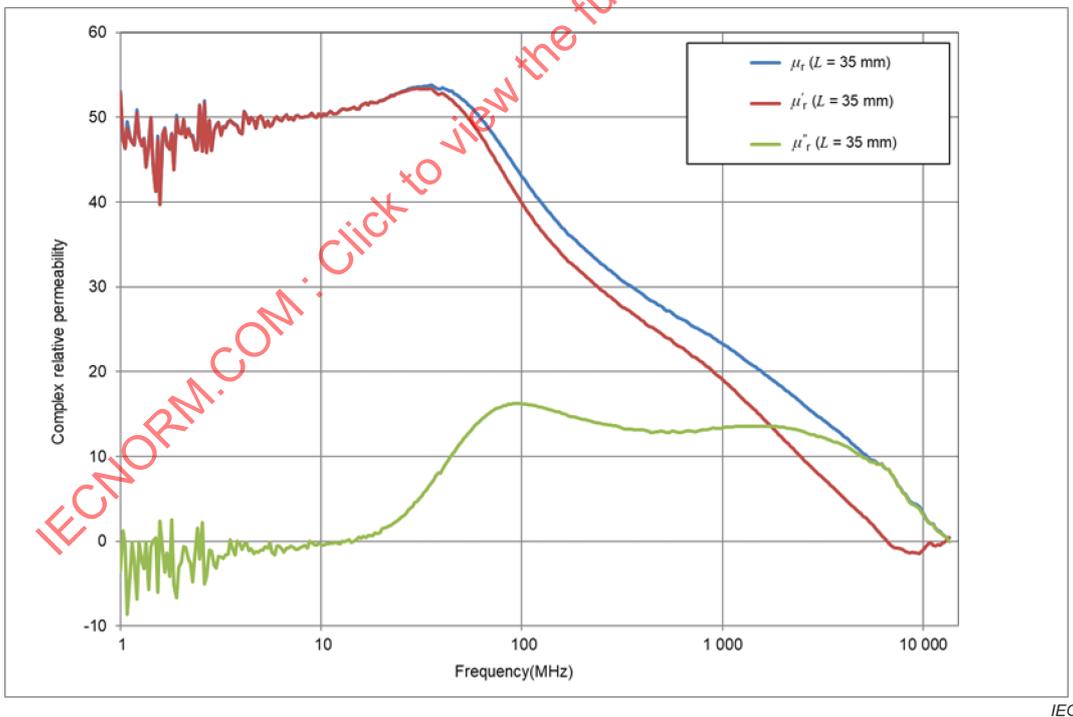


Figure 35 – Measured complex relative permeability after absolute value calibration (Sample B-01)

### 5.5.9 Summary

The shielded loop coil method has a degree of freedom in the shape of a sample since it measures a specimen of any size that can be enclosed in the window aperture at the centre of the coil.

The relative permeability of a sample can be sensitive to the direction of applied bias and RF magnetic fields because of the anisotropic nature of magnetization. Accordingly there is also a direction in which highly accurate measurement can be made, depending on the direction of applied magnetic fields.

It is a useful nature of this method that the relative permeability corresponding to the actual size of the magnetic materials in devices is obtained because the shape-dependent demagnetizing field is counted in the measurements. If a user needs relative permeability inherent in the material, a sample long enough along the measurement direction is used.

In order to calibrate measurement errors caused by leakage magnetic flux from a sample, absolute value calibration is performed in this measurement.

Sample A-02 should suppress electromagnetic noise most at the frequency around 300 MHz where  $\mu''_r$  in Figure 31 has the maximum value.

Sample B-01 in Figure 35 should have good noise suppression effect between 50 MHz and 5 GHz where  $\mu''_r$  is high.

## 5.6 Harmonic resonance cavity perturbation method

### 5.6.1 Theory

An exchange between magnetic and electric energies occurs after an electromagnetic stimulus is given from a small aperture to a metal closed cavity. This is called the natural resonance, and the resonance will be decreased by the cavity wall's energy loss. If the stimulus is applied with the same interval as the energy exchange, the energy in the cavity increases until the energy loss in the cavity becomes the same as the external energy supplied. This is called electromagnetic resonance. The electric field strength in the cavity is null where the magnetic field strength is the maximum and vice versa. A material installed in the magnetic field maximum part shifts the resonance characteristics in proportion to the magnetic characteristics. A small sample in the cavity gives a fractional change in the resonance frequency as shown in Formula (36)

$$\frac{\Delta\omega}{\omega_0} = -\frac{\Delta W}{W_0} \quad (36)$$

where

$\Delta\omega$  is the shift in the angular resonance frequency;

$\omega_0$  is the angular resonance frequency of the blank cavity;

$\Delta W$  is the change in the stored energy;

$W_0$  is the stored energy of the blank cavity.

The electromagnetic expression of the above terms is shown as follows:

$$\Delta W = \int_{\Delta v} \left[ \epsilon_0 (\epsilon'_r - 1) E \cdot E^* + \mu_0 (\mu'_r - 1) H \cdot H^* \right] dv \quad (37)$$

where

$E$  is the electric field strength;

$H$  is the magnetic field strength;

$\Delta v$  is the sample volume;

$\varepsilon_r$  is the complex relative permittivity of the material:  $\varepsilon_r = \varepsilon'_r - j\varepsilon''_r$ ;

$\mu_r$  is the complex relative permeability of the material:  $\mu_r = \mu'_r - j\mu''_r$ .

The asterisk shows the complex conjugate of the field vector and the terms in square brackets are integrated over the volume of the sample.

$$W_0 = \frac{1}{2} \int_V [\varepsilon_0 \mathbf{E} \cdot \mathbf{E}^* + \mu_0 \mathbf{H} \cdot \mathbf{H}^*] dv \quad (38)$$

where the integral is over the volume of the cavity.

$V$  is the volume of the cavity.

The resonance cavity perturbation method is a classical method and it enables the permeability evaluation over a broad frequency range using the same sample in the range of different cavities of different resonance frequencies. After a small sample is put into a region of the strongest magnetic field strength and zero electric field strength parts of a cavity, the resonance frequency shifts proportionally to the magnetic susceptibility of the material ( $\mu'_r$ ) and the cavity loss factor increases with the loss of the material ( $\mu''_r$ ). [1]<sup>1</sup> The perturbation evaluated in the cavity with a small coupling factor indicates that the connected loads at the outside will have a small influence on the results.

## 5.6.2 Permeability evaluation

### 5.6.2.1 General

If the sample is small and located in the regions of a maximum of  $H$  and an electric field strength  $E$  of zero in the cavity, the energy change in the cavity is proportional to the permeability of the sample. The method to characterize the material as shown above is called the resonance cavity perturbation method. The permeability of the sample is written as shown in Formula (39)

$$\begin{aligned} \mu'_r &= 1 + \frac{V}{\alpha \Delta v} \left( \frac{f_0 - f_s}{f_0} \right) \\ \mu''_r &= \frac{V}{2\alpha \Delta v} \left( \frac{1}{Q_s} - \frac{1}{Q_0} \right) \end{aligned} \quad (39)$$

where

$V$  is the volume of the cavity;

$\Delta v$  is the volume of the sample;

$\alpha$  is the factor defined by the sample position and the cavity mode;

$f_0$  is the resonance frequency of the blank cavity;

$f_s$  is the resonance frequency of the sample installed cavity;

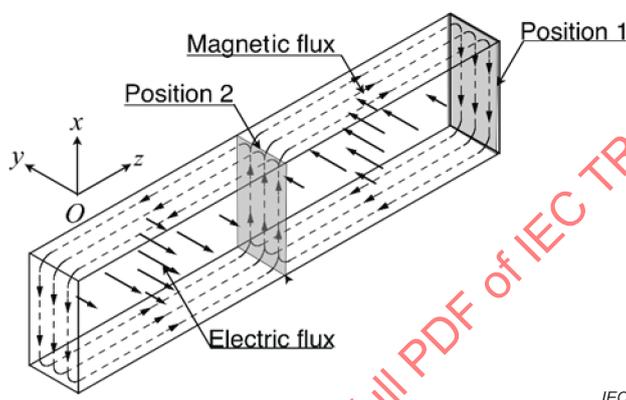
$Q_0$  is the  $Q$  factor of the blank cavity;

$Q_s$  is the  $Q$  factor of the sample installed cavity.

<sup>1</sup> Numbers in square brackets refer to the Bibliography.

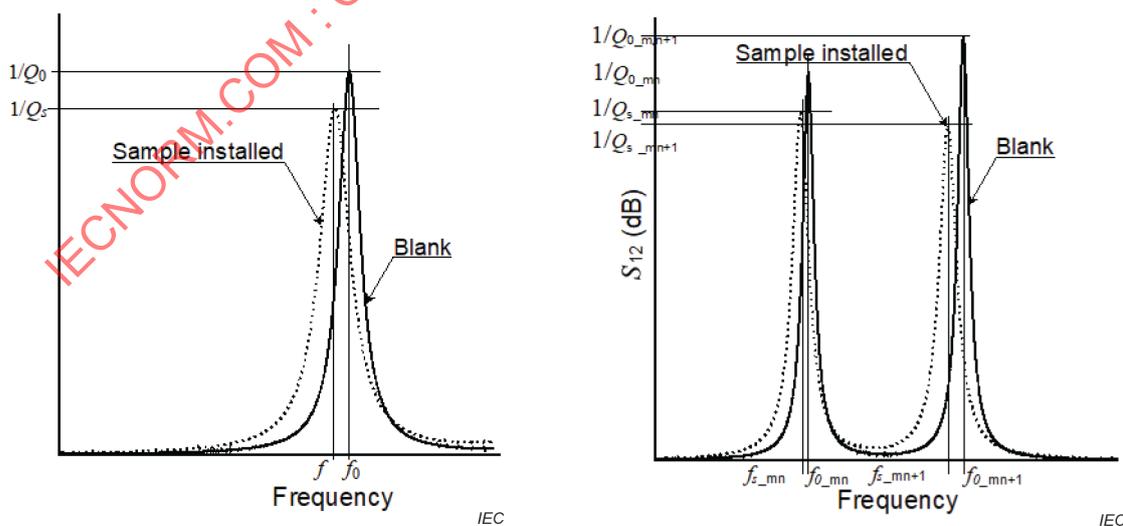
The formula shows that the real part of the permeability is described by the resonance frequency shift ratio and the imaginary part is described by the increase of the cavity loss. A clear one-to-one relationship between the complex permeability and the frequency shift ratio or the loss increase is confirmed by the formula, and the measurement accuracy of the resonance characteristic is essential in the permeability evaluation.

The resonance cavity perturbation method has been established for a resonance cavity of a single resonance frequency and the permeability measurement for one frequency was considered. If a rectangular waveguide  $TE_{012}$  cavity is used as the resonance cavity, the regions of a maximum of  $H$  and an electric field strength  $E$  of zero are found at the centre and ends of the cavity as shown in Figure 36 (Position 1 and Position 2). Therefore no magnetic field is applied to both ends of the sample. The installation of the sample in this area of intrinsic permeability is evaluated without the depolarization field.



**Figure 36 – Electromagnetic flux to evaluate permeability in the harmonic resonance cavity resonator**

Two examples for the resonance characteristics change are shown in Figure 37. Figure 37a) shows the resonance curve change observed in the single frequency resonator. Figure 37b) shows the resonance frequency change in a cavity with two resonance frequencies.

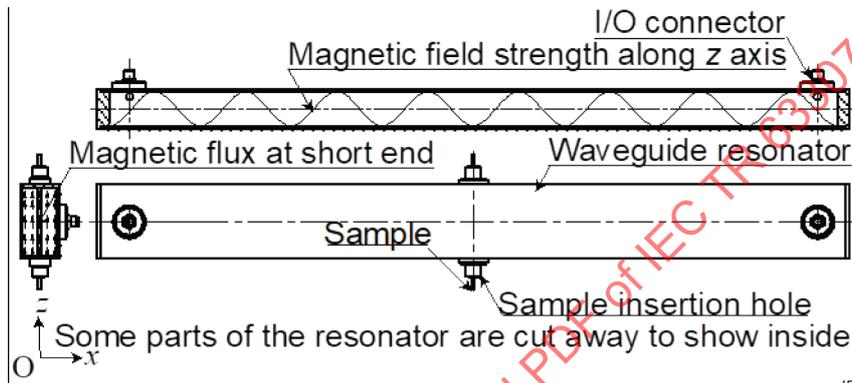


a) Single resonance frequency

b) Two resonance frequencies cavity

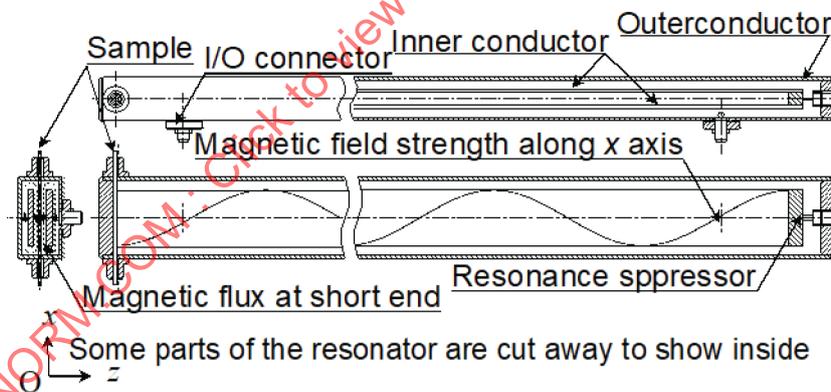
**Figure 37 – Example of the resonance characteristics change**

A rectangular waveguide shorted at both ends will resonate at those frequencies for which the length is equal to an integral multiple of a half wavelength in the waveguide. If only a single mode such as  $TE_{10}$  is found in the waveguide, this can be called a harmonic resonance cavity because the resonance will be observed at the harmonic number,  $n$ , of the waveguide mode [22]. It is proposed here to use the resonator to evaluate the frequency characteristics of materials by the resonance cavity perturbation method. The dimensions of the waveguide resonator become very big at values lower than 2 GHz. A TEM-mode resonator is appropriate in this frequency range but the magnetic field distribution of the TEM-mode resonator with a single line is not the same as the waveguide resonator. The magnetic field distribution of a TEM-mode resonator with two parallel plates as the centre conductor is the same as that shown in Figure 34. This structure of the resonator was used at the frequency range from 250 MHz to 2 GHz. Examples of the structure of the resonators and the resonance frequencies are shown in Figure 38 and Figure 39 respectively.



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Figure 38 – Cavity resonator for 3,6 GHz to 7,2 GHz



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Figure 39 – Cavity resonator for 0,25 GHz to 2 GHz

The numbers of the resonance frequencies in the band are defined by the length of the resonator. A longer resonator length increases the numbers of the resonance frequencies in the band and gives accurate frequency characteristics of the material. However, a small difference between the resonance frequencies makes it difficult to evaluate the frequency shift caused by the insertion of the sample. Four to eight resonance frequencies in the band are appropriate. Examples are shown in Figure 40.

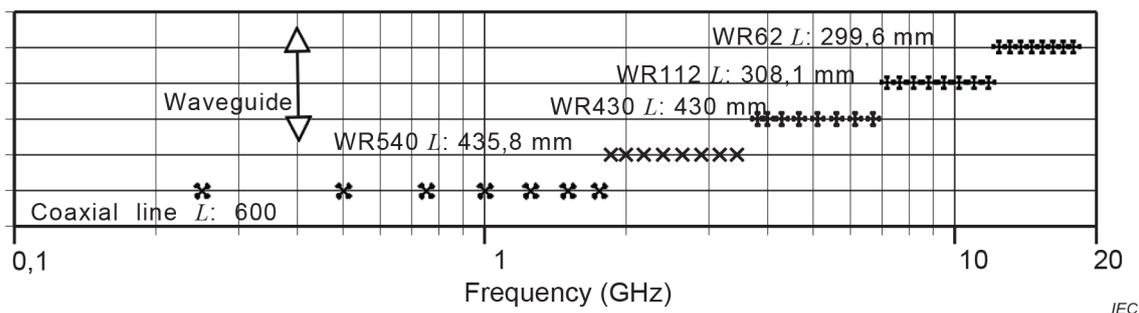


Figure 40 – Examples of resonance frequencies

An example of the harmonic resonance curves in the C-band is shown in Figure 41.

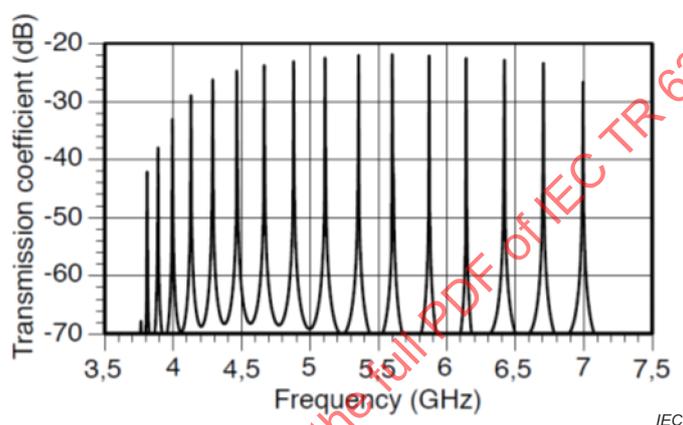


Figure 41 – Example of the resonance curves of a harmonic resonance cavity

#### 5.6.2.2 Measurement frequency and accuracy

Frequency	: $250 \text{ MHz} \leq f \leq 18 \text{ GHz}$
Relative permeability	: $-5 \leq \mu'_r \leq 50$
	$0,1 \leq \mu''_r \leq 10$
	x, y or z axis
Accuracy	: order of significant digits: 2

#### 5.6.2.3 Sample dimensions

##### 5.6.2.3.1 Permeability evaluation parallel to the plane

- Cut out a tape.
- Width: < 2 mm
- Thickness: < 2 mm
- Length: > 100 mm

##### 5.6.2.3.2 Permeability evaluation orthogonal to the plane

- Punch out small disks and stack.
- Diameter: < 2 mm
- Length: > 50 mm

The samples prepared as described above are shown in Figure 42 as examples.

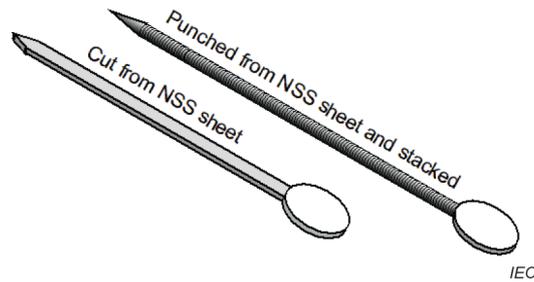


Figure 42 – Examples of samples

#### 5.6.2.4 Environment

Room temperature: 15 °C to 35 °C.

#### 5.6.2.5 Apparatus

##### 5.6.2.5.1 General

The measuring system of the permeability of the NSS is constructed by the network analyzer, and the harmonic resonance cavity resonates in the defined frequency band (see Figure 43).

##### 5.6.2.5.2 Network analyzer

The frequency range of the network analyzer should cover the resonance frequency of the harmonic resonance cavity resonator, and the dynamic range of the analyzer should be more than 40 dB.

##### 5.6.2.5.3 Test fixture

The resonance frequencies of the harmonic resonance cavity should have enough numbers of the resonance frequency to evaluate the frequency characteristics of NSS; more than six resonance frequencies in the band would be a good number. A personal computer used to calculate the complex permeability from the data given by the network analyzer should be provided.

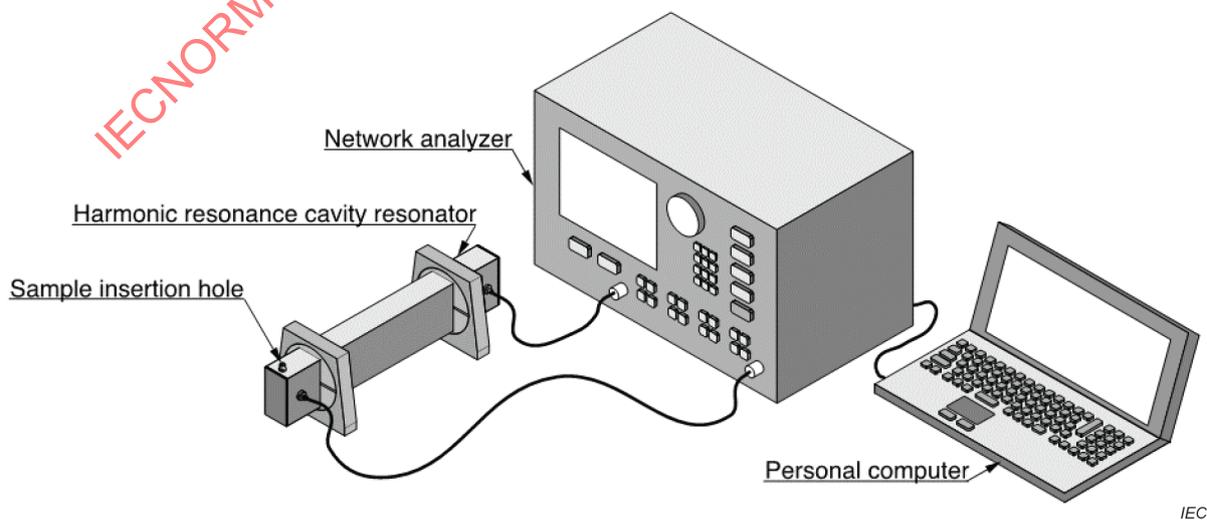


Figure 43 – Measuring system

### 5.6.2.6 Measurement procedure of permeability

#### 5.6.2.6.1 Resonance characteristics ( $f_{0\_mn}$ and $Q_{0\_mn}$ ) evaluation of the blank cavity

##### 5.6.2.6.1.1 General

The resonance frequency,  $f_{0\_mn}$  and the  $Q$  factor,  $Q_{0\_mn}$ , of the blank cavity are measured. The suffix mn means  $n$ -th resonance frequency or the  $Q$  factor in the m-band cavity.

##### 5.6.2.6.1.2 $f_{REF\_mn}$ , the $n$ -th resonance frequency of the m-band cavity

Resonance frequency,  $f_{REF\_mn}$ , of the reference sample installed cavity is measured to define the proportional factor. The suffix mn means the  $n$ -th resonance peak in the m-band cavity.

##### 5.6.2.6.1.3 Calibration factor ( $\alpha_{mn}$ ) definition of the cavity

The proportional factor  $\alpha_{mn}$  is given by inserting a nonmagnetic good conductor as a reference sample because the permeability of the good conductor is 0 in this frequency range. A copper rod will be favourable as a good conductor. The proportional factor  $\alpha_{mn}$  is calculated by the obtained data and the following formula:

$$\alpha_{mn} = \frac{V}{\Delta v_{REF}} \left( \frac{f_{REF\_mn} - f_{0\_mn}}{f_{0\_mn}} \right) \quad (40)$$

where

$V$  is the volume of the cavity;

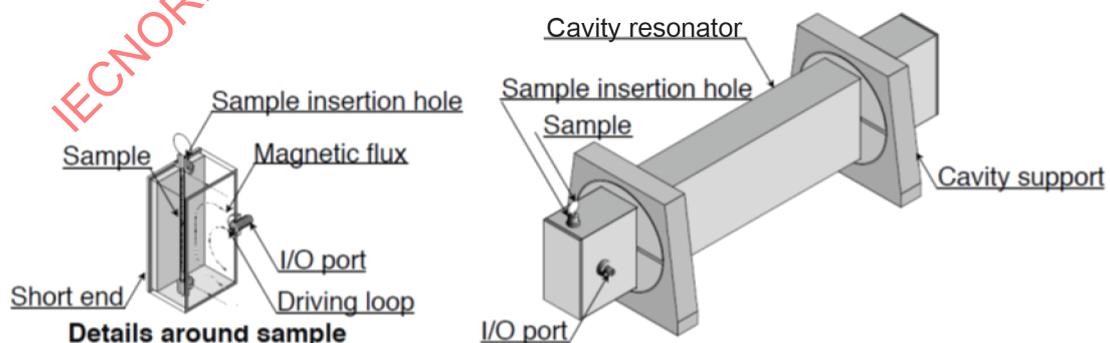
$\Delta v_{REF}$  is the volume of the reference sample in the cavity;

$f_{0\_mn}$  is the  $n$ -th resonance frequency in the m-band vacant cavity;

$f_{REF\_mn}$  is the  $n$ -th resonance frequency in m-band cavity with the reference sample.

##### 5.6.2.6.2 Sample installation

Insert the sample into the sample installation hole of the cavity as shown in Figure 44.



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Figure 44 – Sample installation in the cavity for the permeability measurement

### 5.6.2.6.3 Resonance characteristics ( $f_{s\_mn}$ and $Q_{s\_mn}$ ) evaluation of the sample

The resonance frequency,  $f_s$ , and the Q factor,  $Q_s$ , of the cavity installing the sample are measured by a network analyzer. The suffix mn means the resonance characteristics of the  $n$ -th resonance frequency in the m-band cavity.

### 5.6.2.6.4 Calculation of the permeability

The real part and the imaginary part of the relative permeability of the  $n$ -th resonance frequency of the m-band cavity are given as shown in Formula (41) and (42), respectively.

$$\mu'_{r\_mn} = 1 + \frac{V}{\alpha_{mn}\Delta v} \left( \frac{f_{0\_mn} - f_{s\_mn}}{f_{0\_mn}} \right) \quad (41)$$

$$\mu''_{r\_mn} = \frac{V}{2\alpha_{mn}\Delta v} \left( \frac{1}{Q_{s\_mn}} - \frac{1}{Q_{0\_mn}} \right) \quad (42)$$

where

$V$  is the volume of the cavity;

$\Delta v$  is the volume of the sample in the cavity;

$\alpha_m$  is the proportional constant;

$f_0$  is the resonance frequency of the empty cavity;

$f_s$  is the resonance frequency of the sample installed cavity;

$Q_0$  is the  $Q$  factor of the empty cavity;

$Q_s$  is the  $Q$  factor of the sample installed cavity.

### 5.6.2.7 Expression of the results

The obtained results are plotted in terms of the measured frequency and the complex relative permeability as shown in Figure 45. The permeability of a good conductor is 0. If a good conductor is included in the sample, the consistency of the measurement is confirmed and the deviation of the relative permeability of the conductor from 0 corresponds to the accuracy of the measurement. Permeability<sub>xy</sub> is the permeability in the sheet plane. Permeability<sub>z</sub> is the permeability perpendicular to the sheet. The subscript after the under score is the sample name.

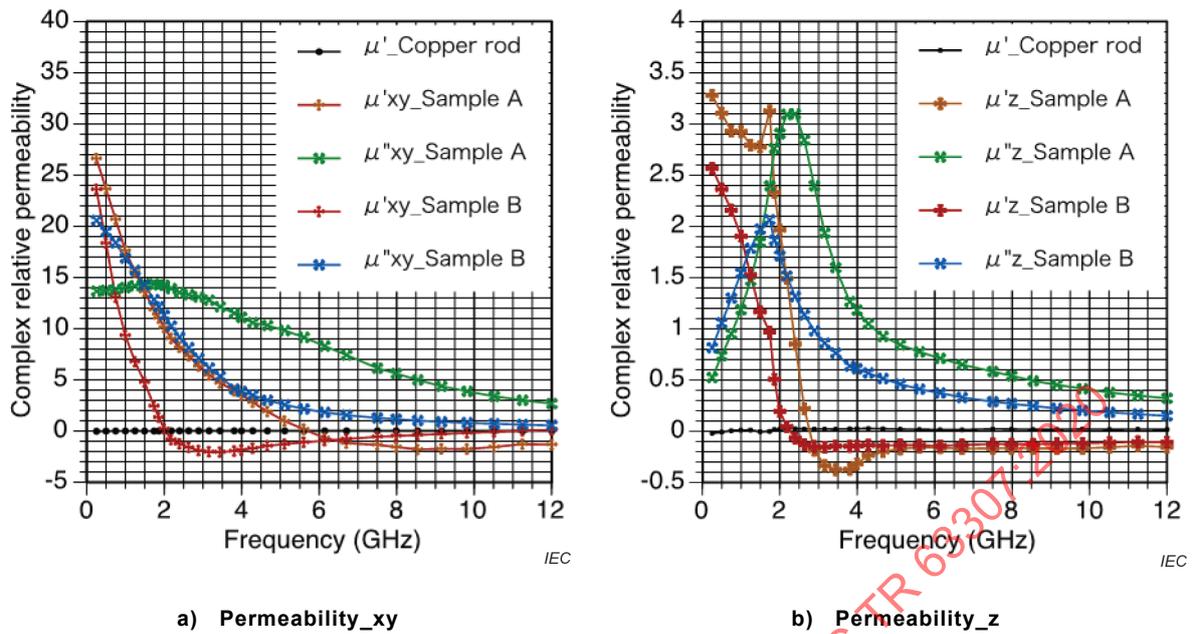


Figure 45 – Measured results of the permeability for Sample A and B and a copper rod

### 5.6.3 Permittivity evaluation

#### 5.6.3.1 General

The permittivity of the NSS material is strongly frequency dependent and anisotropic, just as the permeability of the NSS is strongly frequency dependent and anisotropic.

If a small sample is installed at the region of the maximum electric field strength and the magnetic field strength is zero in the cavity as shown in Figure 46, the energy change in the cavity is proportional to the permittivity of the sample. The method to characterize the material as shown above is called the resonance cavity perturbation method [21].

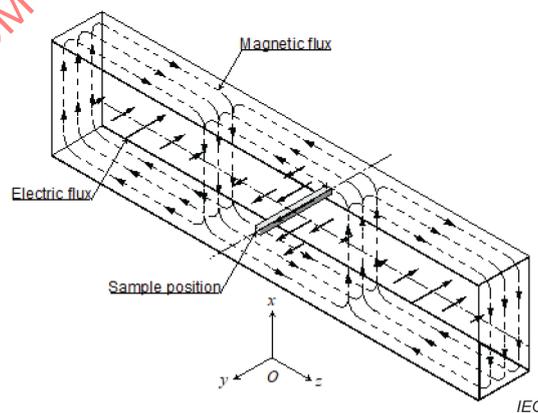


Figure 46 – Electromagnetic flux to evaluate permittivity in the harmonic resonance cavity resonator

The evaluation of the permittivity will be carried out by the same procedure as the permeability was evaluated. The permittivity of the sample is described as shown in Formula (43). The suffix  $m_n$  means the  $n$ -th resonance frequency or the  $Q$  factor in the  $m$ -band cavity.



#### 5.6.3.4 Environment

Room temperature is 15 °C to 35 °C.

#### 5.6.3.5 Apparatus

Network analyzer

Test fixture

#### 5.6.3.6 Measurement procedure of the permittivity

##### 5.6.3.6.1 Resonance characteristics ( $f_{0\_mn}$ and $Q_{0\_mn}$ ) evaluation of the blank test fixture

Measure the resonance frequency  $f_{0\_mn}$  and the  $Q$  factor  $Q_{0\_mn}$  of the cavity where  $m$  is the measurement band, S or C, and  $n$  is the order of the resonance peak in the band.

##### 5.6.3.6.2 Sample installation

Insert the sample into the sample installation hole of the cavity as shown in Figure 47.

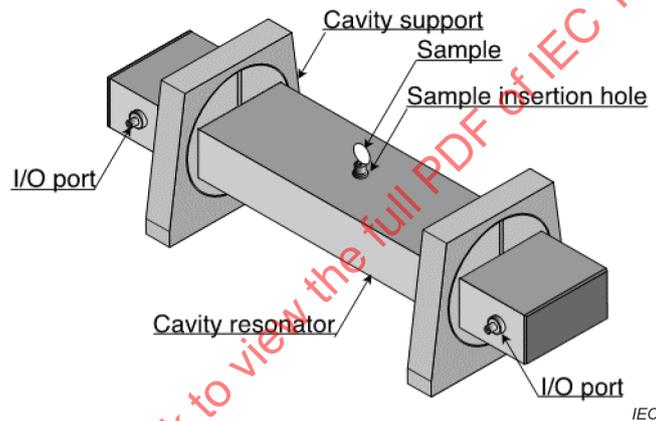


Figure 47 – Sample installation in the cavity for the permittivity measurement

##### 5.6.3.6.3 Resonance characteristics ( $f_{s\_mn}$ and $Q_{s\_mn}$ ) evaluation of the sample

Measure the resonance frequency  $f_{mn}$  and the  $Q$  factor  $Q_{s\_mn}$  of the sample installed cavity. The suffix  $m$  is the measurement band, S or C, and  $n$  is the order of the resonance peak in the band.

##### 5.6.3.6.4 Calculation of the permeability

The relative permeability of the  $n$ -th resonance frequency of the  $m$  band cavity is given as follows

$$\epsilon'_{r\_mn} = 1 + \frac{V}{2\Delta v} \left( \frac{f_{0\_mn} - f_{s\_mn}}{f_{0\_mn}} \right) \quad (44)$$

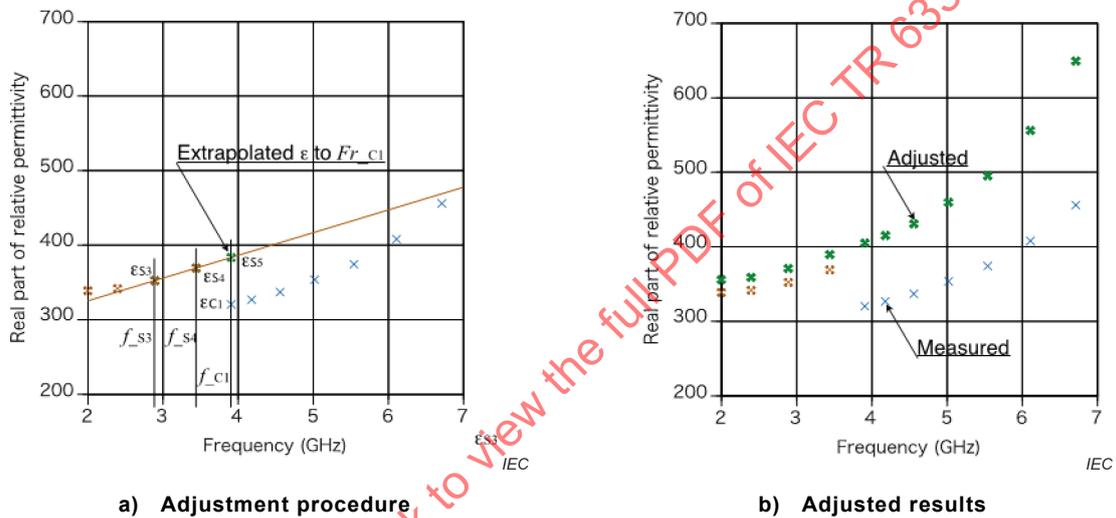
$$\epsilon''_{r\_mn} = \frac{V}{4\Delta v} \left( \frac{1}{Q_{s\_mn}} - \frac{1}{Q_{0\_mn}} \right) \quad (45)$$

where

- $V$  is the volume of the cavity;
- $\Delta v$  is the volume of the sample in the cavity;
- $f_0$  is the resonance frequency of the m-band blank cavity;
- $f_s$  is the resonance frequency of the m-band sample installed cavity;
- $Q_{0\_mn}$  is the  $n$ -th  $Q$  factor of the m-band vacant cavity;
- $Q_{s\_mn}$  is the  $n$ -th  $Q$  factor of the m-band sample installed cavity.

**5.6.3.7 Adjustment of the permittivity decrease caused by the depolarization field**

The measurements of the permittivity are carried out by the resonators constructed by the rectangular waveguide resonators for the S-band and C-band. Examples of the measurement and the adjusted results are shown in Figure 48a) and Figure 48b), respectively.



**Figure 48 – Adjustment procedure and adjusted results**

Adjustment of the permittivity by using the results of two cavities with different heights has been carried out as follows.

- 1) Calculate the polarizability  $\chi' = \epsilon' - 1$ .
- 2) Estimate the polarizability  $\chi'_{S5\_meas}$  at  $f_{C1}$  by extrapolating  $\chi'_{S3\_meas}$  and  $\chi'_{S4\_meas}$

$$\chi'_{S5} = \epsilon'_{S5\_meas} - 1 = \frac{\epsilon'_{S4\_meas} - \epsilon'_{S3\_meas}}{f_{S4} - f_{S3}}(f_{C1} - f_{S3}) + \epsilon'_{S3\_meas} - 1 \tag{46}$$

- 3)  $\chi'_{S5\_meas}$  would be the polarizability if measured at  $f_{C1}$  in the S-band cavity.
- 4) The polarizability of the material measured at the S-band cavity with the cavity height,  $h_S$ , is  $\chi'_{S\_meas}$  and at the C-band cavity with the cavity height,  $h_C$ , is  $\chi'_{C\_meas}$ .
- 5) Suppose that the electrical length of the stick sample equals the cavity height,  $h_S$  or  $h_C$ , and the depolarization factor of the sample is inversely proportional to the length of the stick. The depolarization factors of the samples can be described as follows:

$$N_S = \frac{k}{h_S} \text{ and } N_C = \frac{k}{h_C} \tag{47}$$

where

$k$  is the proportional constant.

The proportional constant,  $k$ , is given by the formula shown below by using the measured polarizability  $\chi'_{C1}$  and the supposed polarizability  $\chi'_{S5}$ :

$$k = \frac{\frac{1}{\chi'_{C1\_meas}} - \frac{1}{\chi'_{S5\_meas}}}{\frac{1}{h_C} - \frac{1}{h_S}} \quad (48)$$

- 6) The real part of the adjusted dielectric constants at the measured frequencies can be calculated by using Formula (48) and the measured results as follows:

$$\varepsilon'_{Sn\_adjust} = \chi'_{Sn\_adjust} + 1 = \frac{\chi'_{Sn\_meas}}{1 - N_S \chi'_{Sn\_meas}} + 1 \quad (49)$$

$$\varepsilon'_{Cn\_adjust} = \chi'_{Cn\_adjust} + 1 = \frac{\chi'_{Cn\_meas}}{1 - N_C \chi'_{Cn\_meas}} + 1 \quad (50)$$

where

suffix S or C is the name of the band;

suffixes adjust and meas are the adjusted value and measured value;

$n$  is the resonance frequency number in the bands.

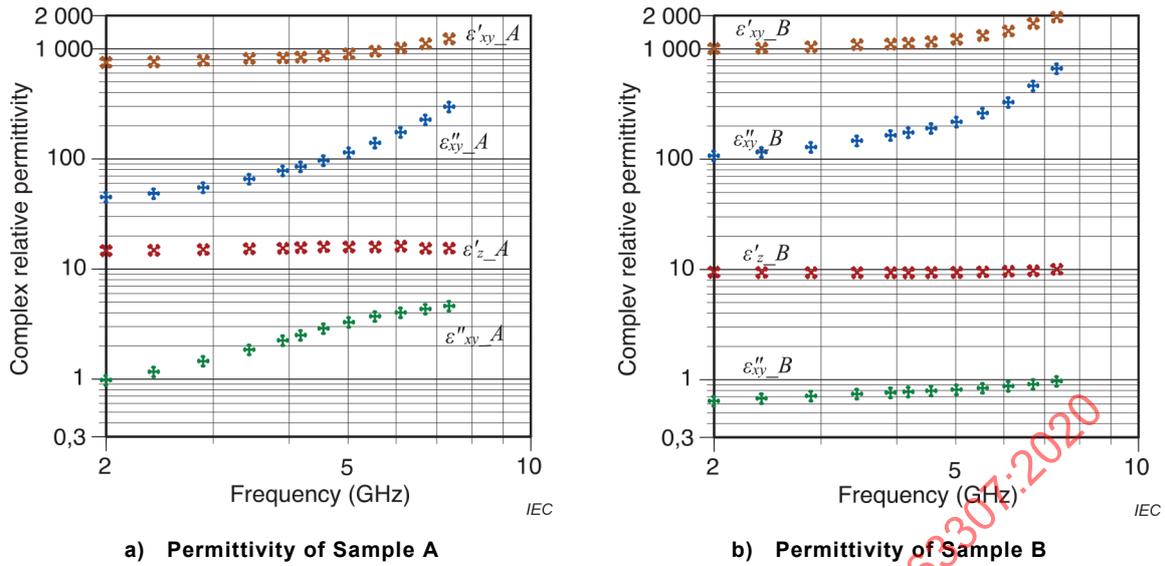
- 7) The imaginary part of the adjusted dielectric constants at the measured frequencies can be calculated by using Formula (50) and the measured results are as follows:

$$\varepsilon''_{Sn\_adjust} = (1 + N_S \chi''_{Sn\_meas})^2 \quad (51)$$

$$\varepsilon''_{Cn\_adjust} = (1 + N_C \chi''_{Cn\_meas})^2 \quad (52)$$

### 5.6.3.8 Expression of the results

The adjusted results are shown in Figure 49. The suffixes in Figure 49 mean the direction of the electric field and the sample name, respectively.



**Figure 49 – Measured results of the permittivity for the two samples, A and B**

The seamless connections of the adjusted results are confirmed from the results above. Although no adjustment for the imaginary part has been carried out in the procedure, the seamless connection shown in the above results confirmed that the adjustment would be consistent.

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## Annex A (informative)

### Derivation of the complex relative permeability of the inductance method

The self-inductance  $L$  of the one-turn coil in Figure 3 is expressed by:

$$L = \frac{Z}{j\omega} = \frac{1}{I} \int_s B ds =$$

$$\frac{\mu_0}{2\pi} (\mu_r - 1) F + \frac{\mu_0}{2\pi} F_0 =$$

$$\frac{\mu_0}{2\pi} (\mu_r' - 1) F - j \frac{\mu_0}{2\pi} \mu_r'' F + \frac{\mu_0}{2\pi} F_0 =$$

$$\frac{x_{\text{NSS}}}{\omega} - j \frac{r_{\text{NSS}}}{\omega} + L_{\text{Short}} \quad (\text{A.1})$$

where

$$F = h \ln \left( \frac{b}{a} \right) \quad (\text{A.2})$$

$$F_0 = h_0 \ln \left( \frac{b_0}{a_0} \right) \quad (\text{A.3})$$

$r_{\text{NSS}}$  and  $x_{\text{NSS}}$  are the real part and imaginary part of the self-inductance with the NSS sample.  $L_{\text{Short}}$  is the self-inductance without the NSS sample. They are given as follows, respectively:

$$r_{\text{NSS}} = \omega \frac{\mu_0}{2\pi} \mu_r'' F \quad (\text{A.4})$$

$$x_{\text{NSS}} = \omega L_{\text{NSS}} = \omega \frac{\mu_0}{2\pi} (\mu_r' - 1) F \quad (\text{A.5})$$

$$L_{\text{Short}} = \frac{\mu_0}{2\pi} F_0 \cdot \quad (\text{A.6})$$

The impedance  $Z_{\text{NSS}}$  is due to the effect of the fixture and is expressed by the impedance of the fixture with and without the NSS sample,  $Z_m$  and  $Z_{\text{sm}}$ , as follows:

$$Z_{\text{NSS}} = Z_m - Z_{\text{sm}} = r_m - r_{\text{sm}} + j(x_m - x_{\text{sm}}) =$$

$$r_{\text{NSS}} + jx_{\text{NSS}} = r_{\text{NSS}} + j\omega L_{\text{NSS}} \quad (\text{A.7})$$

where

$$\begin{aligned}
 Z_m &= r_m + jx_m = \\
 r_{\text{fixture}} + jx_{\text{fixture}} + r_{\text{Short}} + j\omega L &= \\
 r_{\text{fixture}} + jx_{\text{fixture}} + r_{\text{Short}} + (r_{\text{NSS}} + j\omega L_{\text{NSS}} + j\omega L_{\text{Short}}) & \quad (\text{A.8})
 \end{aligned}$$

$$\begin{aligned}
 Z_{\text{sm}} &= r_{\text{sm}} + jx_{\text{sm}} = \\
 r_{\text{fixture}} + jx_{\text{fixture}} + r_{\text{Short}} + j\omega L_{\text{Short}} & \quad (\text{A.9})
 \end{aligned}$$

Then, the complex permeability is given by:

$$\mu_r = \frac{2\pi}{\mu_0} \frac{Z_m - Z_{\text{sm}}}{j\omega F} + 1 = \frac{2\pi}{\mu_0} \frac{Z_{\text{NSS}}}{j\omega F} + 1 \quad (\text{A.10})$$

that is,

$$\mu_r' = \frac{2\pi}{\mu_0} \frac{x_m - x_{\text{sm}}}{\omega F} + 1 = \frac{2\pi}{\mu_0} \frac{x_{\text{NSS}}}{\omega F} + 1 \quad (\text{A.11})$$

$$\mu_r'' = \frac{2\pi}{\mu_0} \frac{r_m - r_{\text{sm}}}{\omega F} = \frac{2\pi}{\mu_0} \frac{r_{\text{NSS}}}{\omega F} \quad (\text{A.12})$$

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